



<http://algs4.cs.princeton.edu>

## 4.1 CONNECTED COMPONENTS

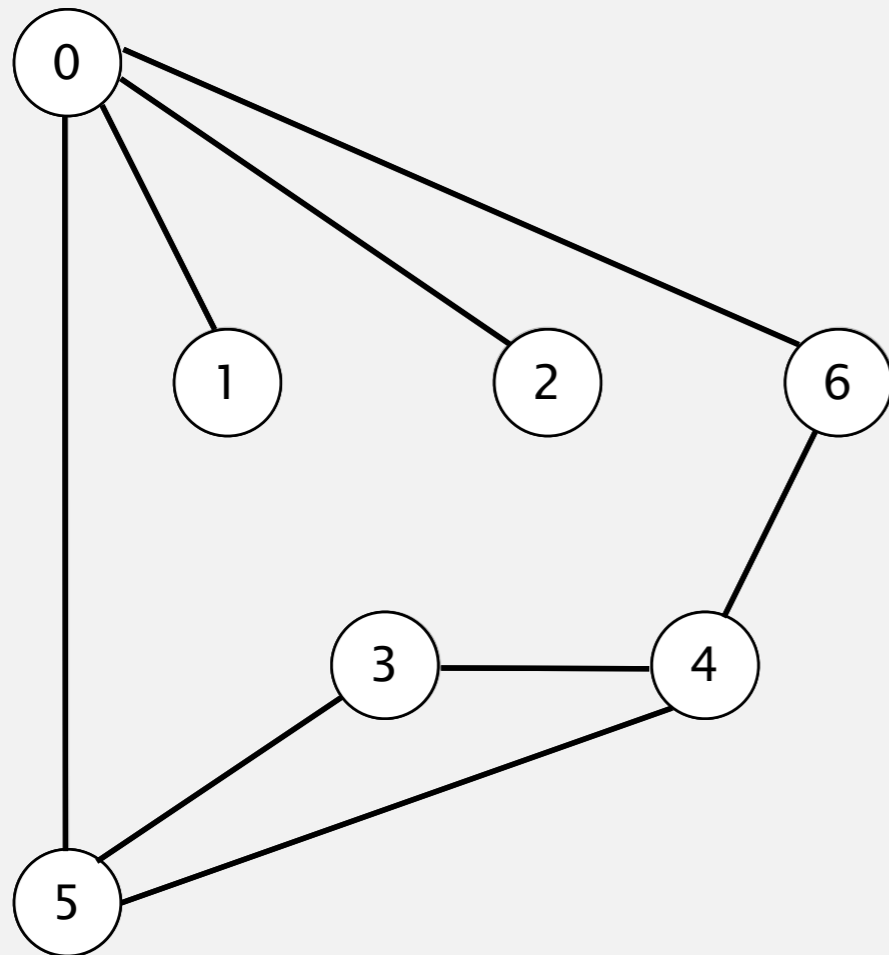
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# Connected components demo

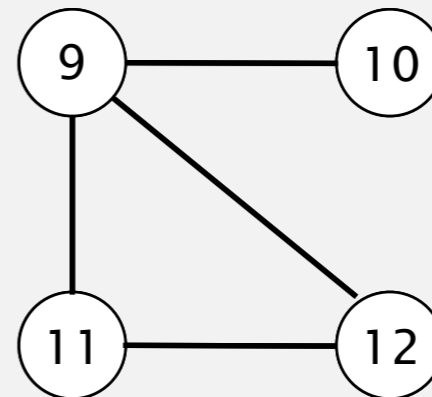
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To visit a vertex  $v$  :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



graph G

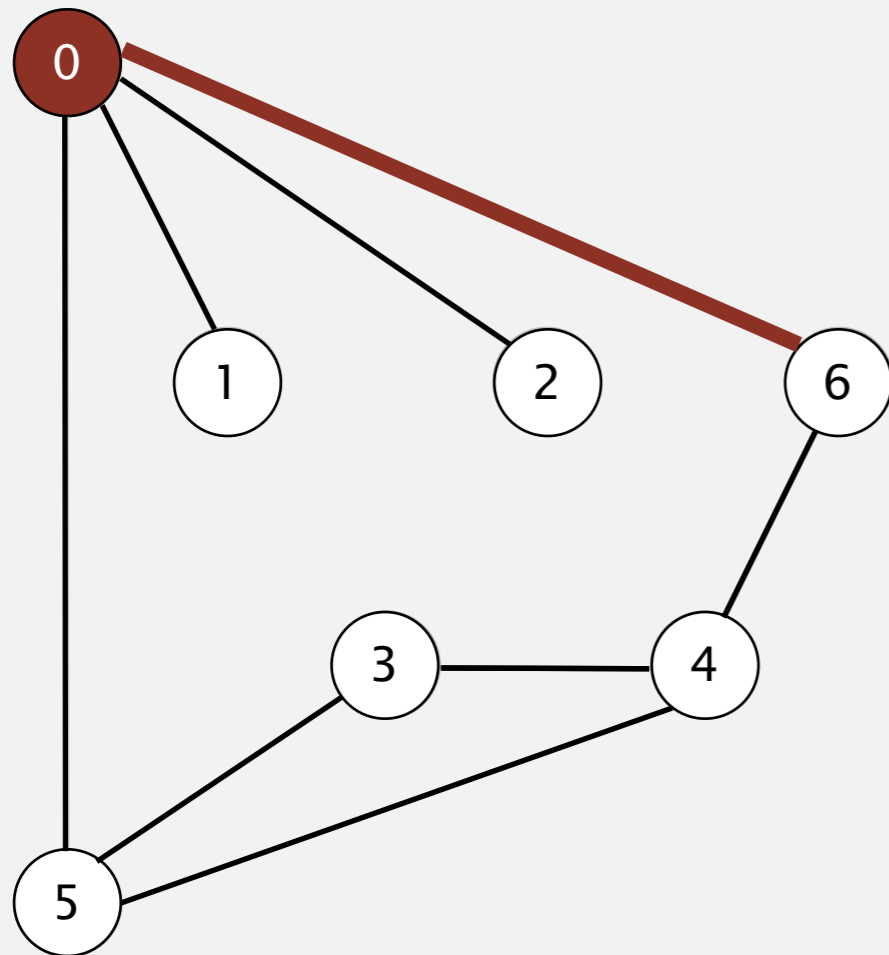


<u>v</u>	<u>marked[]</u>	<u>id[]</u>
0	F	-
1	F	-
2	F	-
3	F	-
4	F	-
5	F	-
6	F	-
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

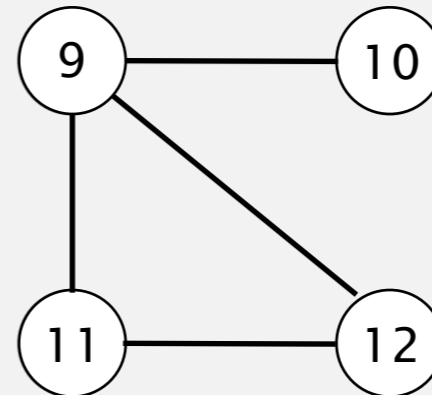
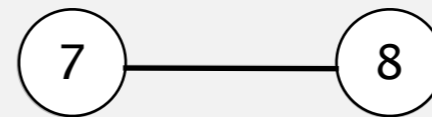
# Connected components demo

To visit a vertex  $v$  :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



visit 0

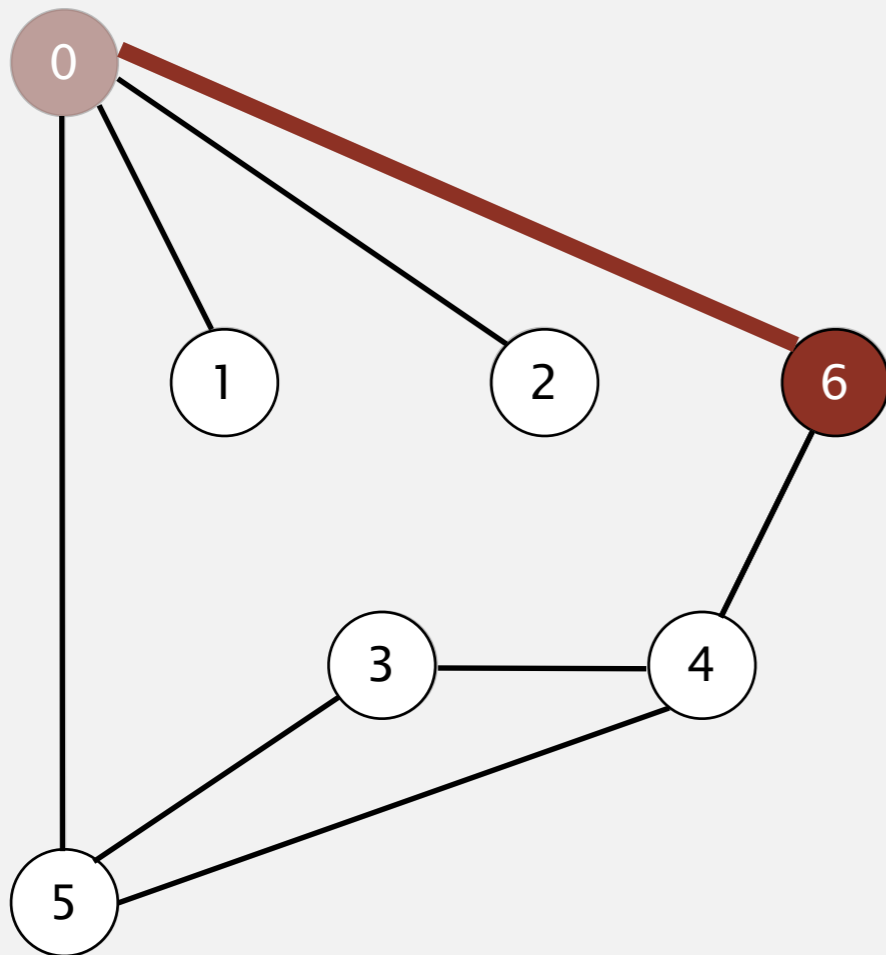


v	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	F	-
4	F	-
5	F	-
6	F	-
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

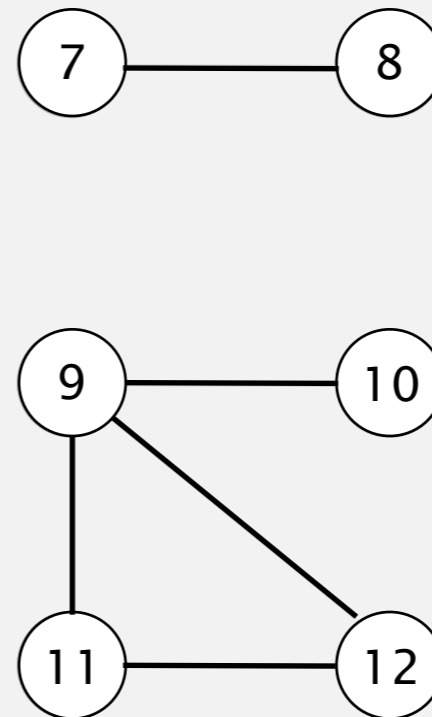
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



visit 6

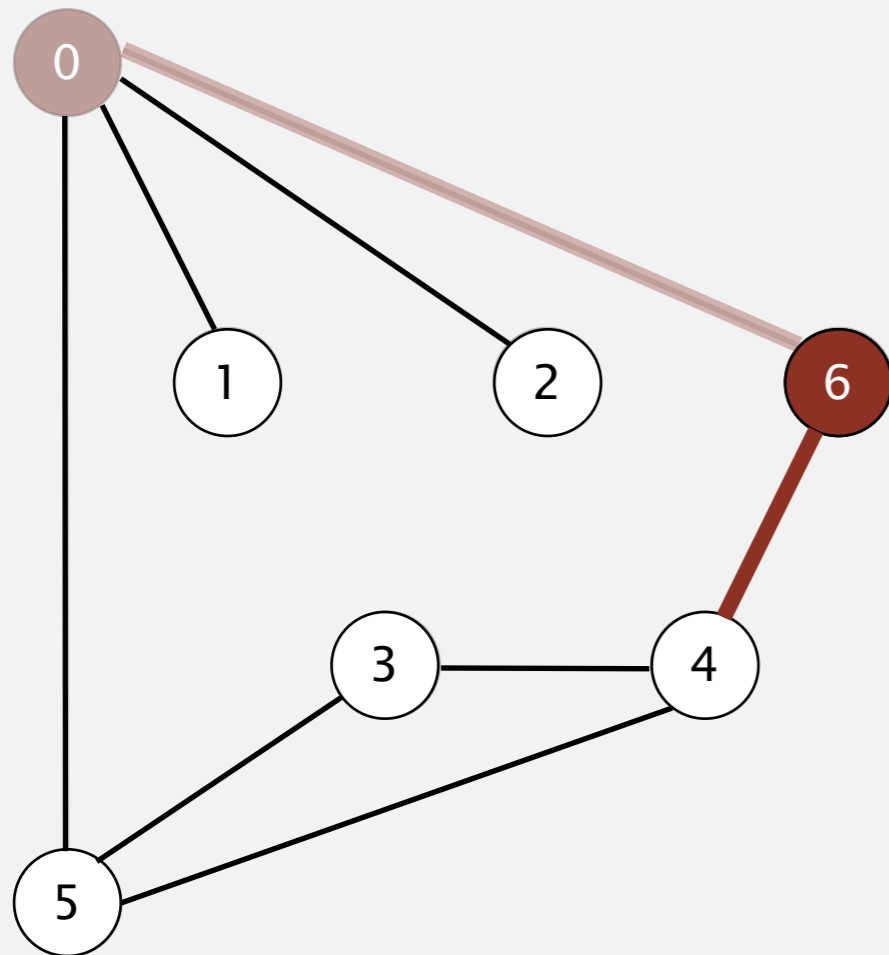


$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	F	-
4	F	-
5	F	-
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

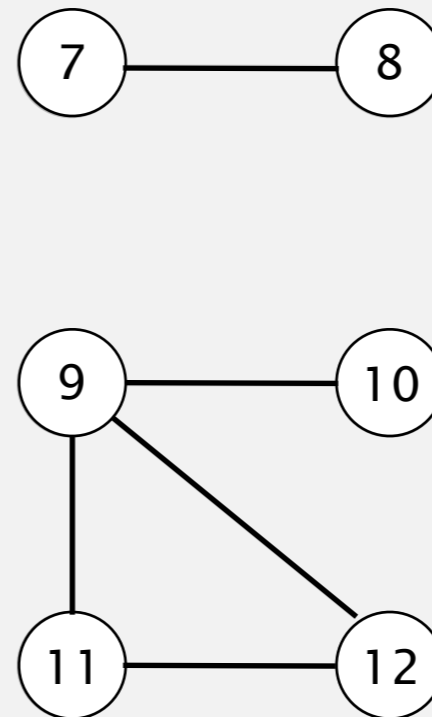
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visit 6

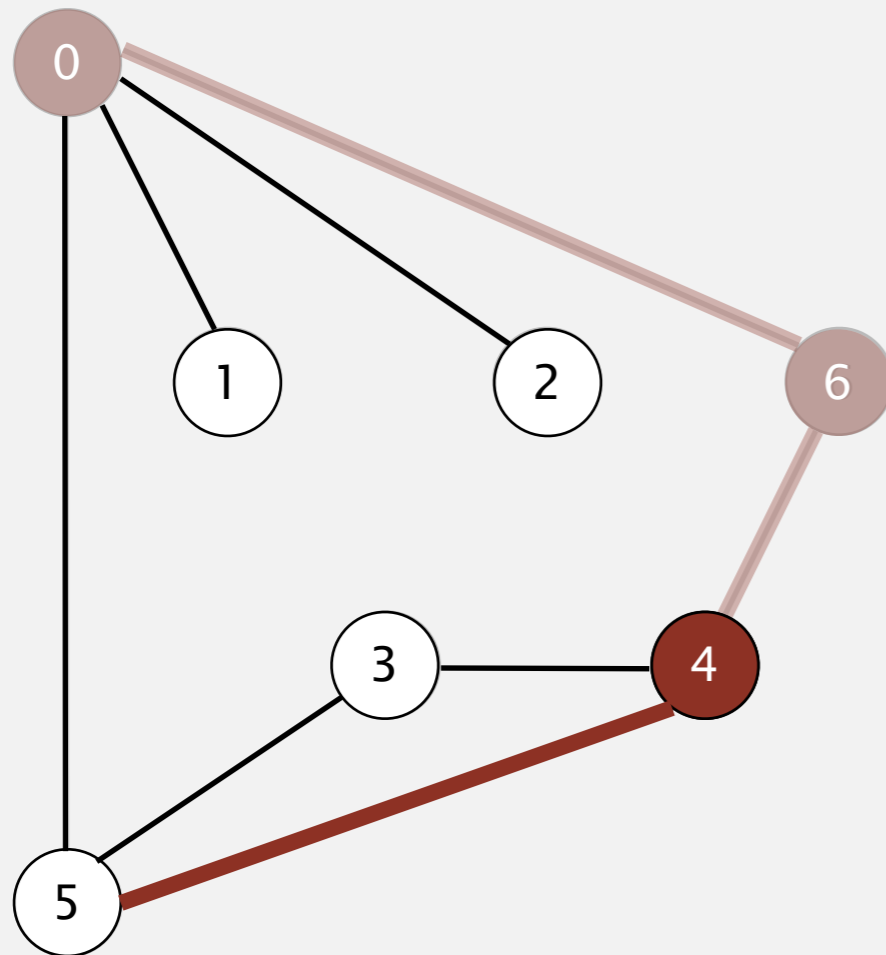


$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	F	-
4	F	-
5	F	-
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

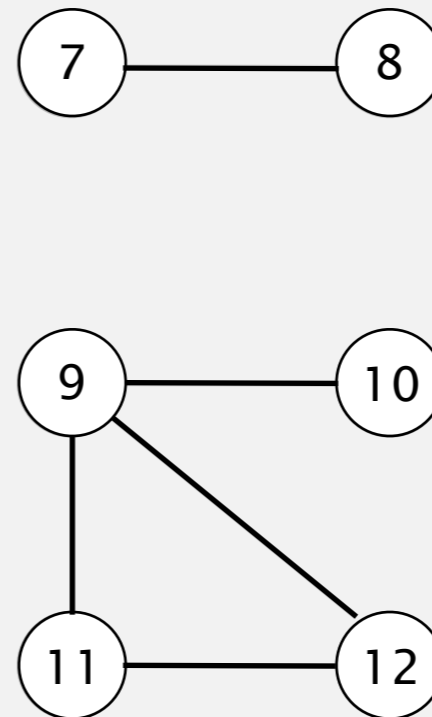
# Connected components demo

To visit a vertex  $v$  :

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- Recursively visit all unmarked vertices adjacent to  $v$ .



visit 4

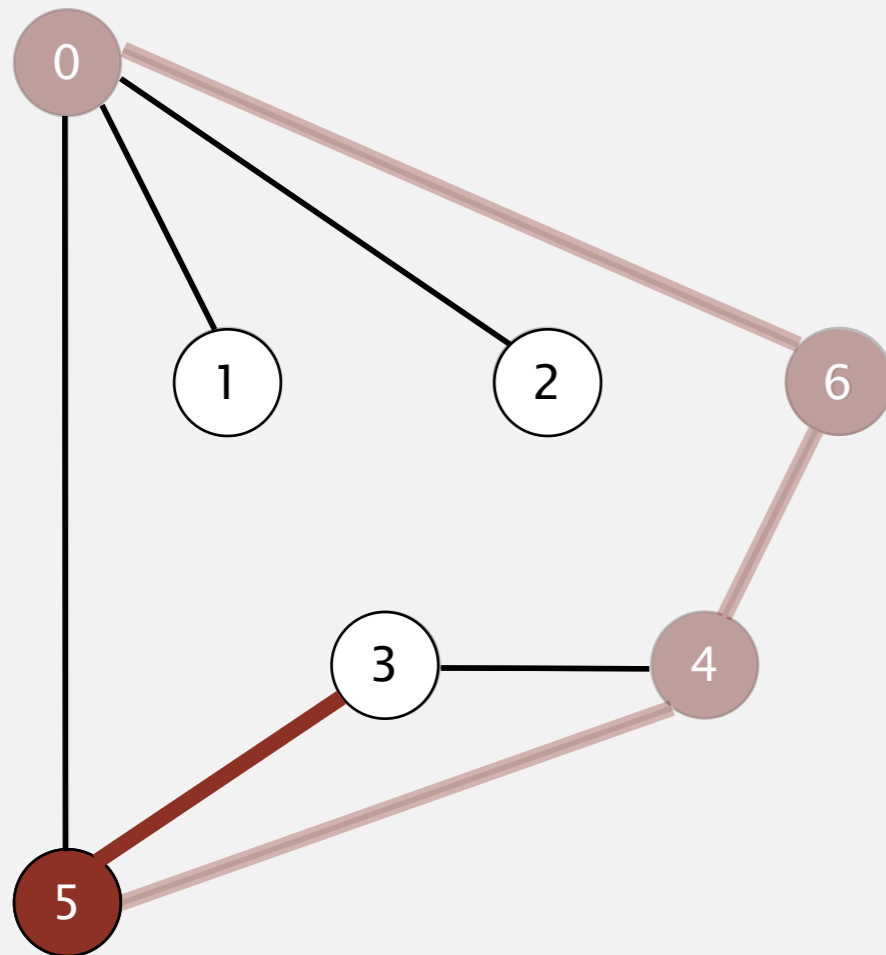


$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	F	-
4	T	0
5	F	-
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

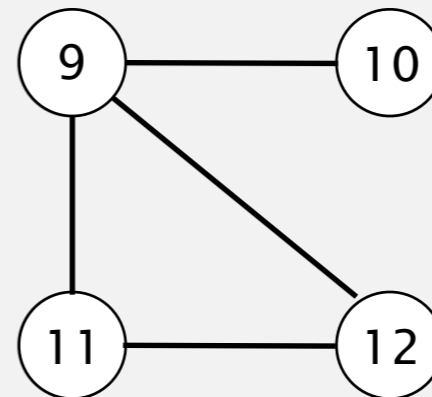
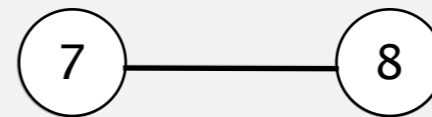
# Connected components demo

To visit a vertex  $v$ :

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- Recursively visit all unmarked vertices adjacent to  $v$ .



visit 5

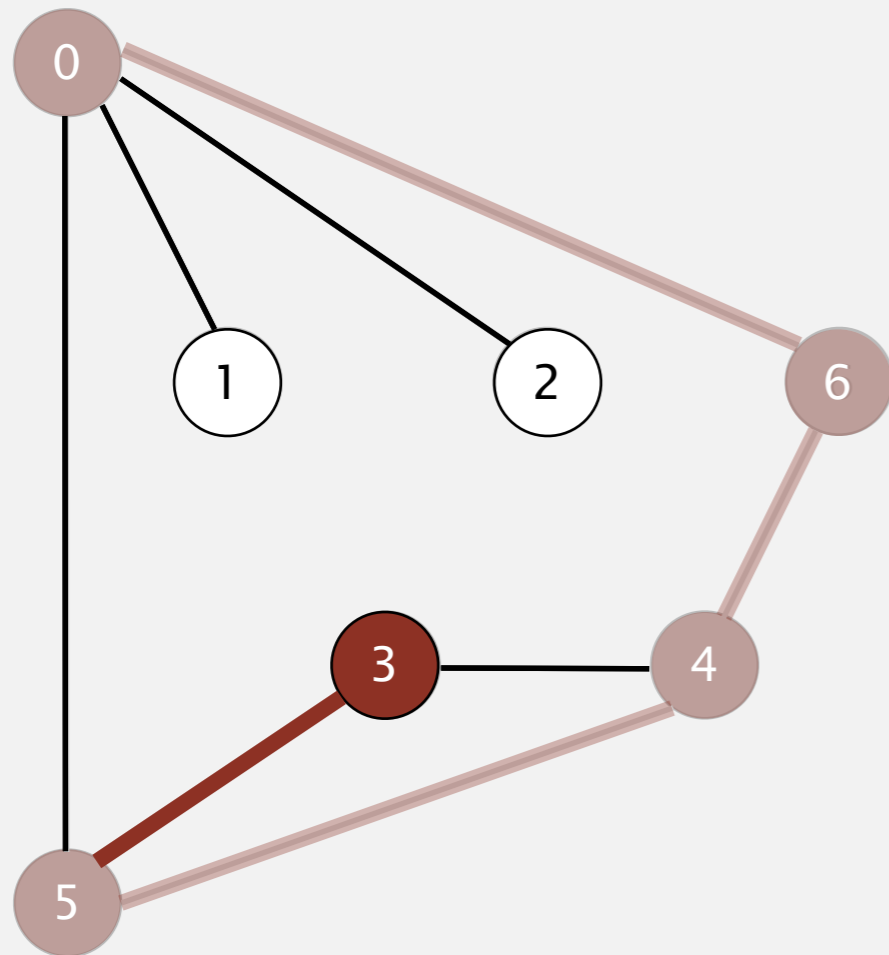


$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	F	-
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

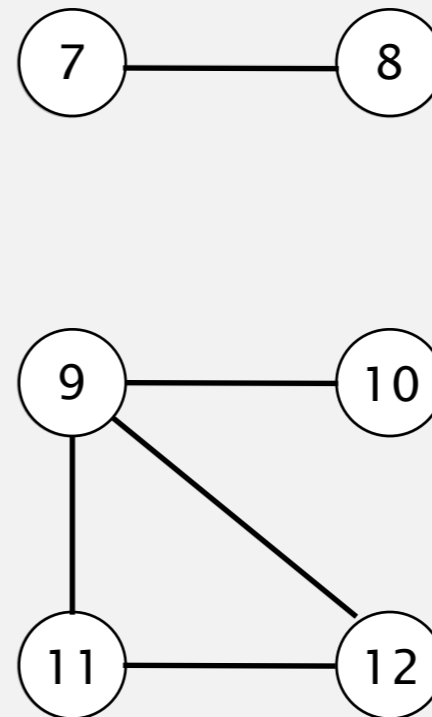
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



visit 3



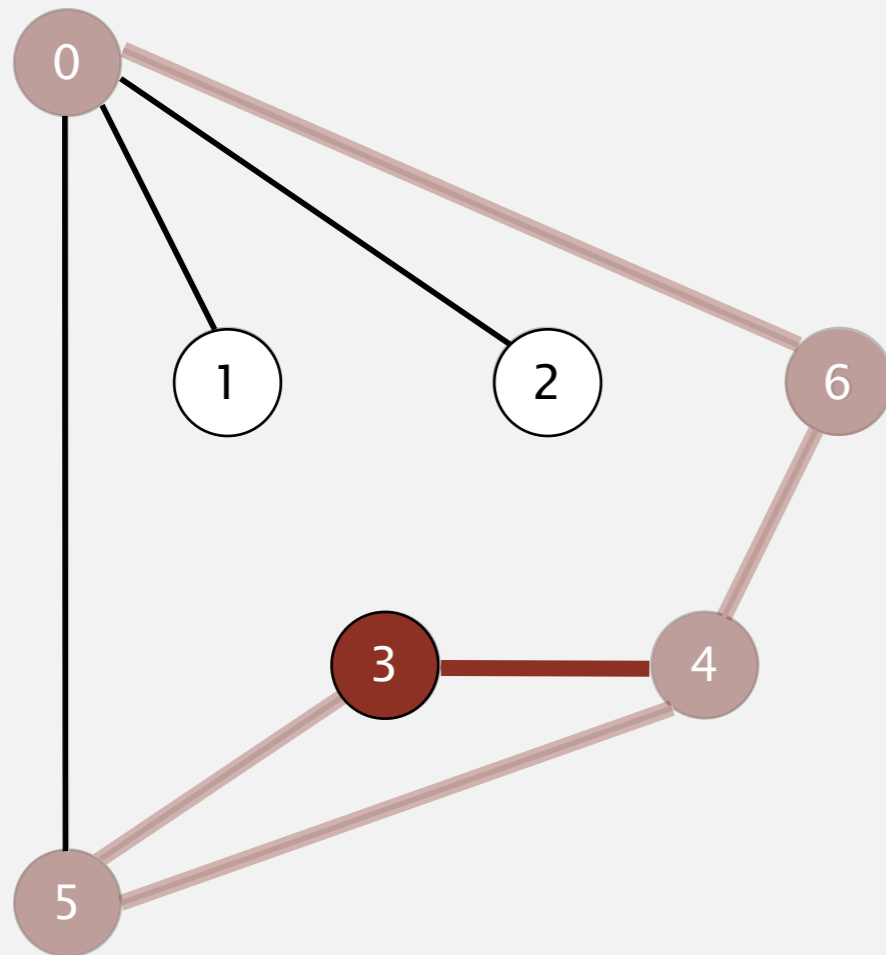
$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-



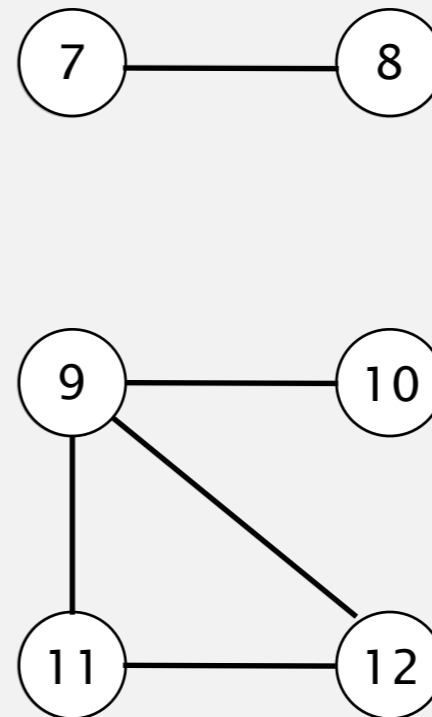
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visit 3

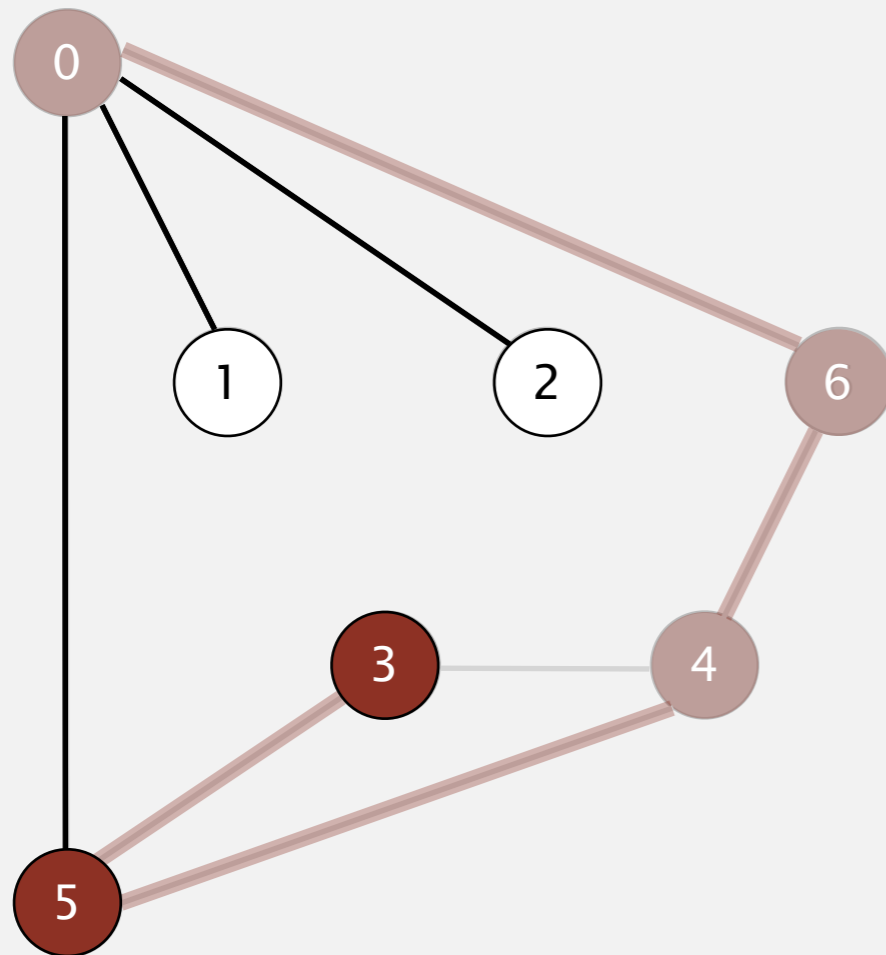


$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

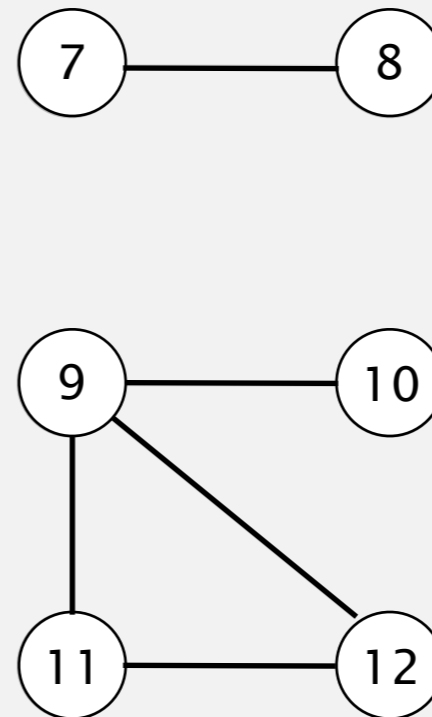
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- Recursively visit all unmarked vertices adjacent to  $v$ .



**3 done**

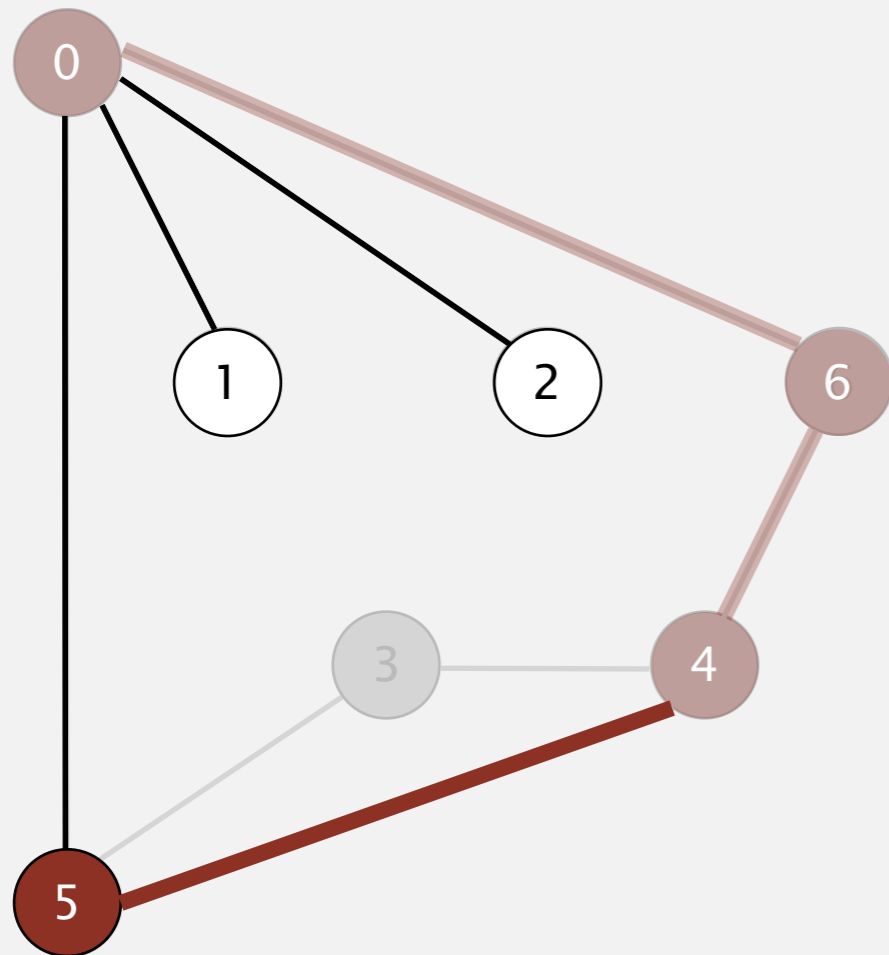


$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

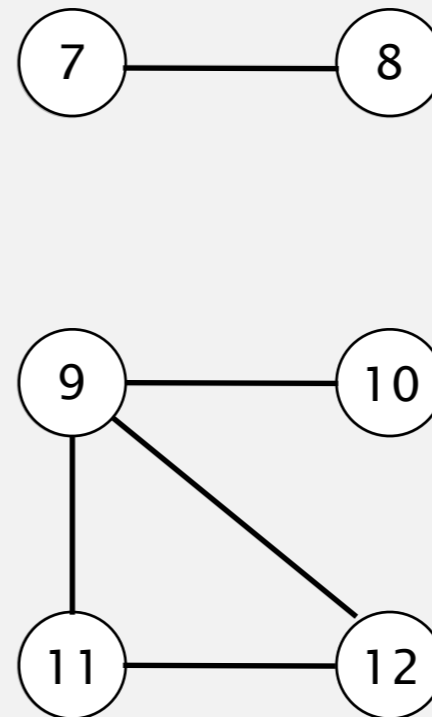
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- Recursively visit all unmarked vertices adjacent to  $v$ .



visit 5

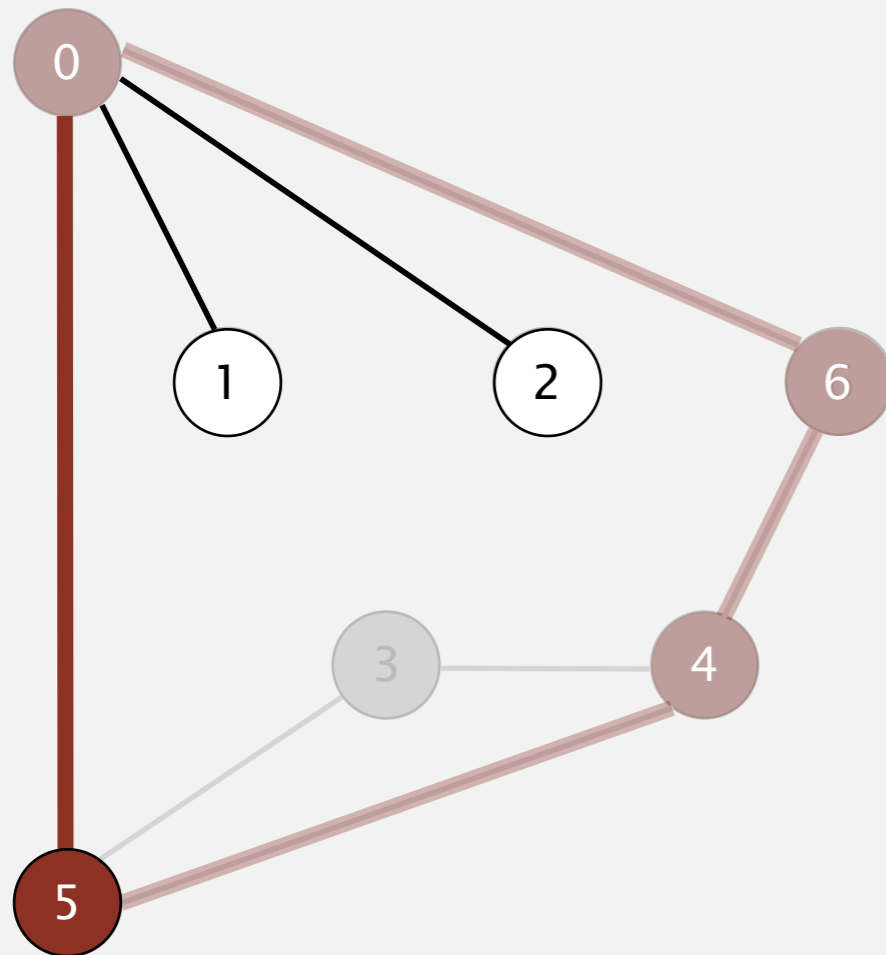


$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

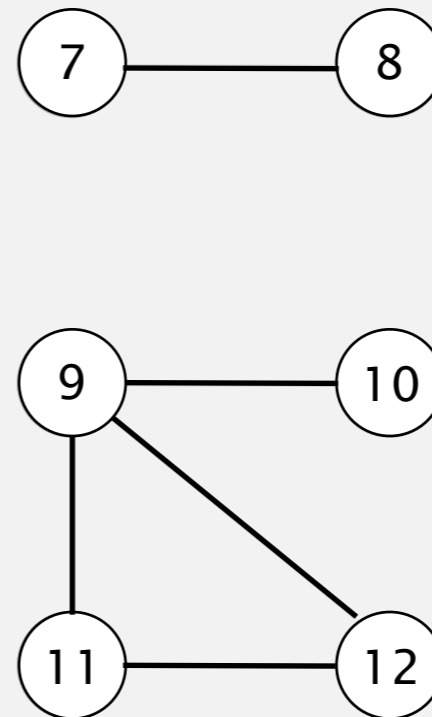
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visit 5

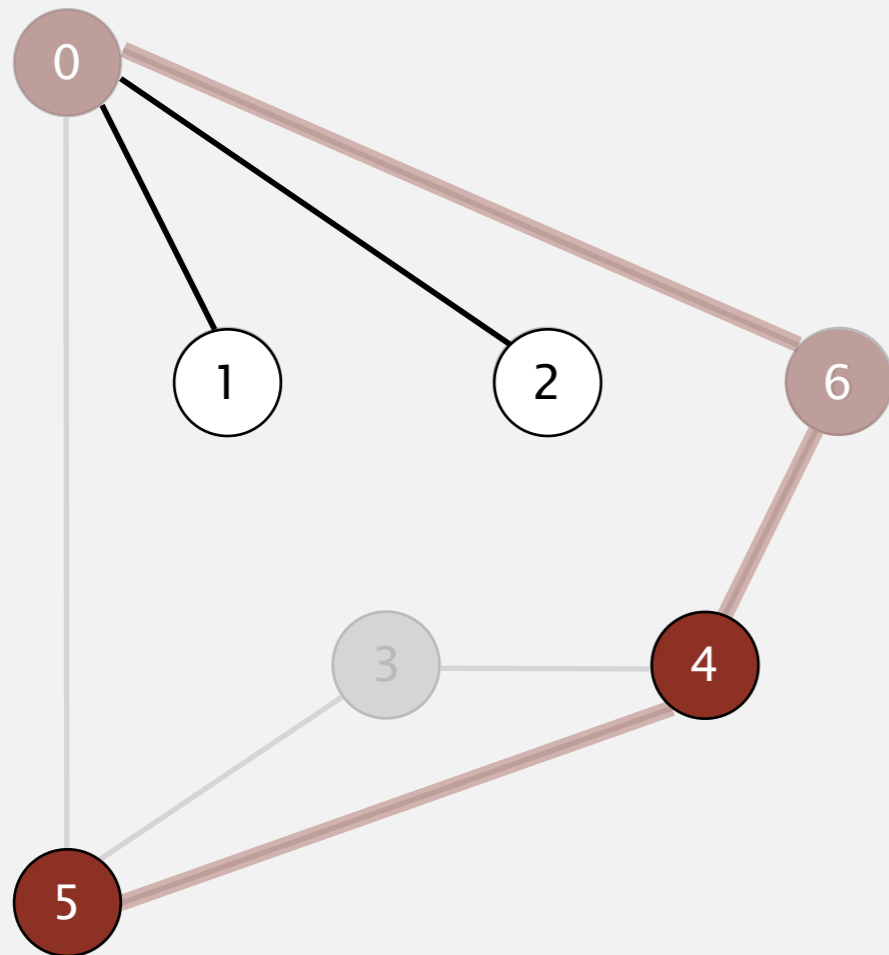


$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

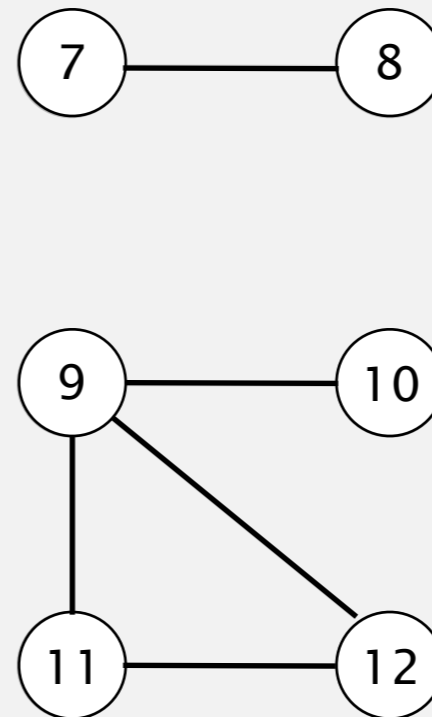
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



**5 done**

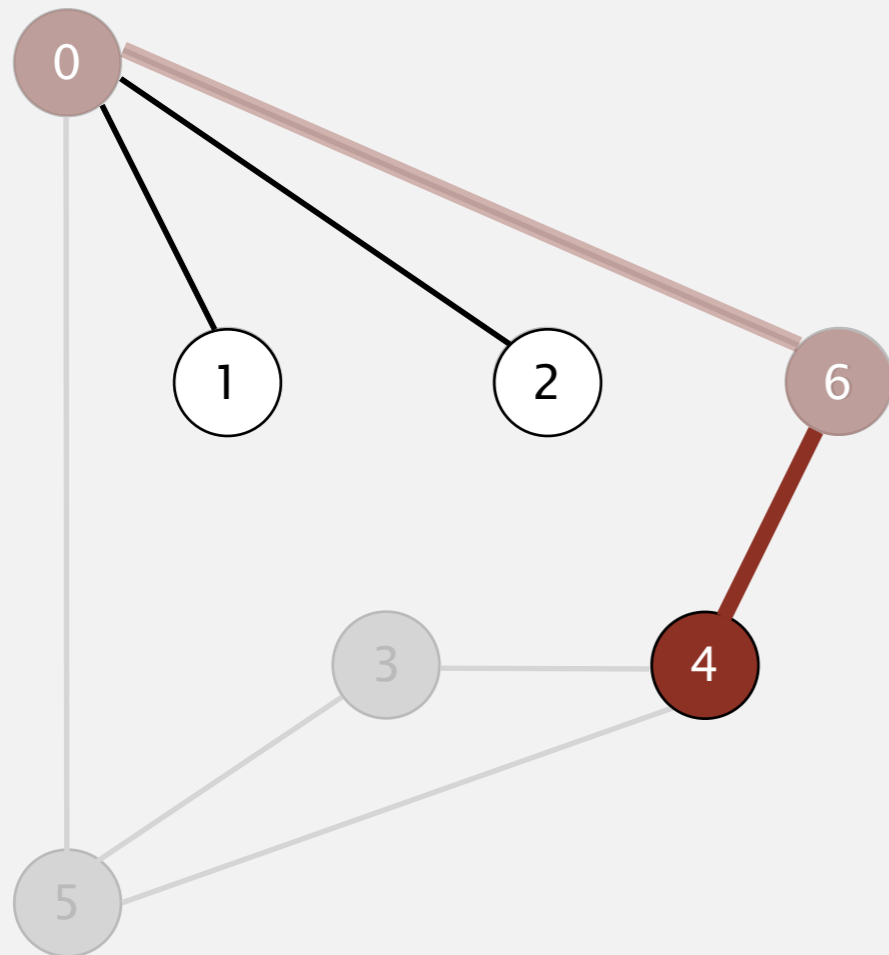


$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

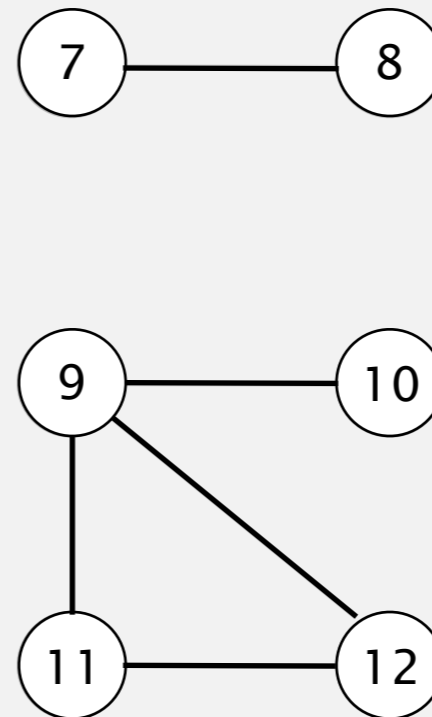
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visit 4

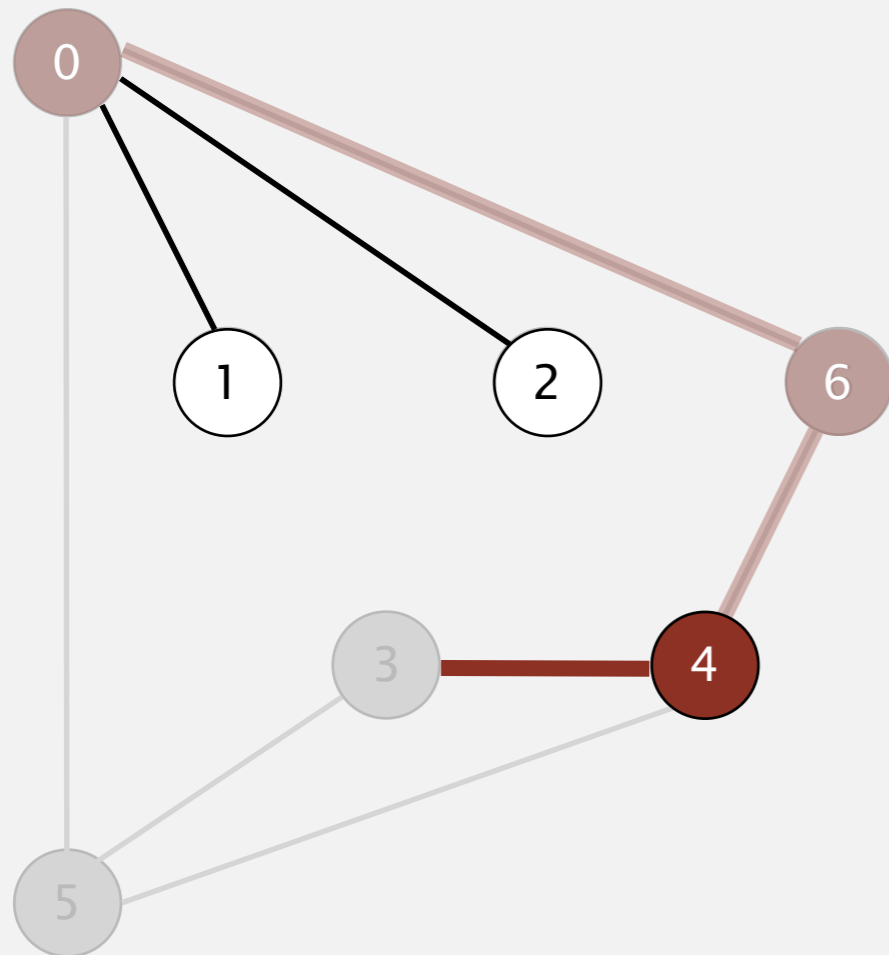


$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

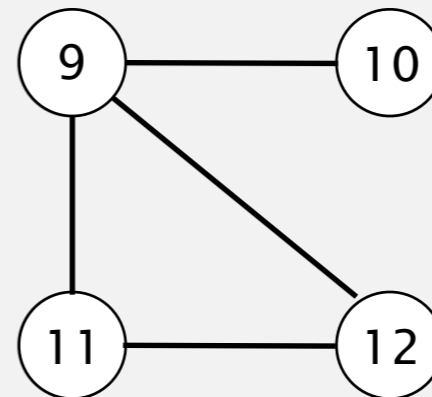
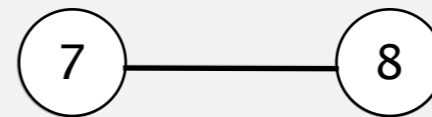
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visit 4

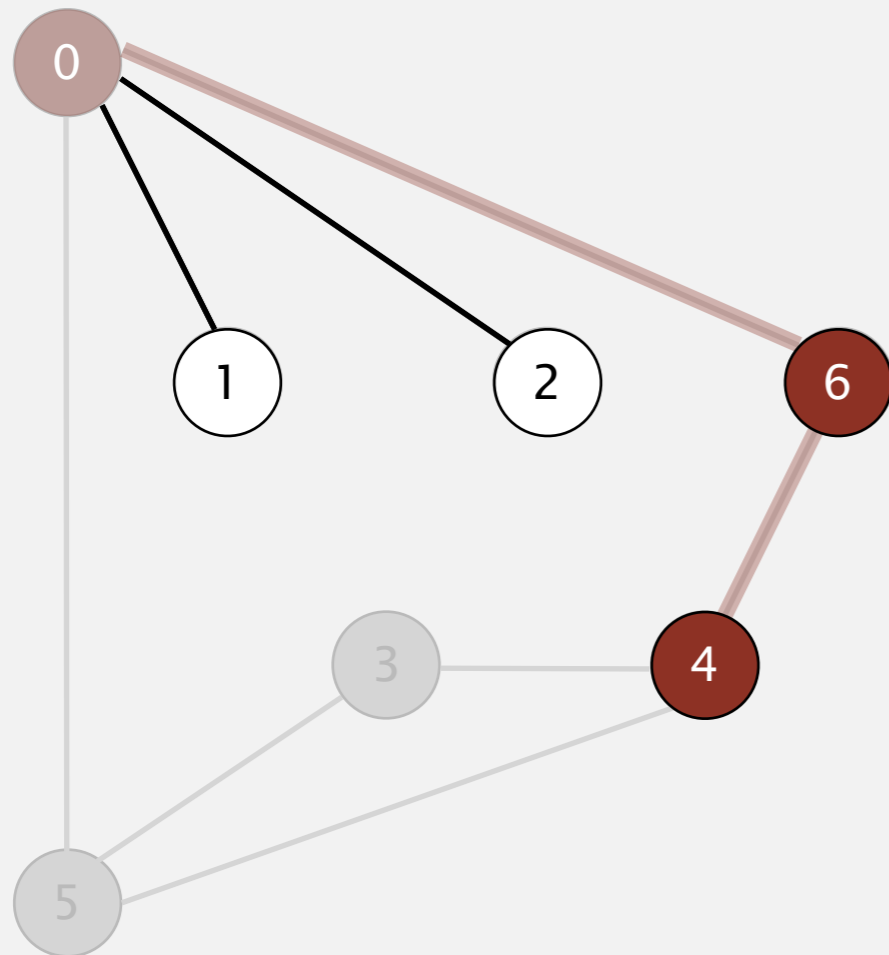


$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

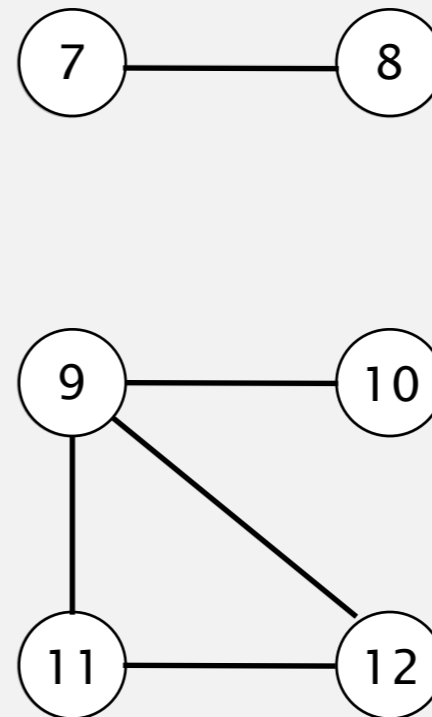
# Connected components demo

To visit a vertex  $v$  :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



**4 done**



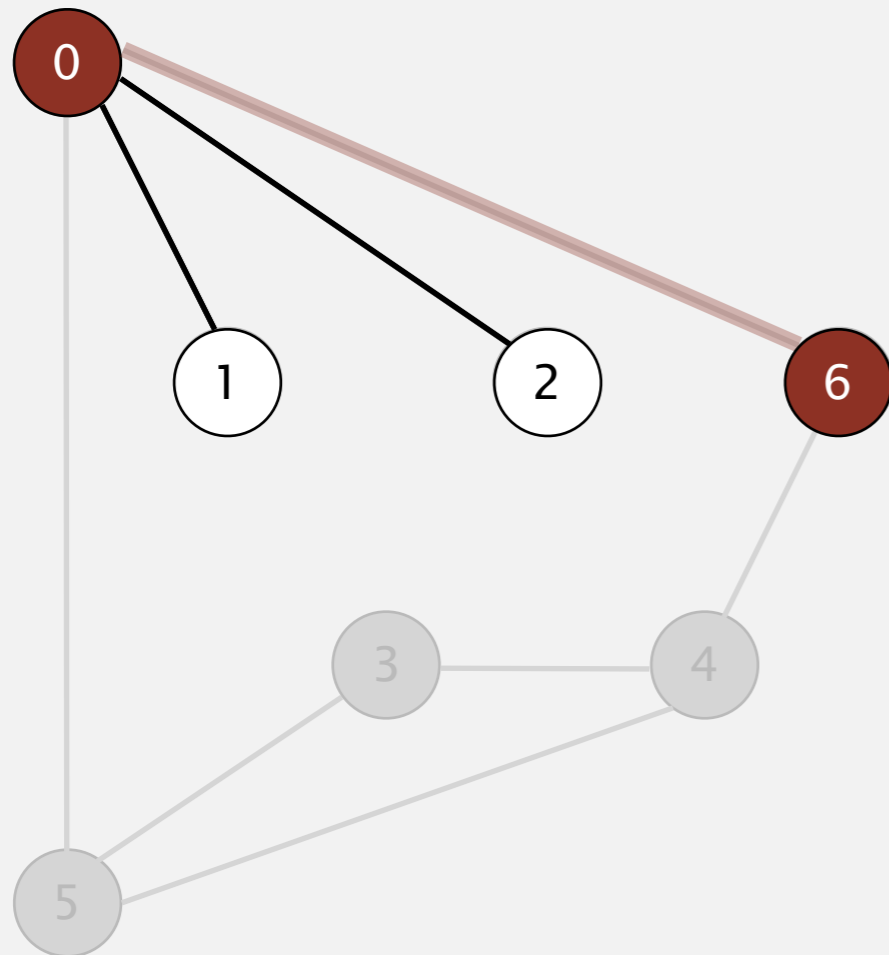
$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-



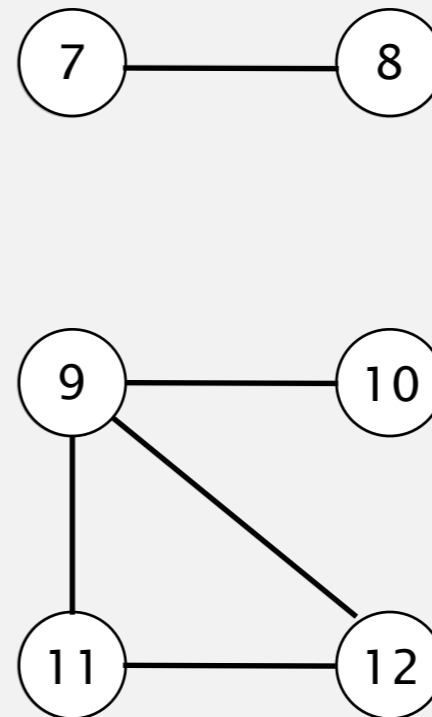
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



**6 done**

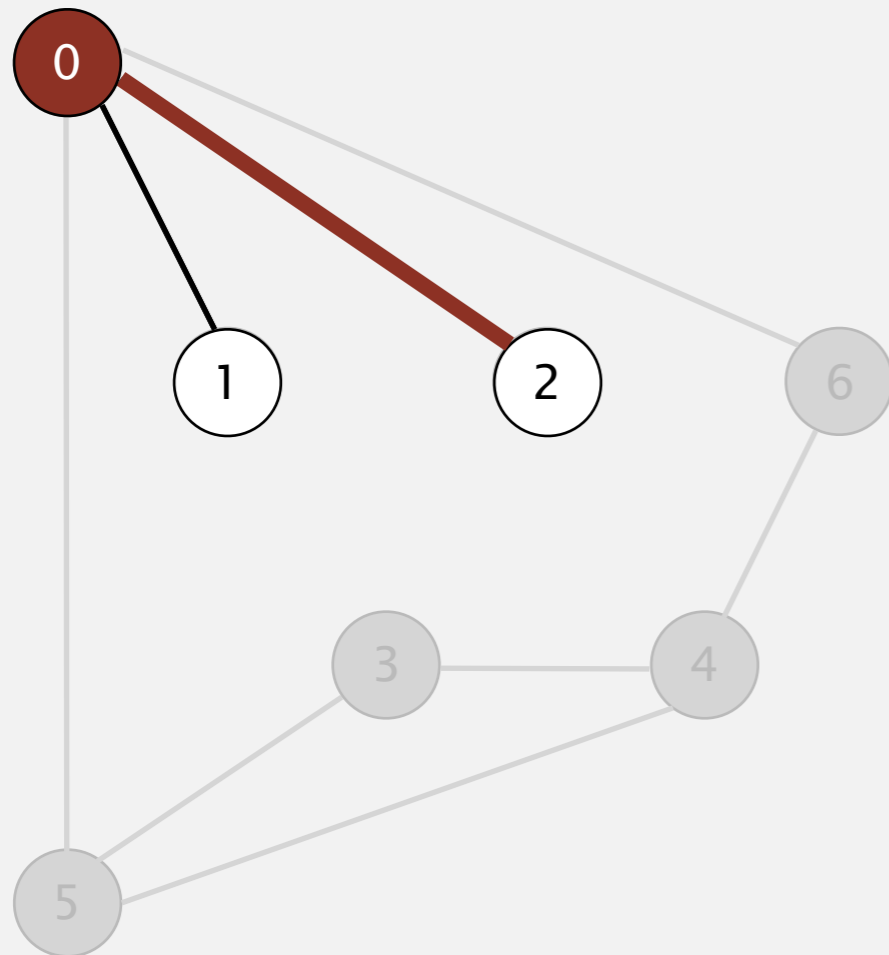


$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

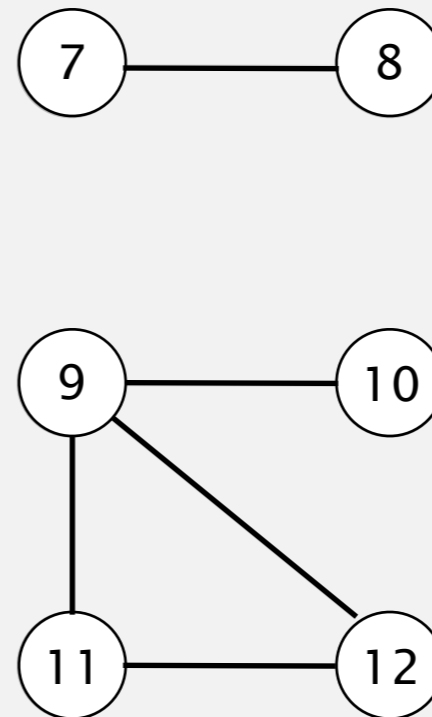
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



visit 0

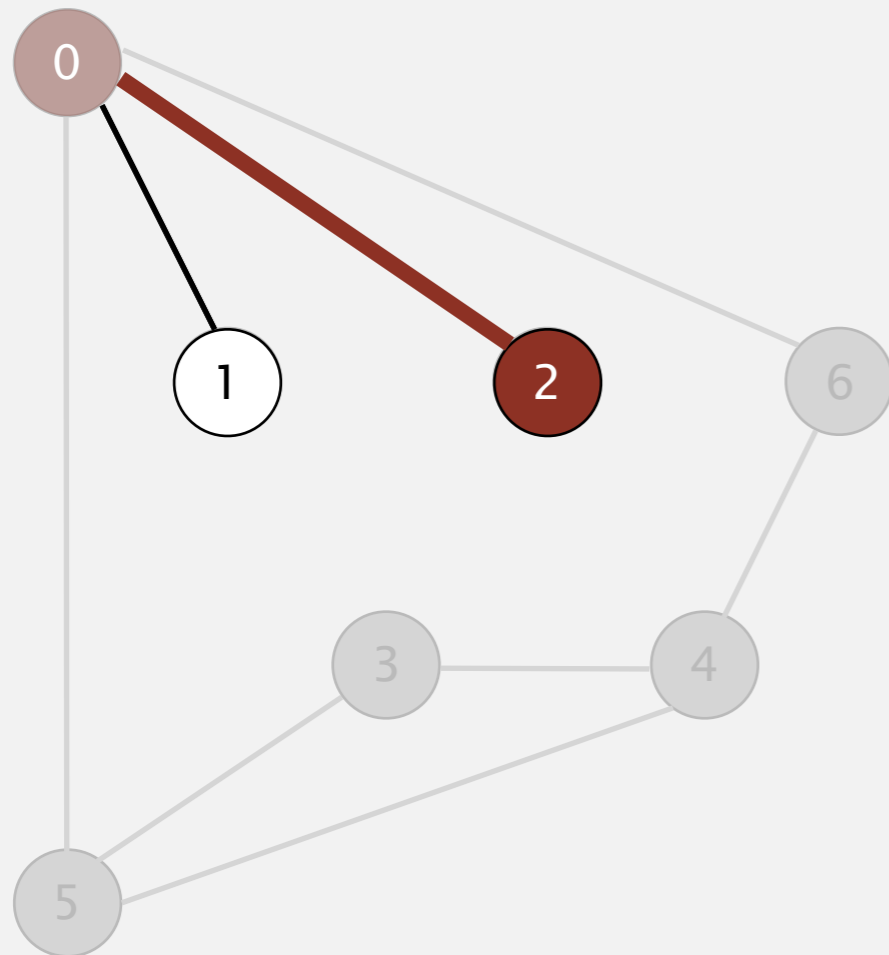


$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

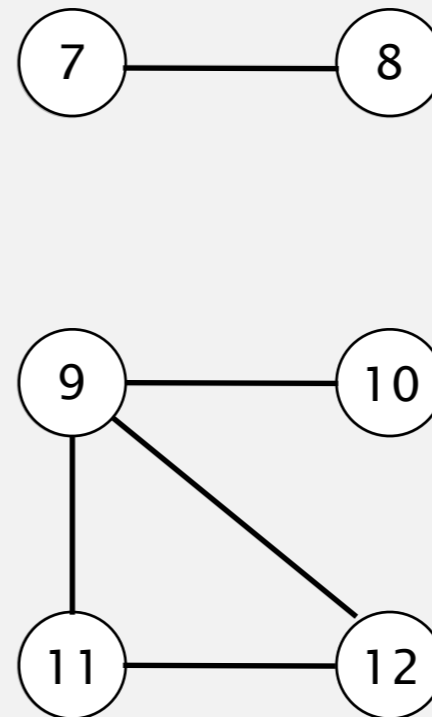
# Connected components demo

To visit a vertex  $v$  :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



visit 2

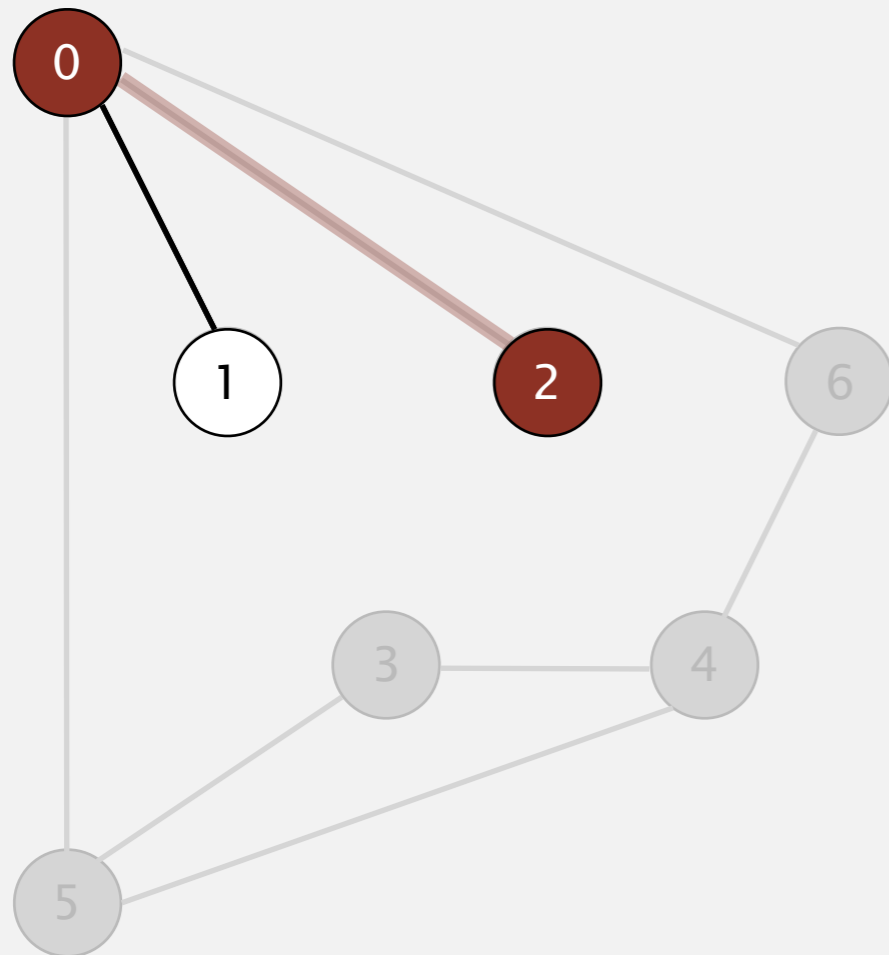


$v$	marked[]	id[]
0	T	0
1	F	-
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

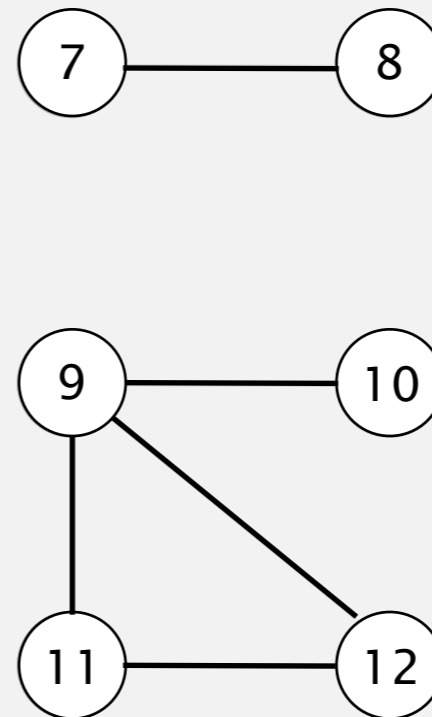
# Connected components demo

To visit a vertex  $v$  :

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- Recursively visit all unmarked vertices adjacent to  $v$ .



**2 done**

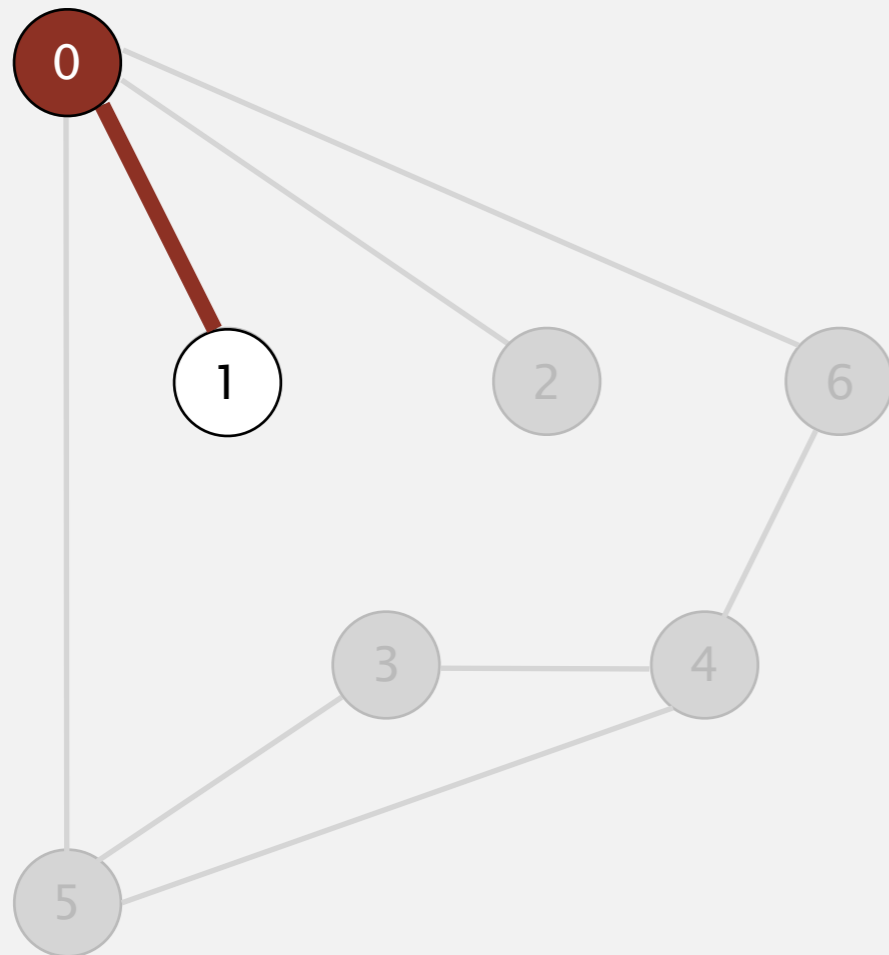


$v$	marked[]	id[]
0	T	0
1	F	-
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

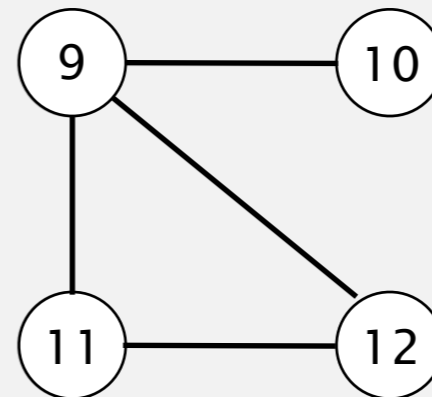
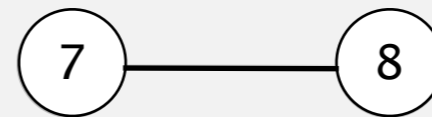
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visit 0

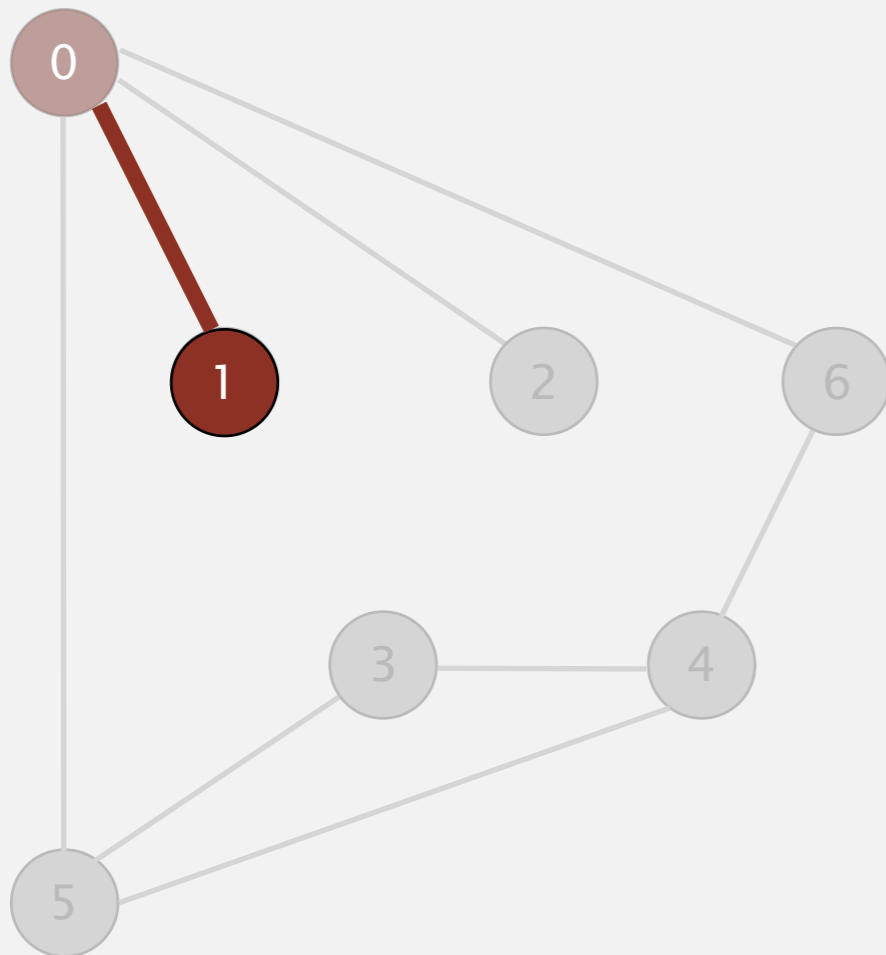


$v$	marked[]	id[]
0	T	0
1	F	-
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

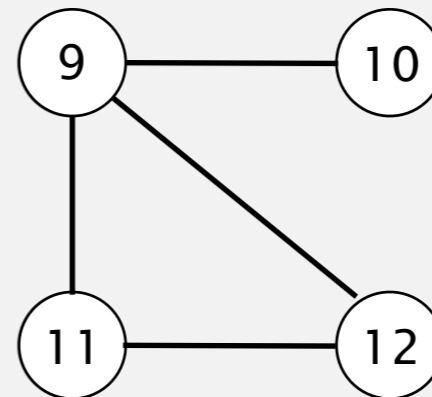
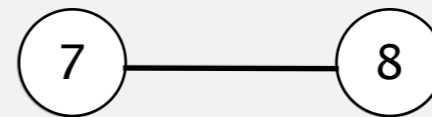
# Connected components demo

To visit a vertex  $v$  :

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**visit 1**

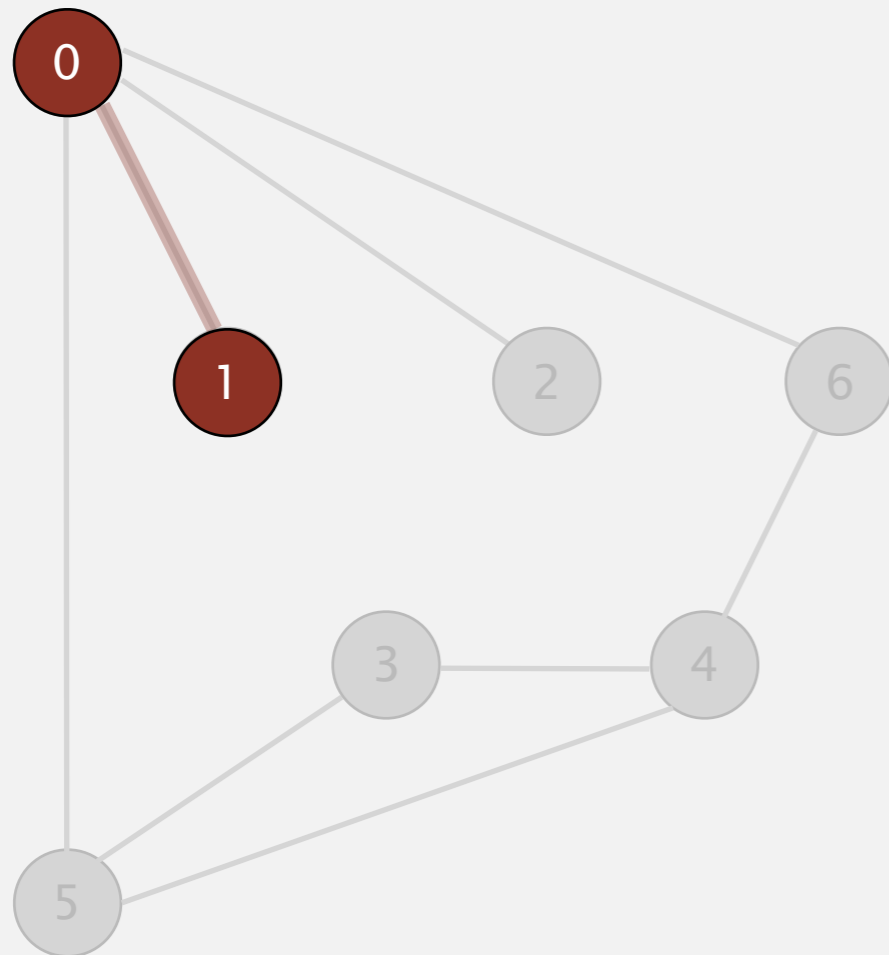


$v$	marked[]	id[]
0	T	0
1	<b>T</b>	<b>0</b>
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

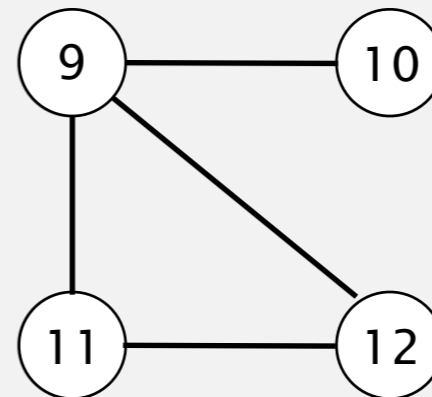
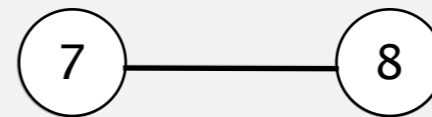
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



**1 done**



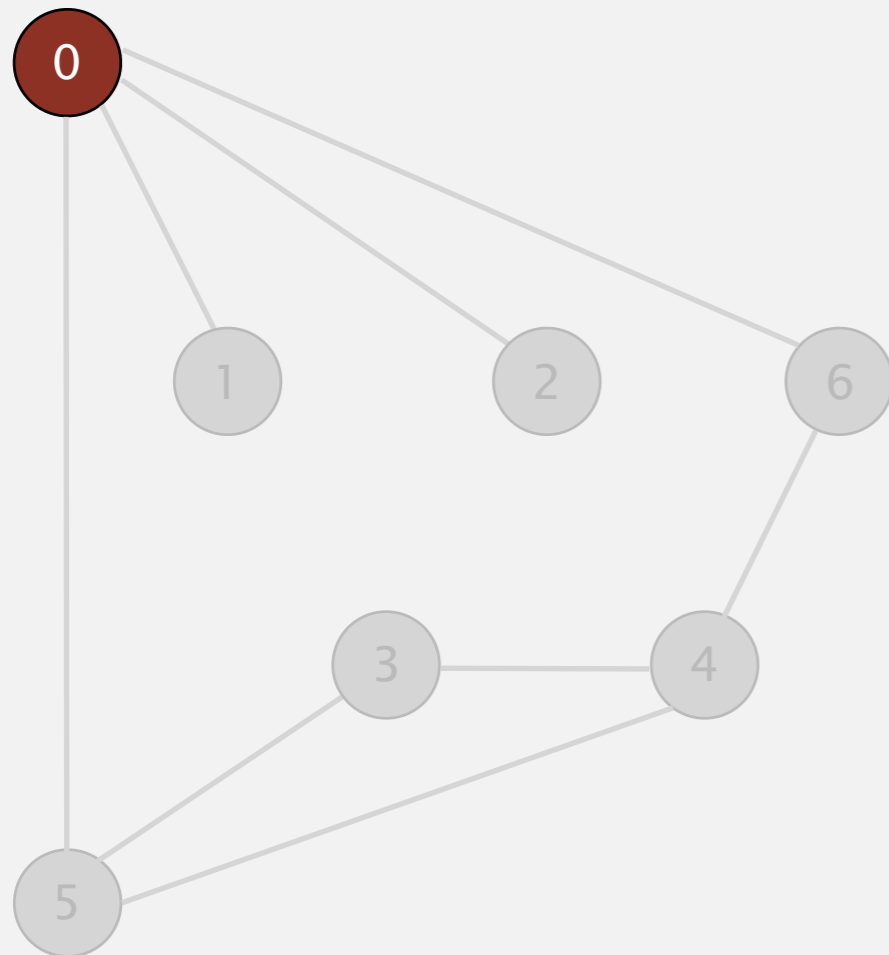
$v$	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

# Connected components demo

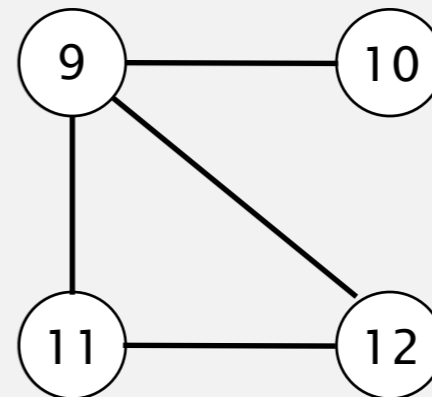
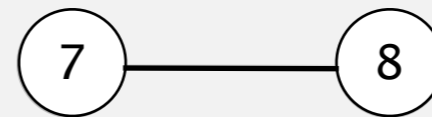
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To visit a vertex  $v$ :

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- Recursively visit all unmarked vertices adjacent to  $v$ .



**0 done**



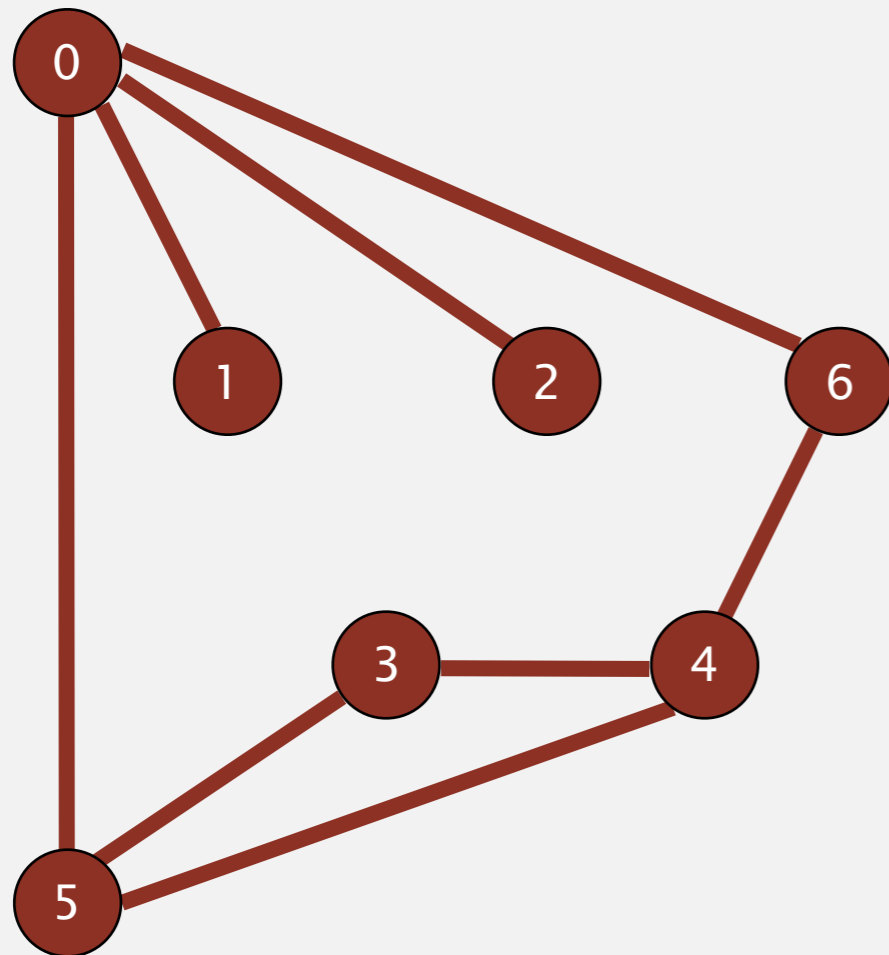
$v$	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-



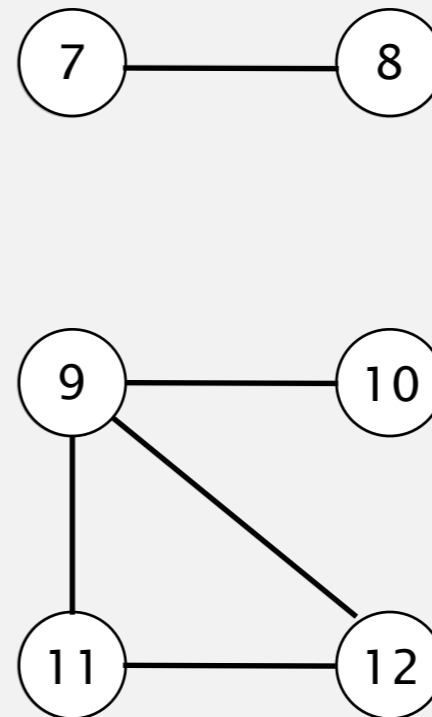
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



connected component: 0 1 2 3 4 5 6



$v$	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

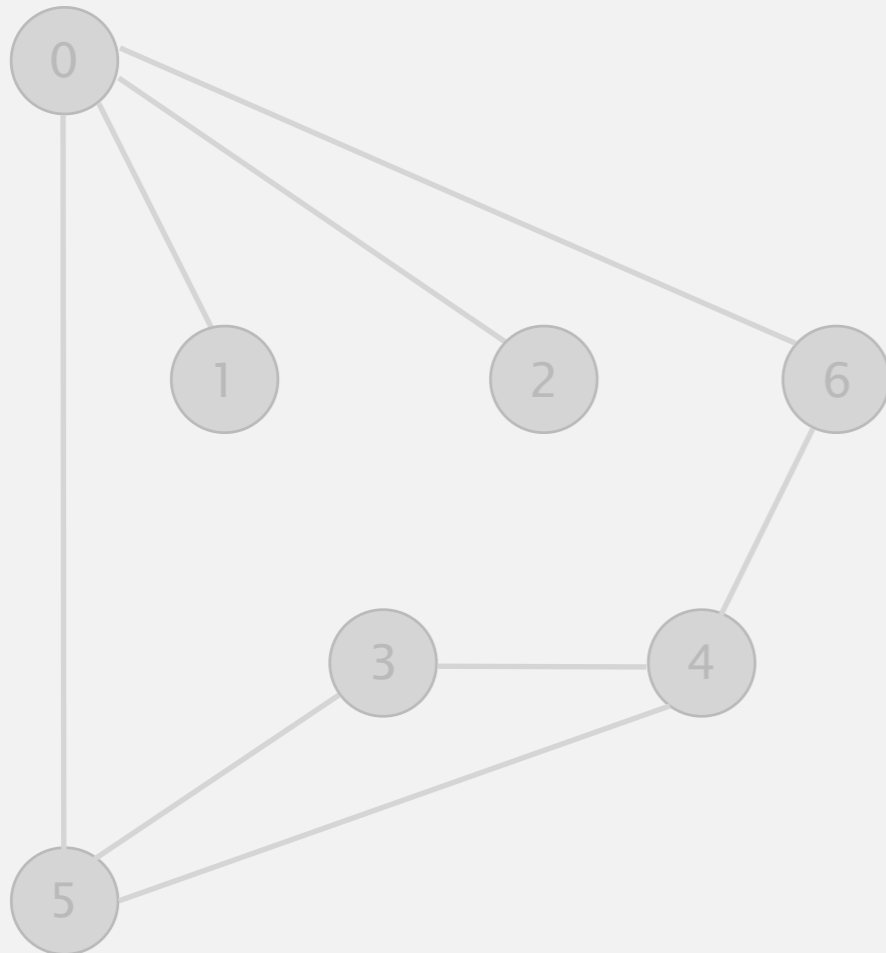
connected component →

# Connected components demo

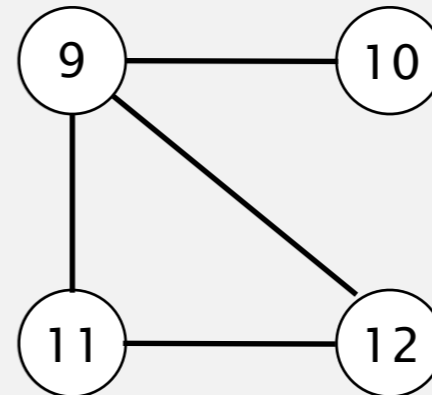
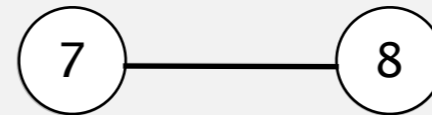
---

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



check 1 2 3 4 5 6

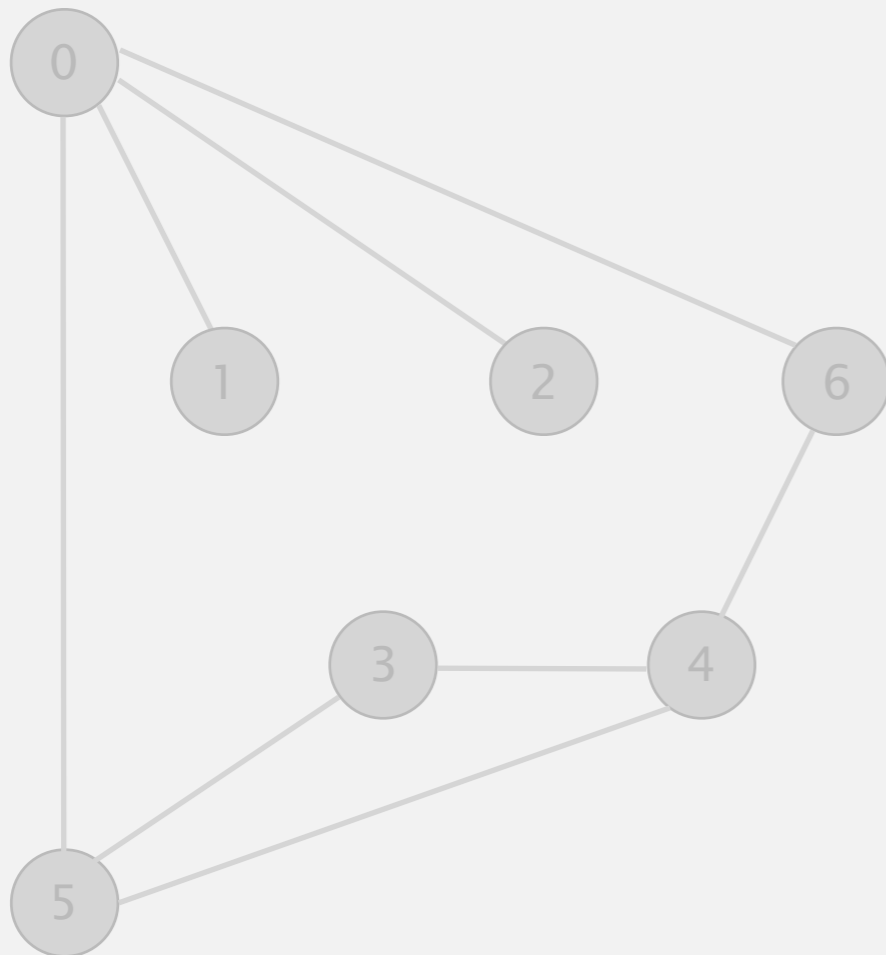


<u>v</u>	<u>marked[]</u>	<u>id[]</u>
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

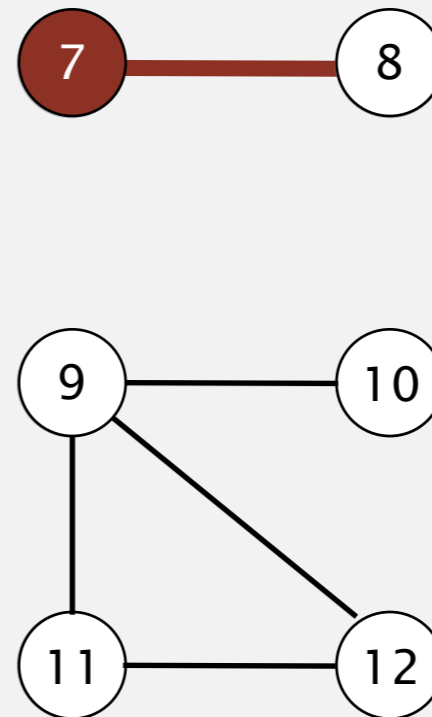
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



visit 7

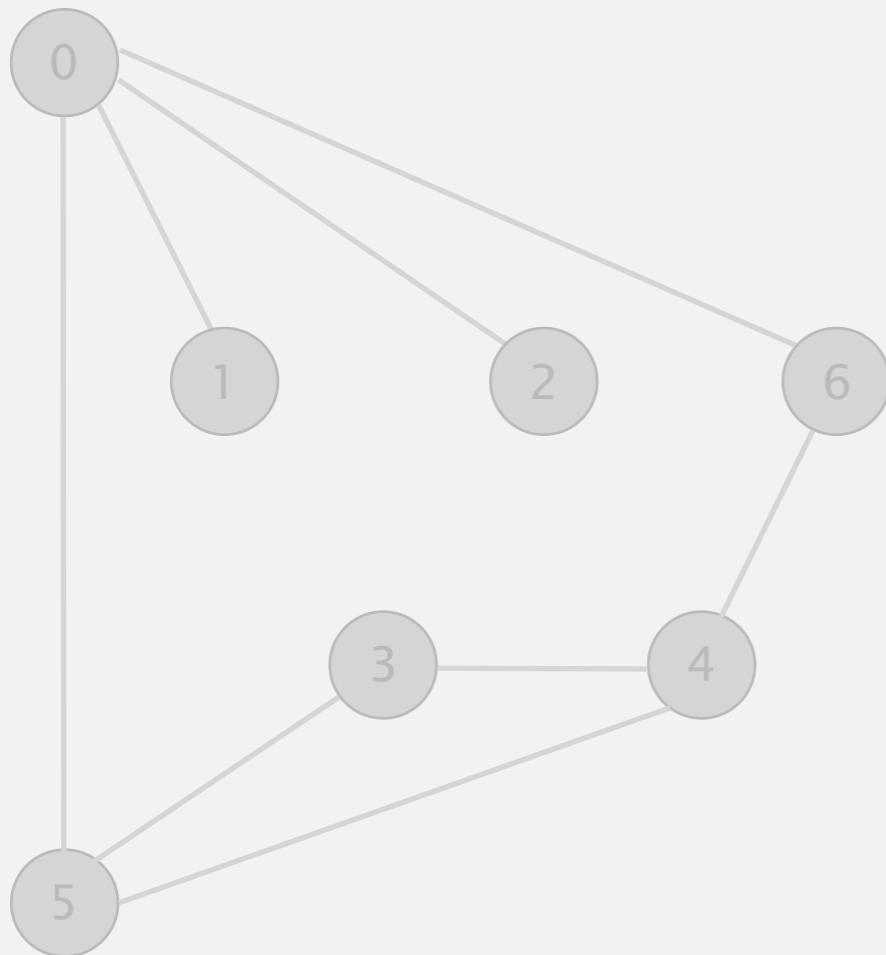


$v$	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

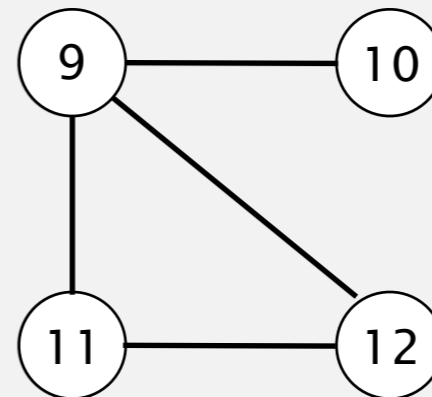
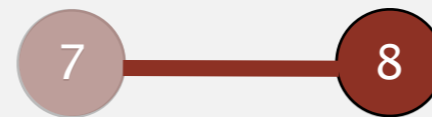
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



visit 8

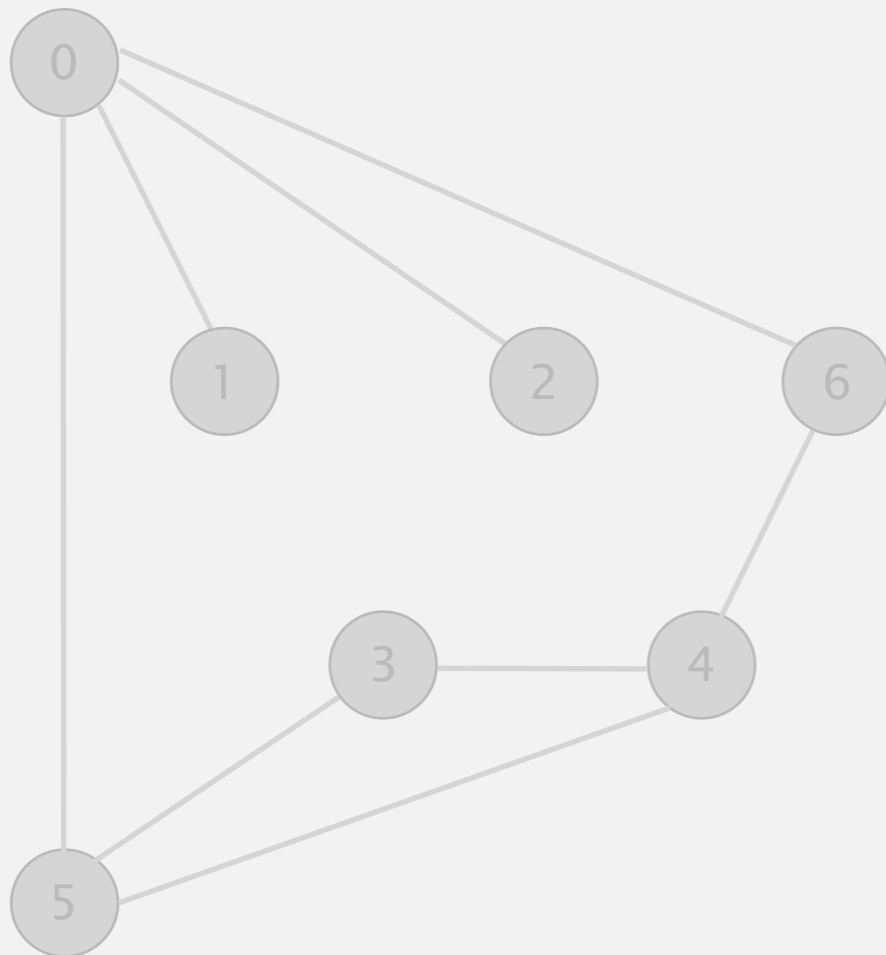


$v$	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	<b>T</b>	<b>1</b>
9	F	-
10	F	-
11	F	-
12	F	-

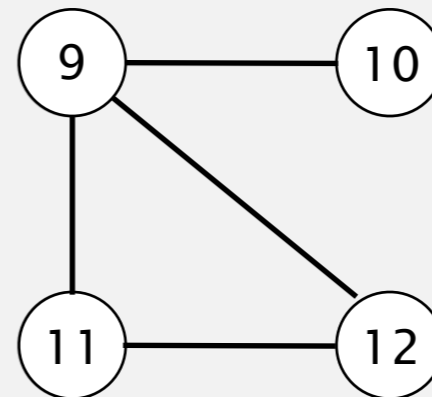
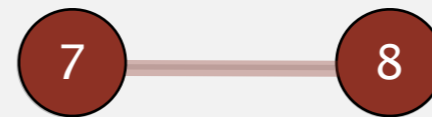
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



**8 done**

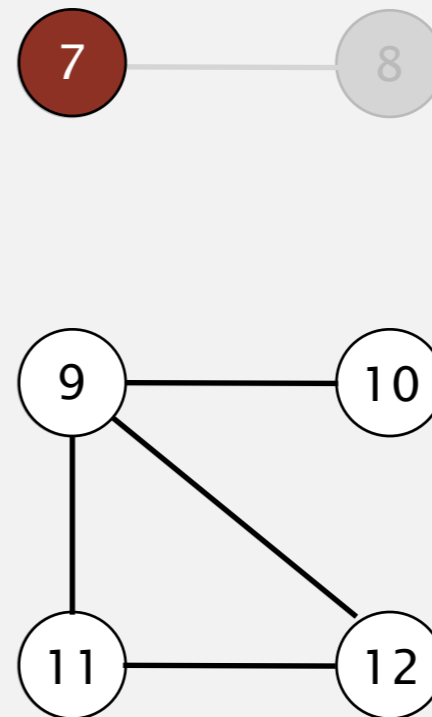
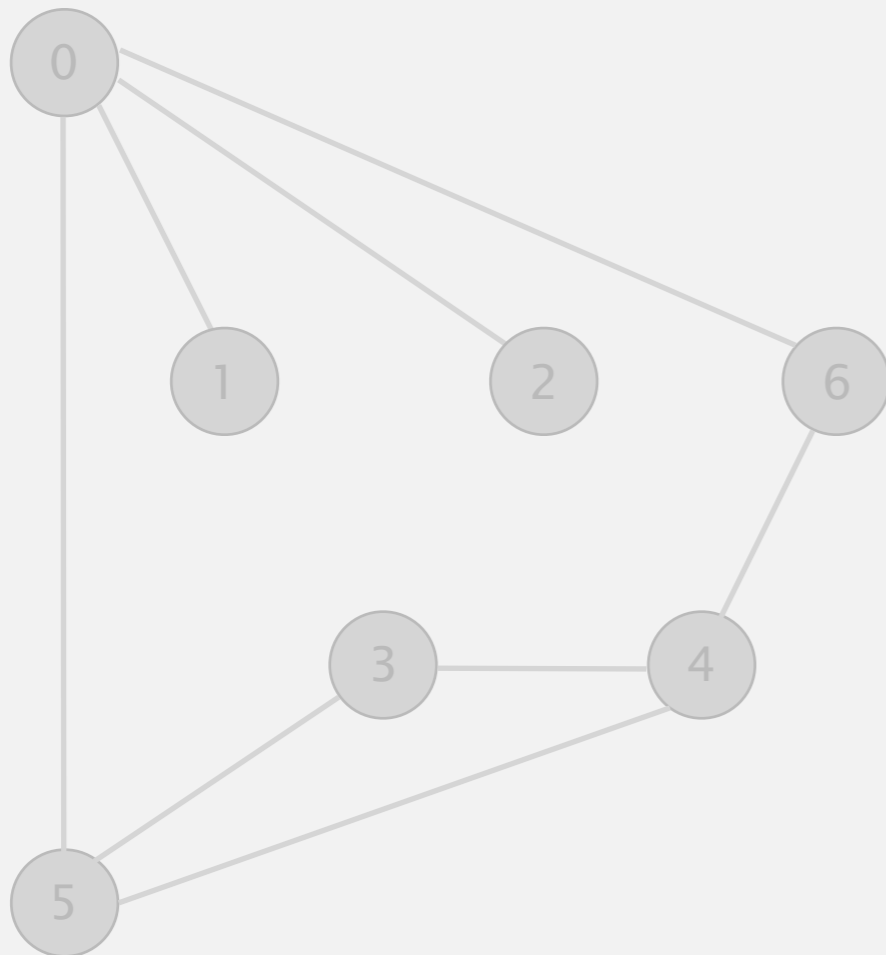


$v$	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	F	-
10	F	-
11	F	-
12	F	-

# Connected components demo

To visit a vertex  $v$  :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



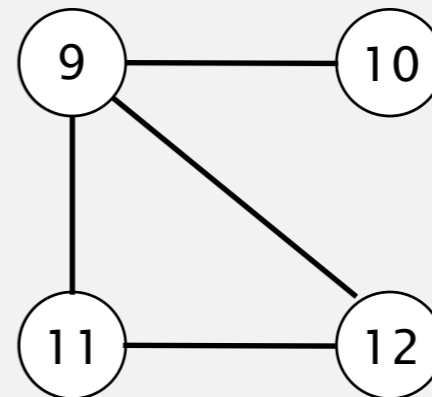
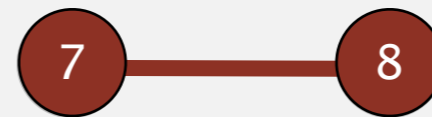
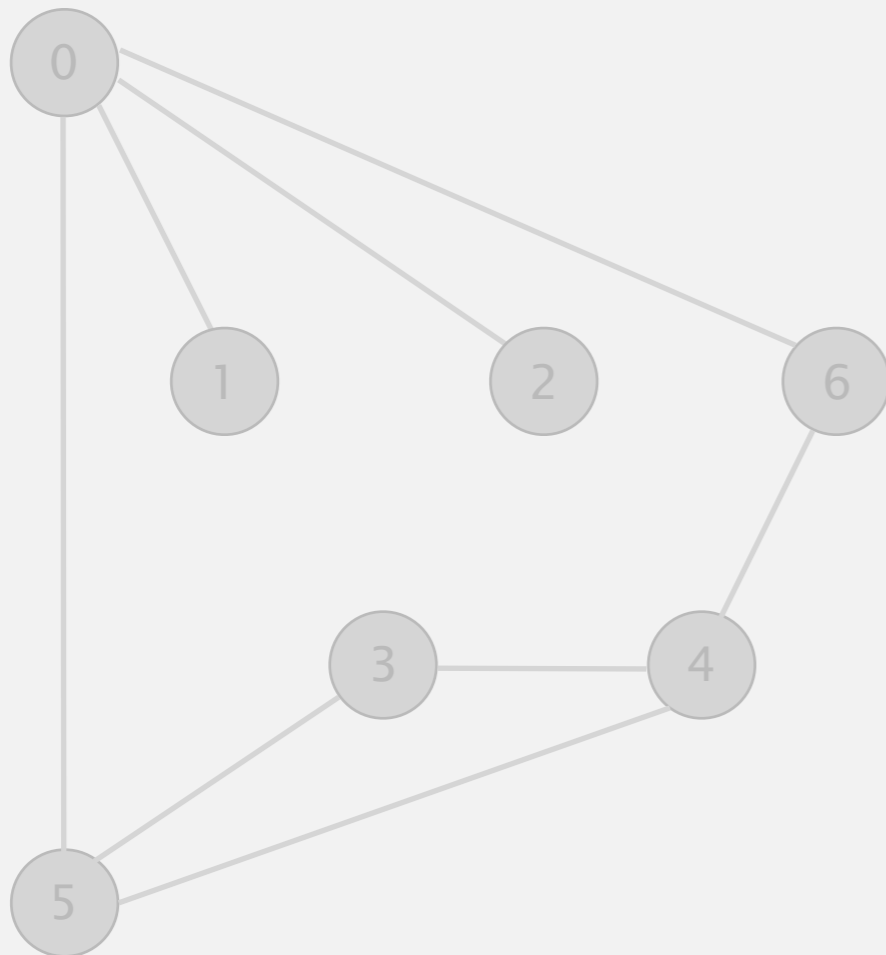
<u>v</u>	<u>marked[]</u>	<u>id[]</u>
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	<b>T</b>	<b>1</b>
8	<b>T</b>	<b>1</b>
9	F	-
10	F	-
11	F	-
12	F	-

**7 done**

# Connected components demo

To visit a vertex  $v$  :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



$v$	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	F	-
10	F	-
11	F	-
12	F	-

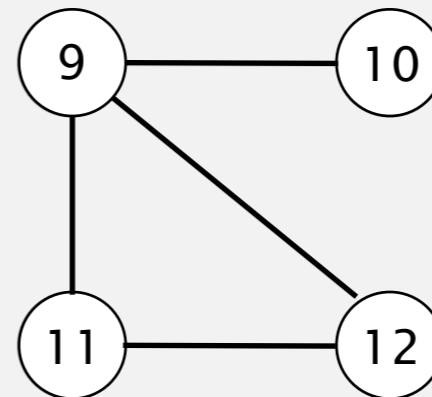
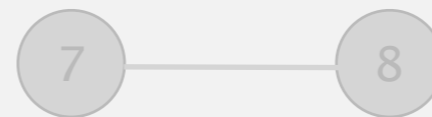
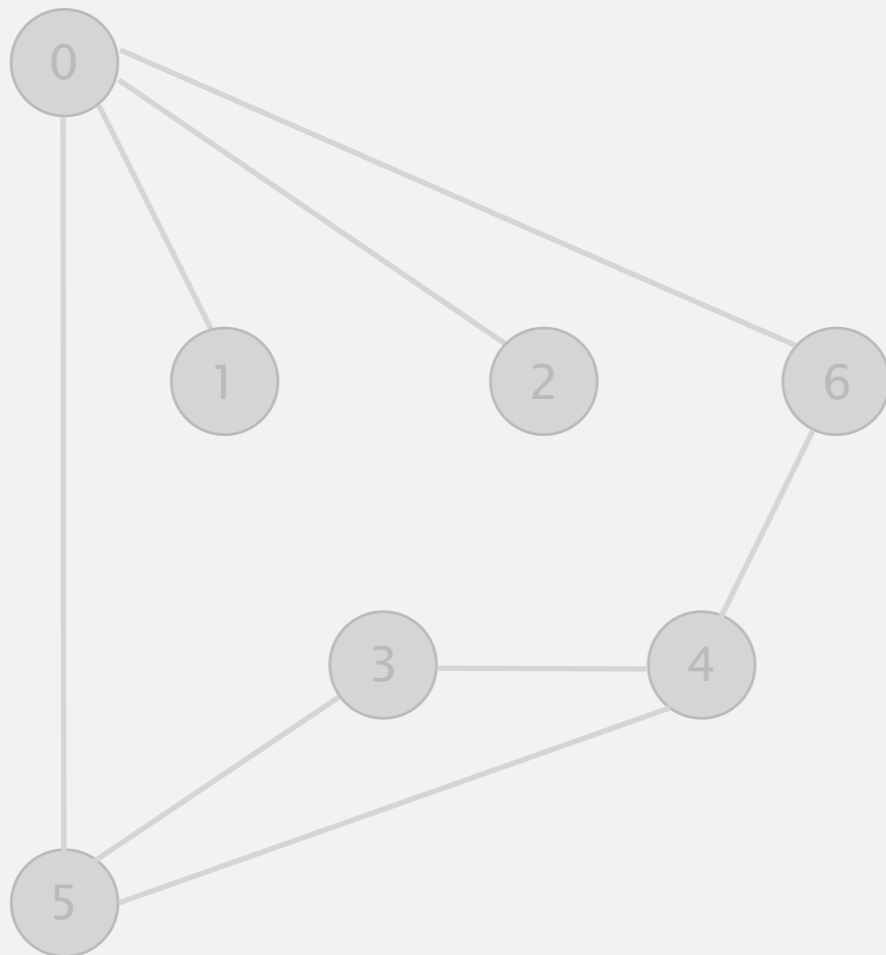
**connected component: 7 8**

# Connected components demo

---

To visit a vertex  $v$  :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



$v$	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	F	-
10	F	-
11	F	-
12	F	-

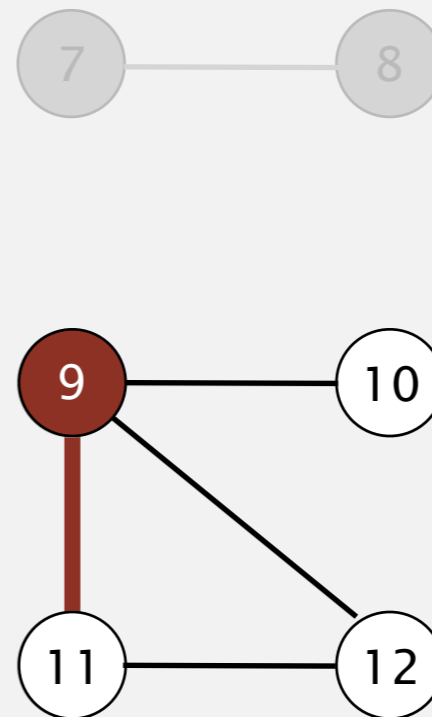
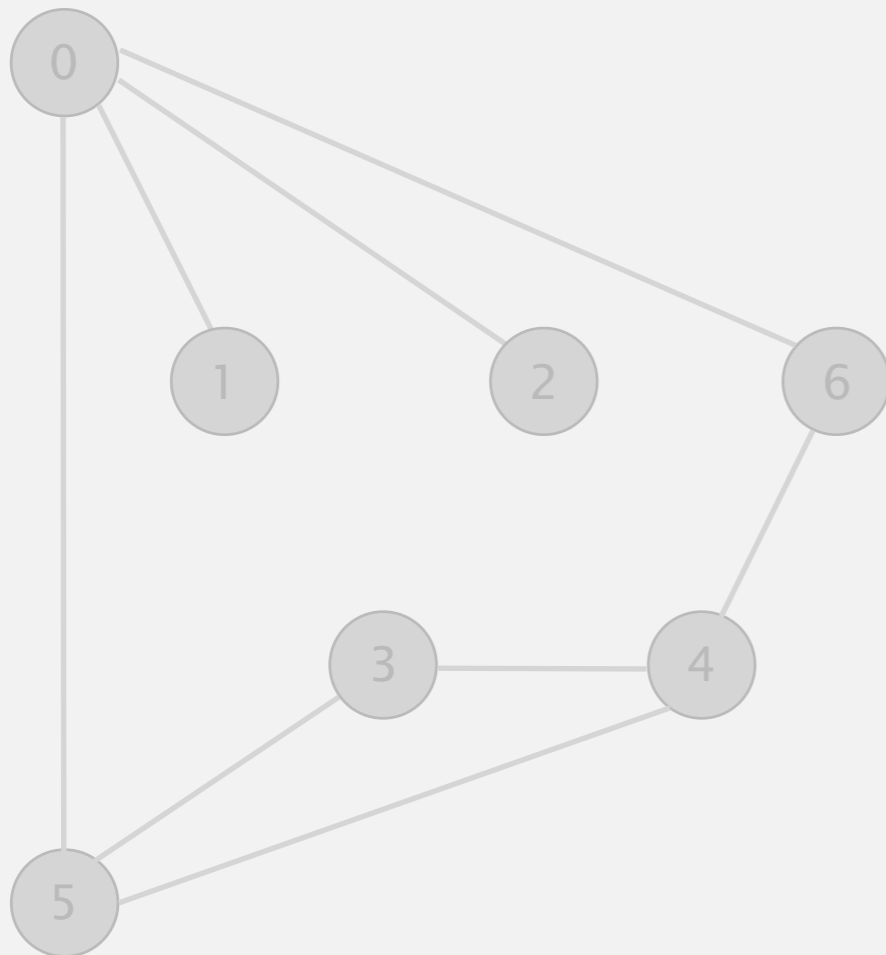
**check 8**



# Connected components demo

To visit a vertex  $v$  :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



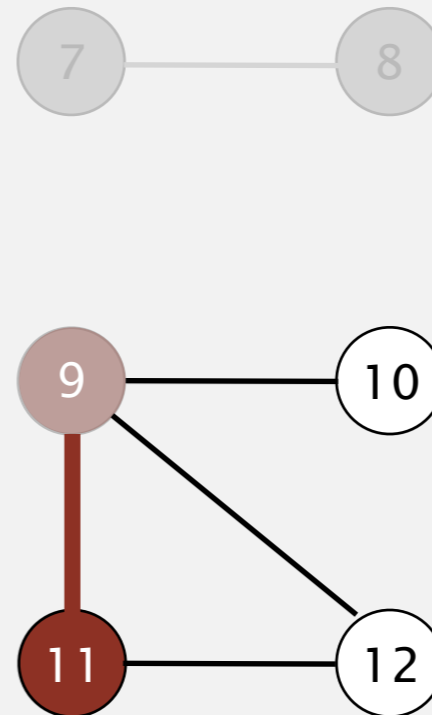
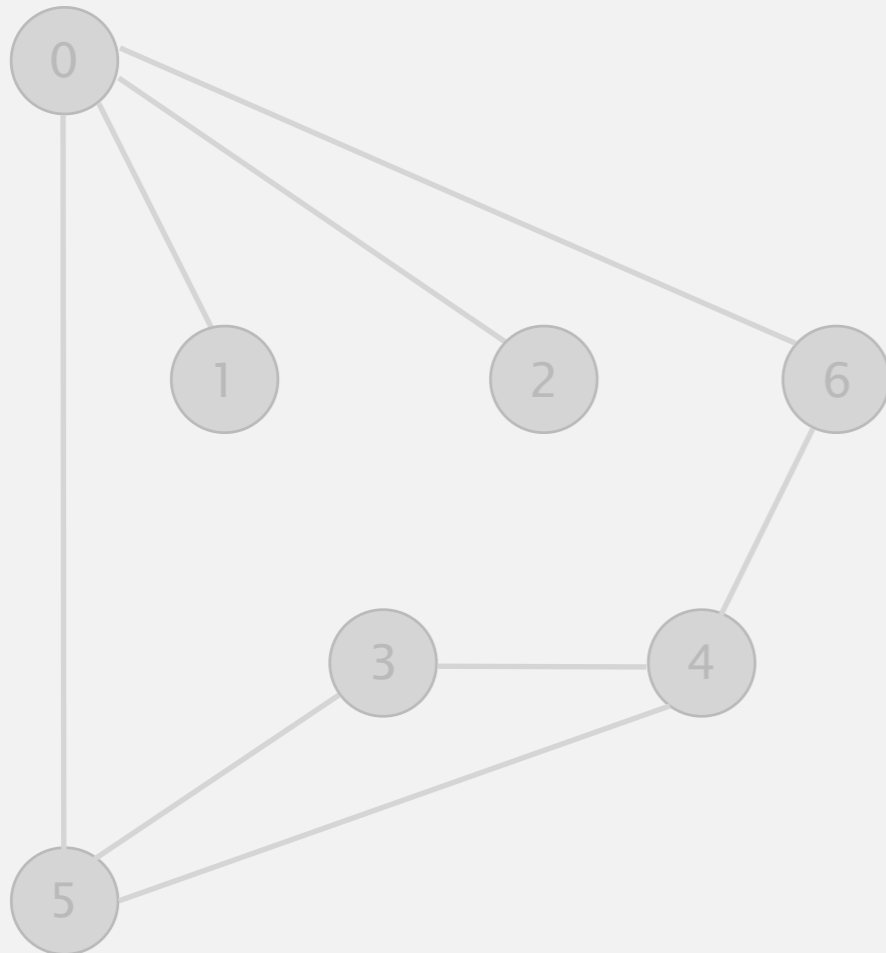
$v$	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	<b>T</b>	<b>2</b>
10	F	-
11	F	-
12	F	-

**visit 9**

# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



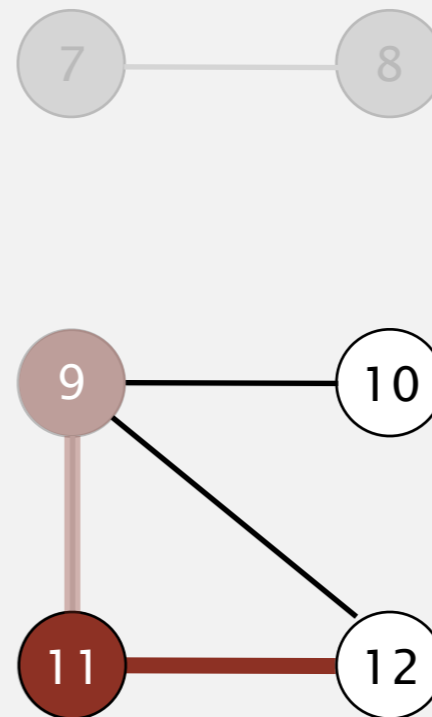
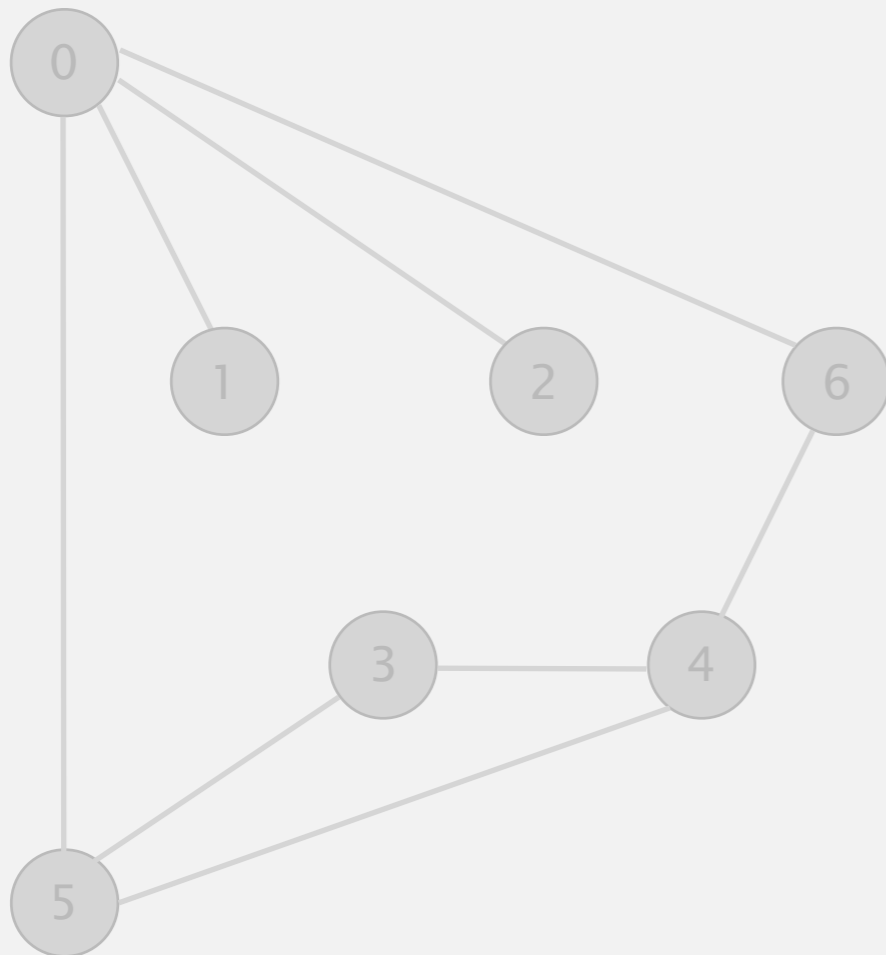
$v$	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	F	-
11	T	2
12	F	-

visit 11

# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



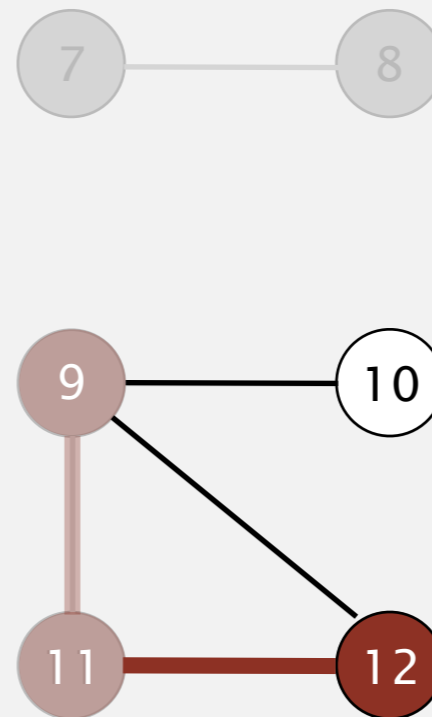
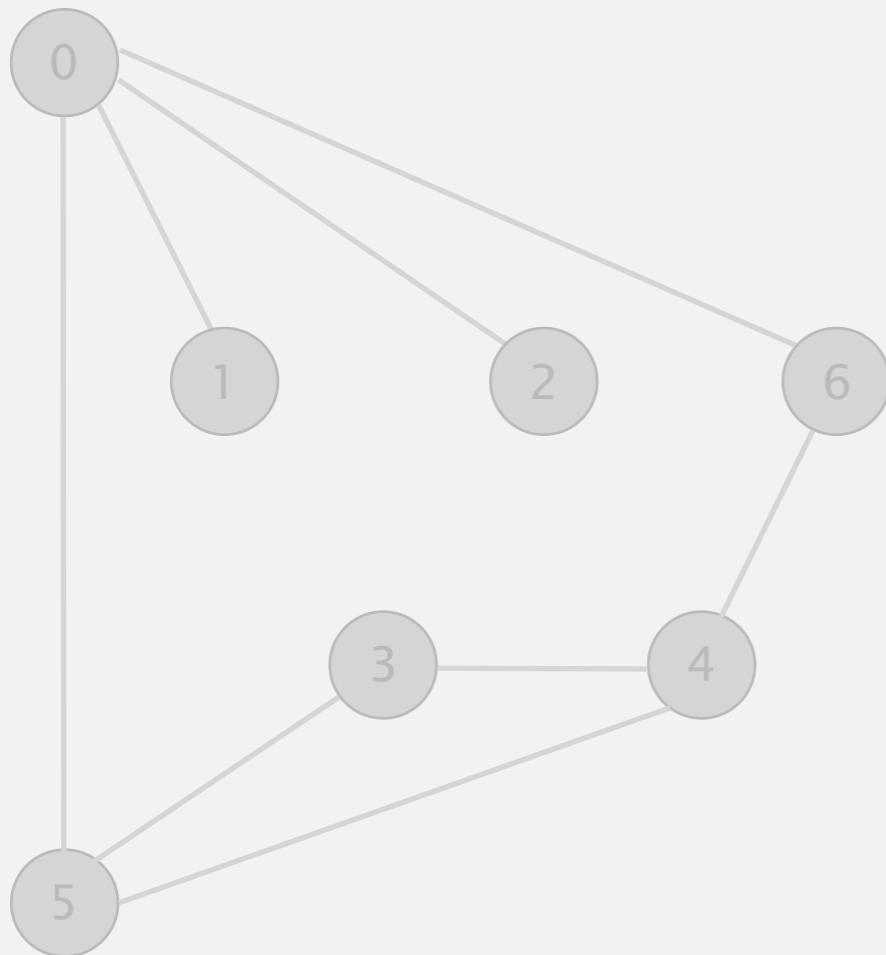
$v$	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	F	-
11	T	2
12	F	-

visit 11

# Connected components demo

To visit a vertex  $v$  :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



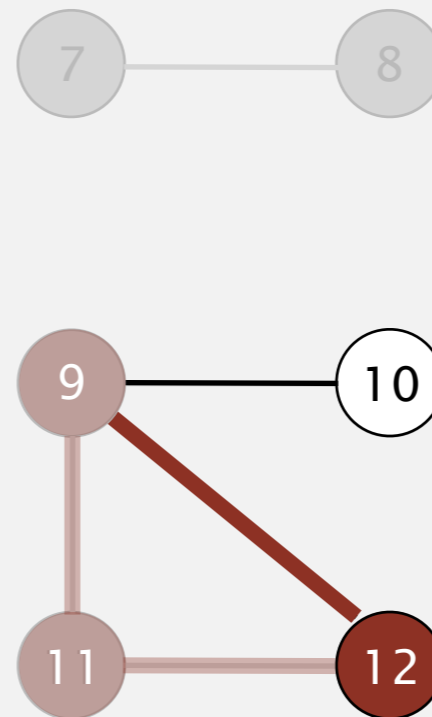
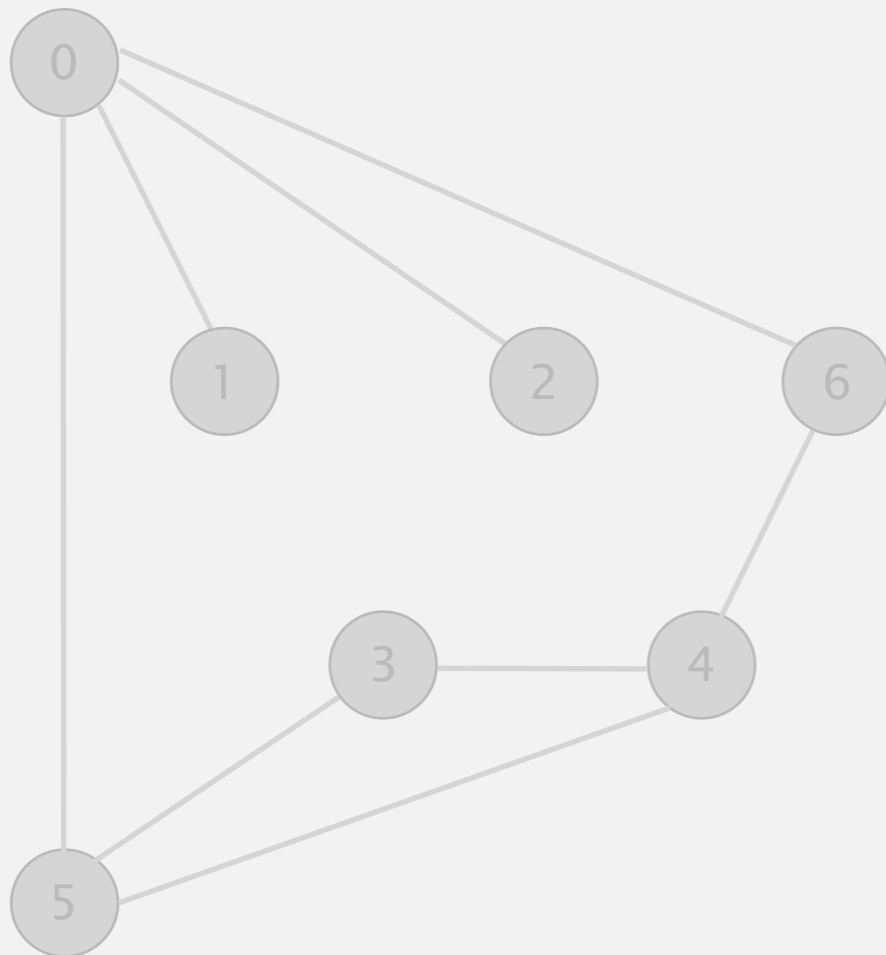
$v$	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	F	-
11	T	2
12	T	2

visit 12

# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



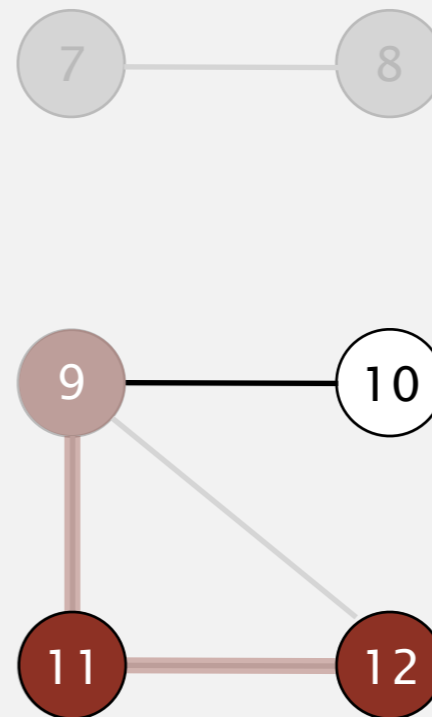
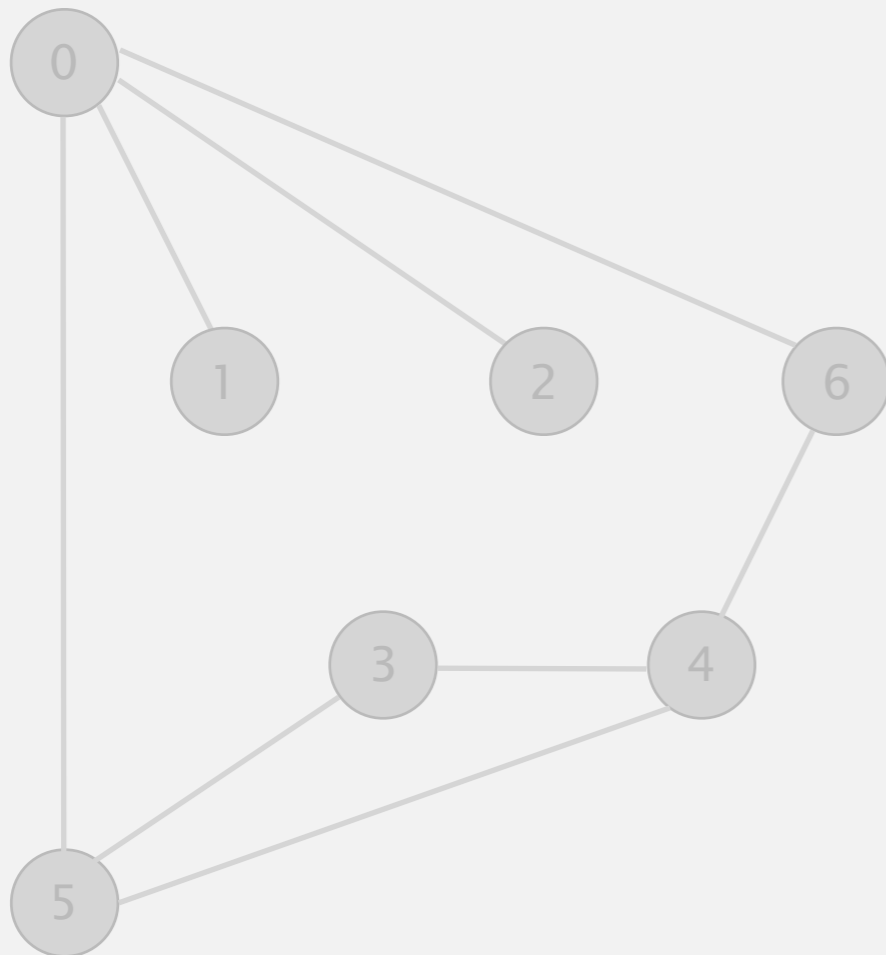
$v$	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	F	-
11	T	2
12	T	2

visit 12

# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



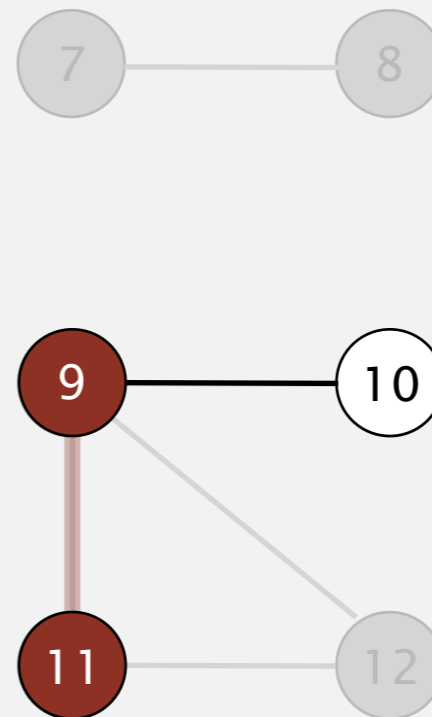
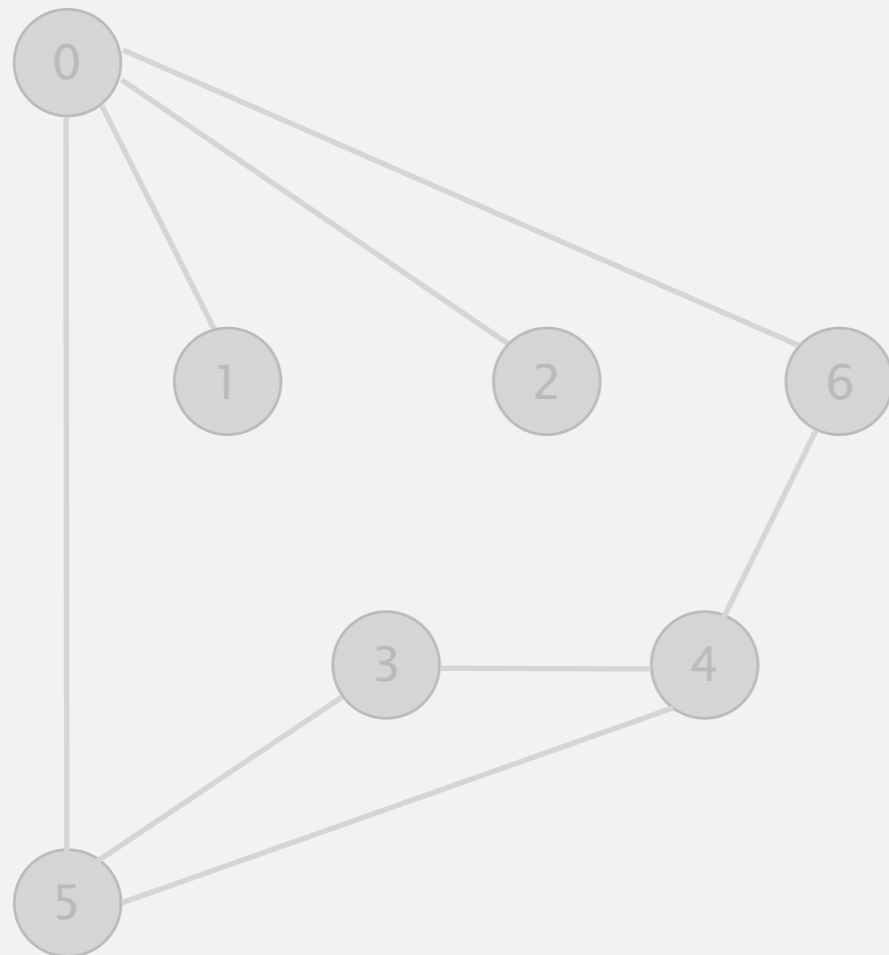
$v$	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	F	-
11	T	2
12	T	2

**12 done**

# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



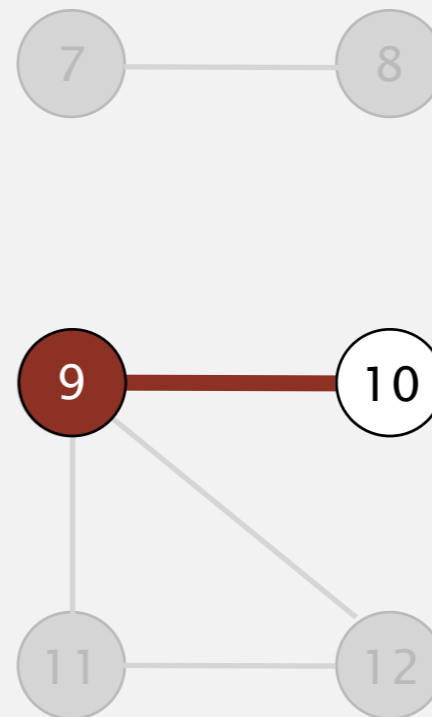
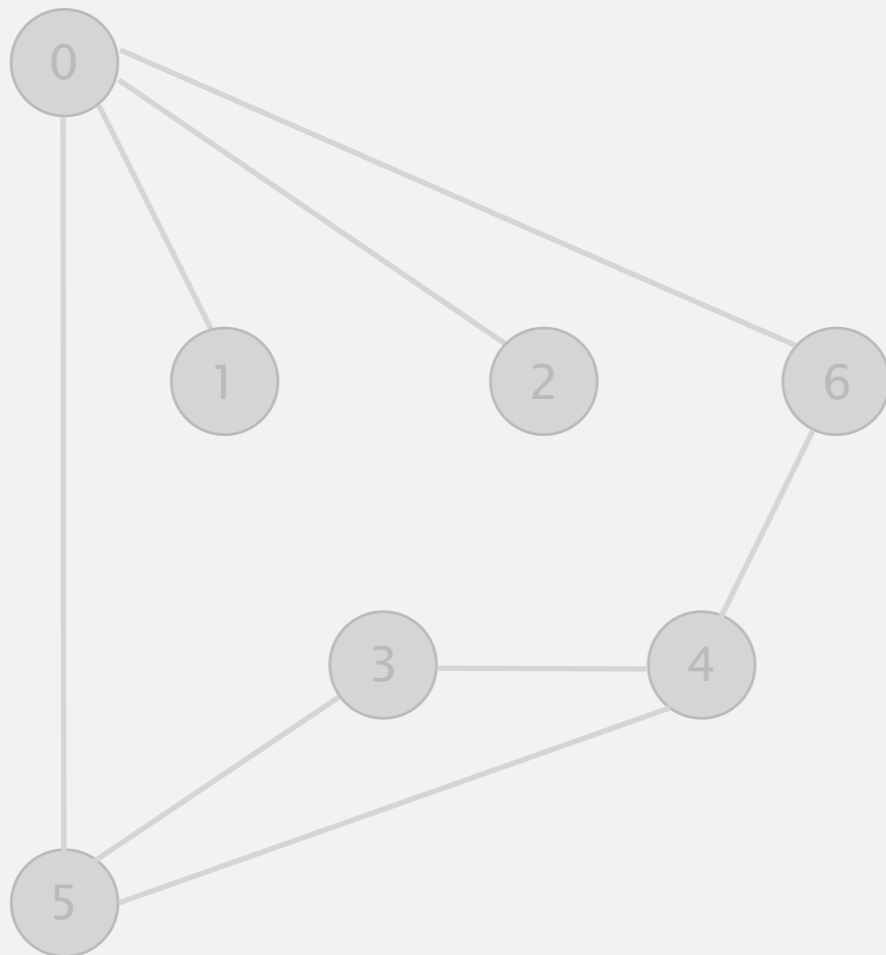
$v$	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	F	-
11	T	2
12	T	2

**11 done**

# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



$v$	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	F	-
11	T	2
12	T	2

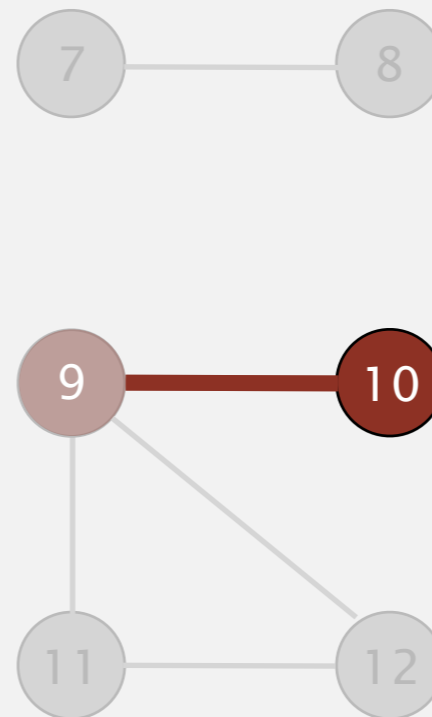
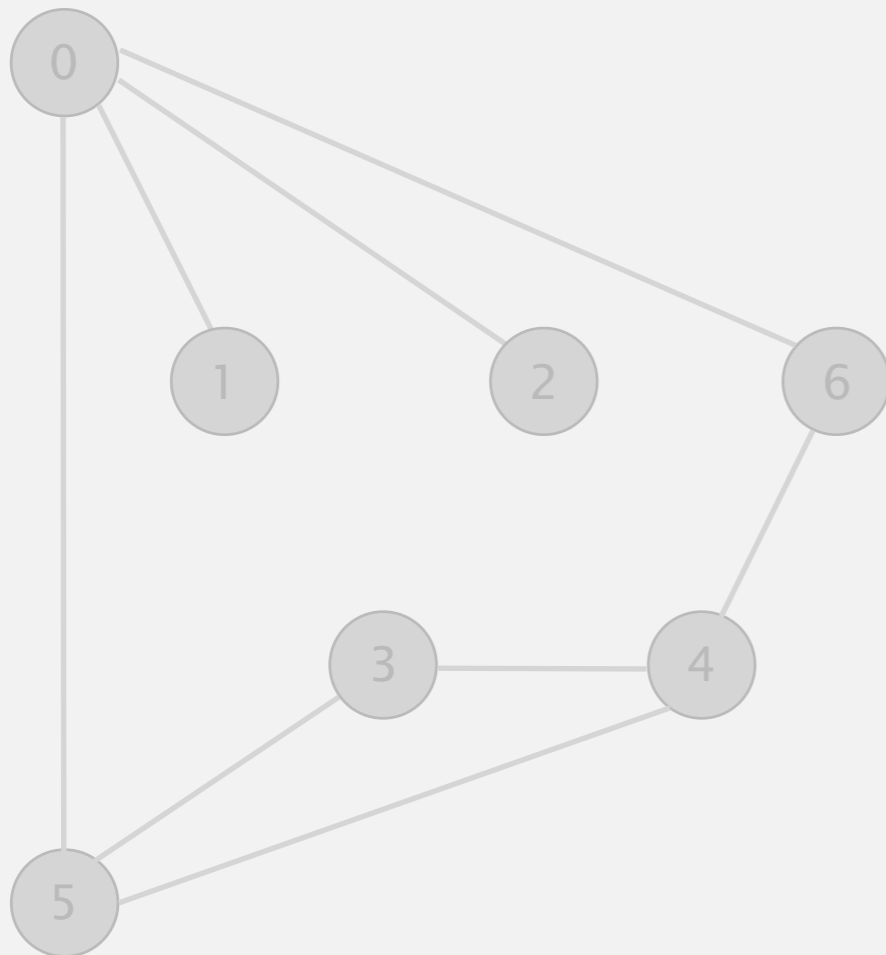
visit 9



# Connected components demo

To visit a vertex  $v$  :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



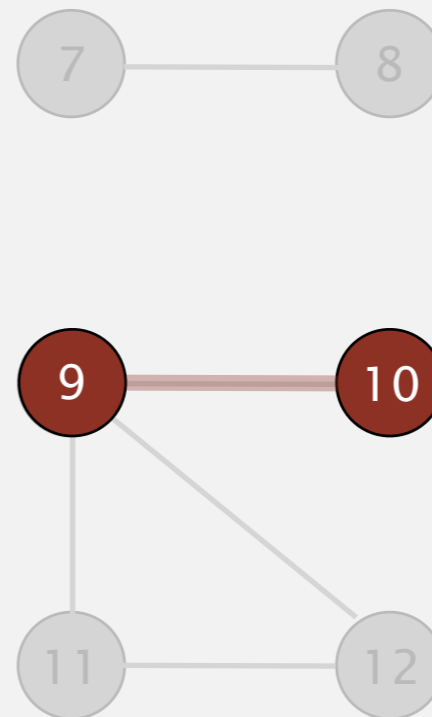
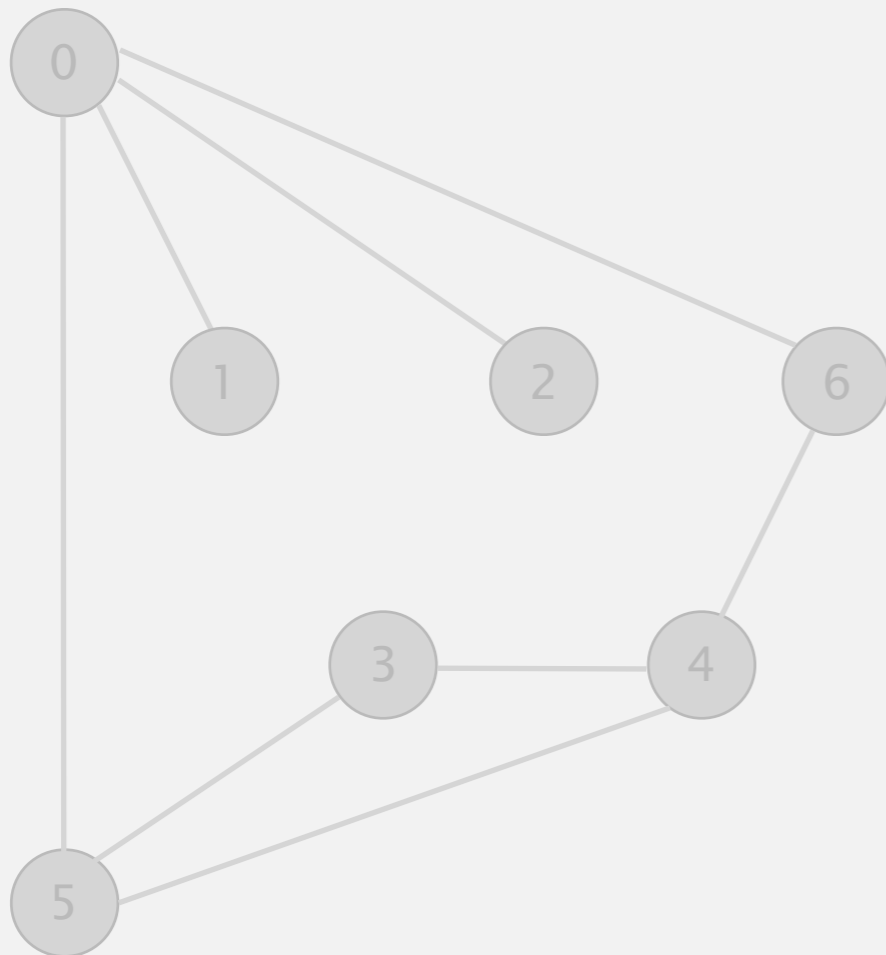
$v$	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	<b>T</b>	<b>2</b>
11	T	2
12	T	2

**visit 10**

# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



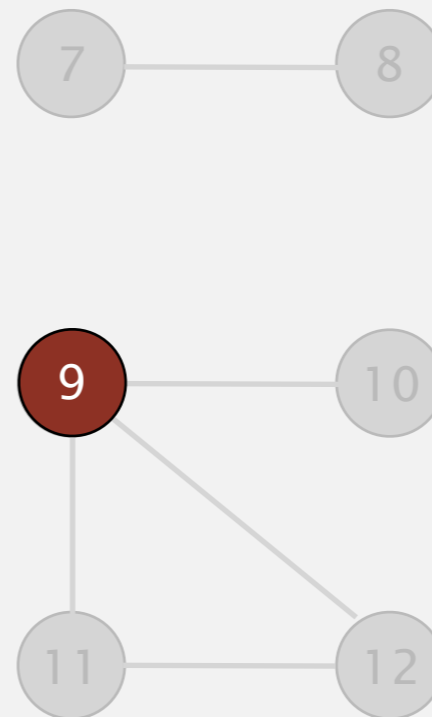
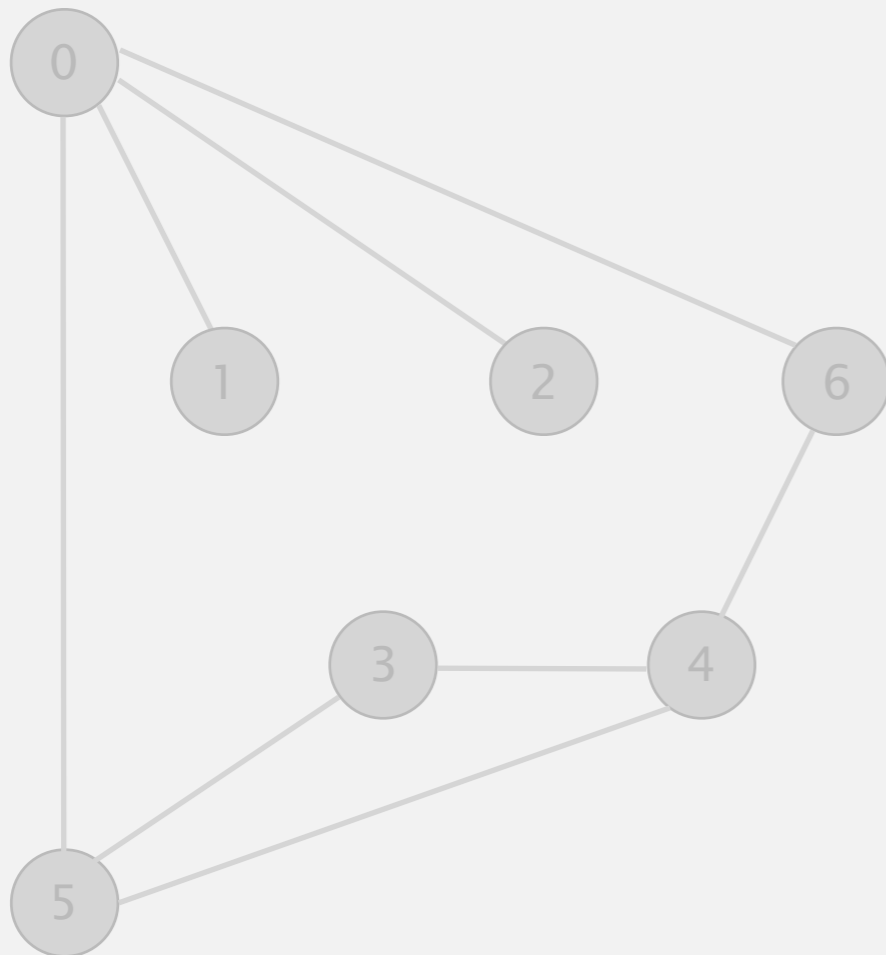
$v$	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	T	2
11	T	2
12	T	2

**10 done**

# Connected components demo

To visit a vertex  $v$  :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



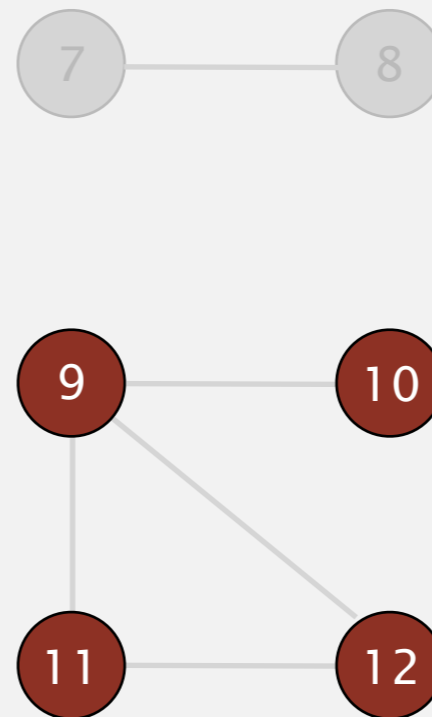
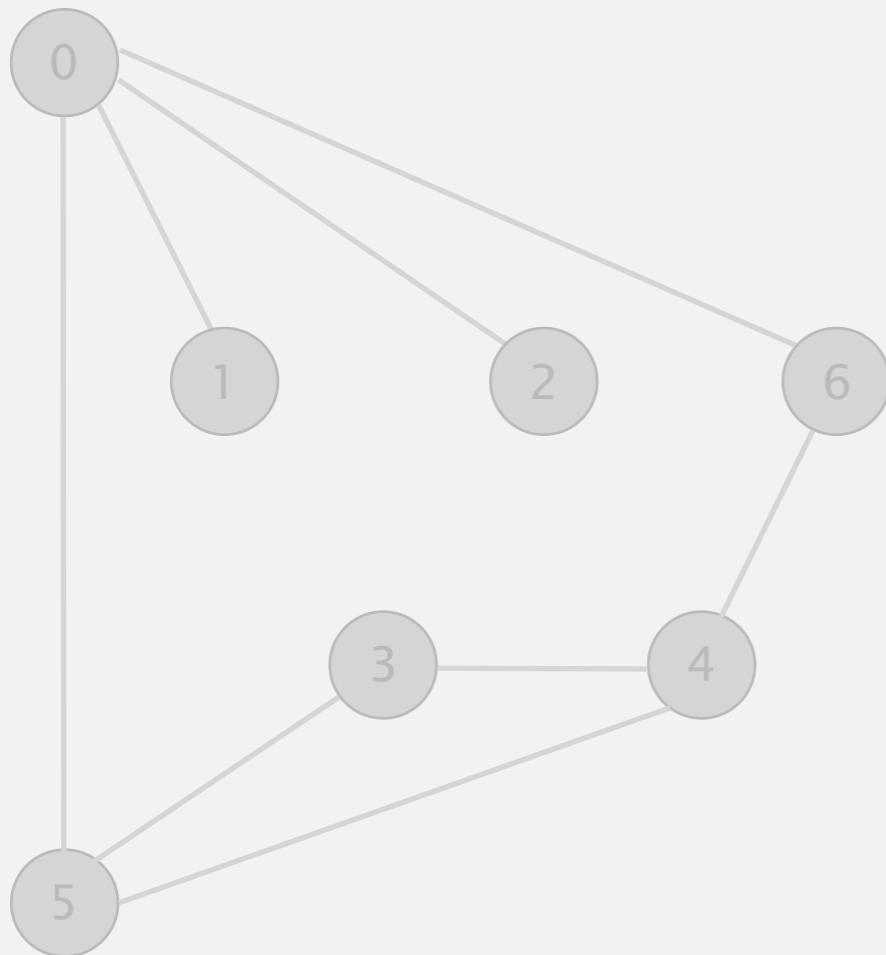
$v$	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	T	2
11	T	2
12	T	2

**9 done**

# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



<b>v</b>	<b>marked[]</b>	<b>id[]</b>
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	<b>T</b>	<b>2</b>
10	<b>T</b>	<b>2</b>
11	<b>T</b>	<b>2</b>
12	<b>T</b>	<b>2</b>

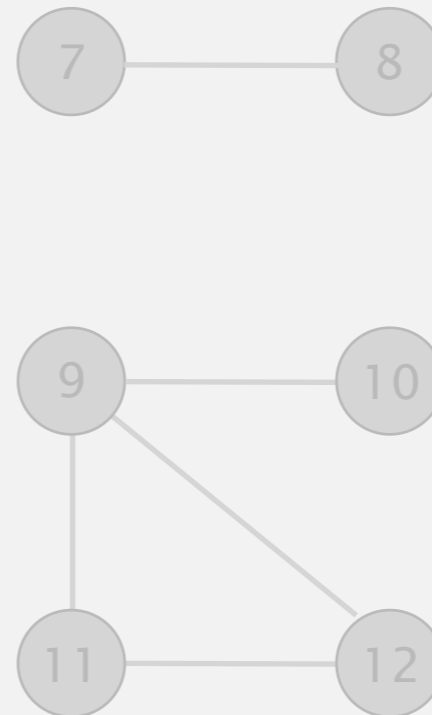
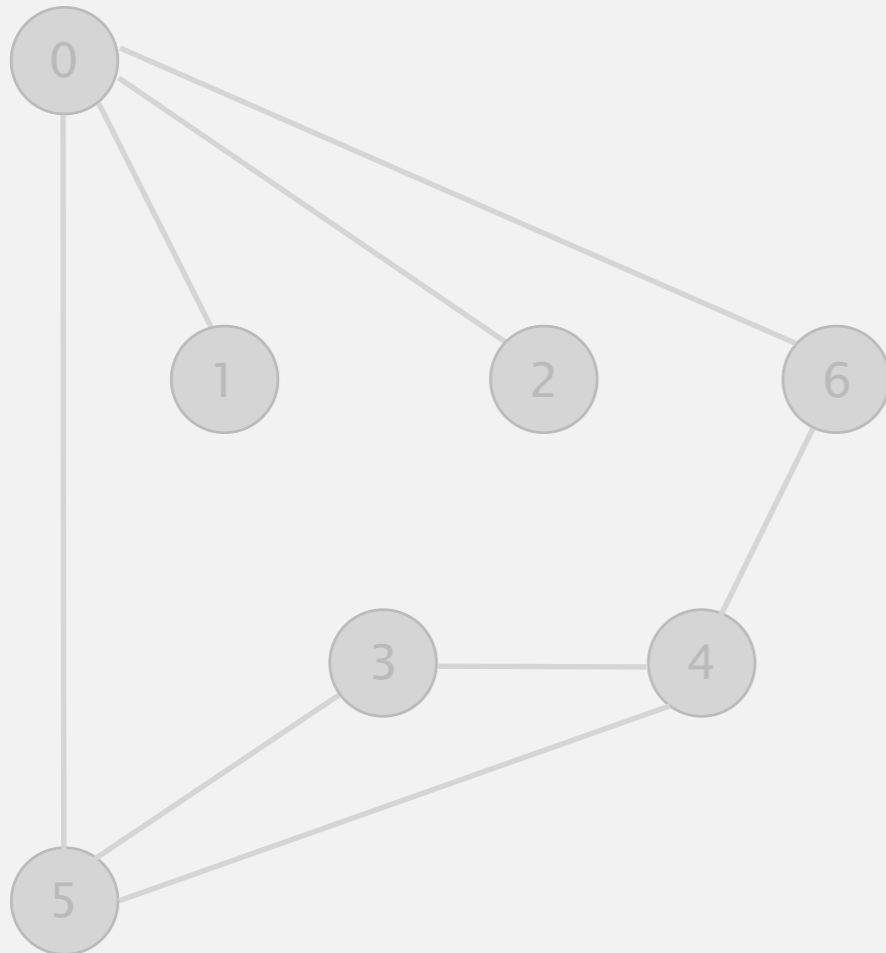
**connected component: 9 10 11 12**

# Connected components demo

---

To visit a vertex  $v$  :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



<u>v</u>	<u>marked[]</u>	<u>id[]</u>
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	T	2
11	T	2
12	T	2

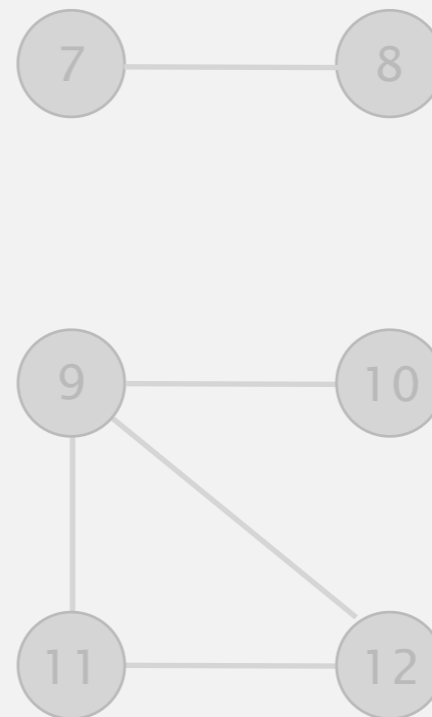
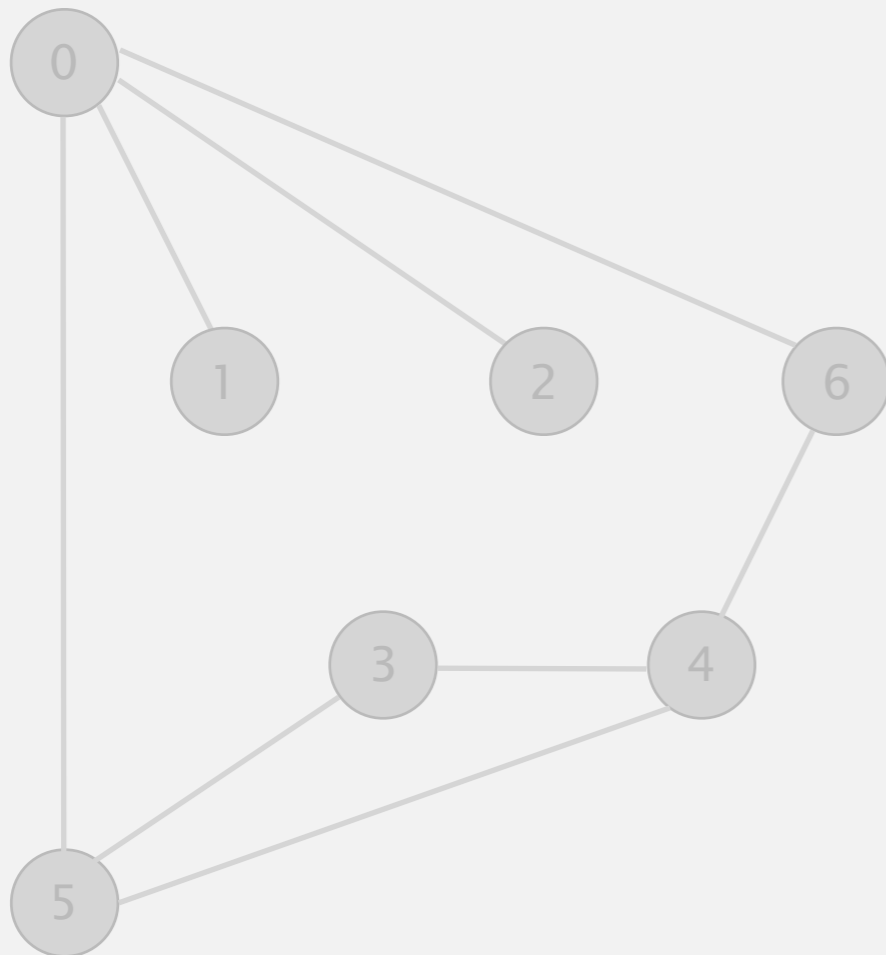
**check 10 11 12**

# Connected components demo

---

To visit a vertex  $v$  :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



<u>v</u>	<u>marked[]</u>	<u>id[]</u>
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	T	2
11	T	2
12	T	2

**done**