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PRIM'S ALGORITHM DEMO

- Prim's algorithm
- lazy implementation
- eager implementation

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Prim's algorithm

lazy implementation

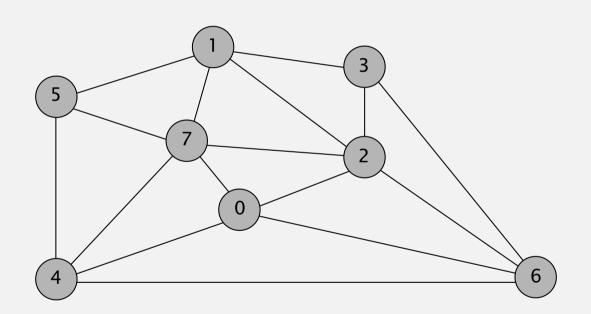
eager implementation



ROBERT SEDGEWICK | KEVIN WAYNE

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- Start with vertex 0 and greedily grow tree *T*.
- Add to *T* the min weight edge with exactly one endpoint in *T*.
- Repeat until V-1 edges.



an edge-weighted graph

0-7	0.10
2-3	0.17
1-7	0.19
0-2	0.20
5-7	0.28
1-3	0.29
1-5	0.32
2-7	0.34
4-5	0.3
1-2	0.36
4-7	0.37
0-4	0.38

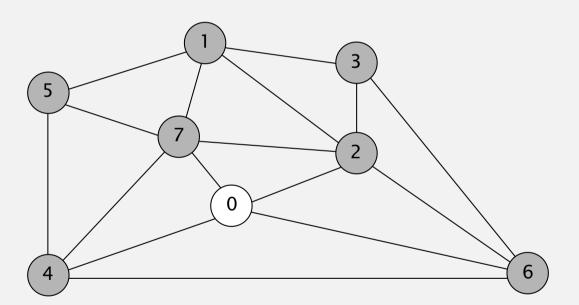
6-2 0.40

3-6 0.52

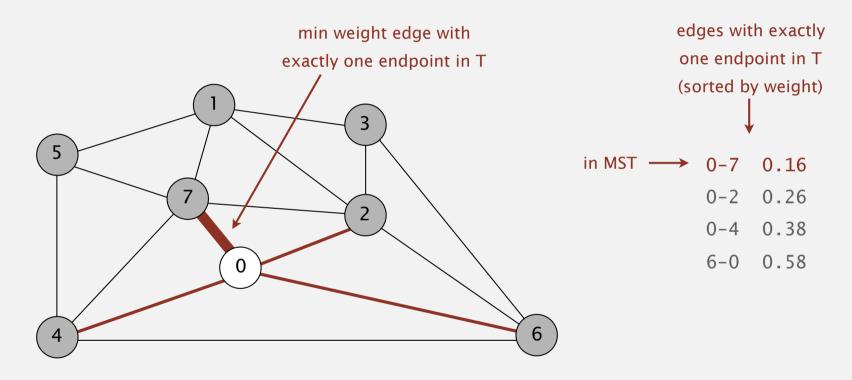
6-0 0.58

6-4 0.93

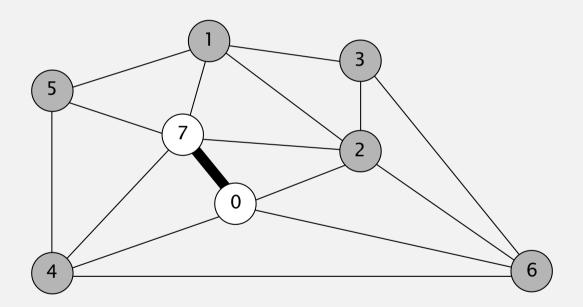
- Start with vertex 0 and greedily grow tree T.
- Add to *T* the min weight edge with exactly one endpoint in *T*.
- Repeat until V 1 edges.



- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

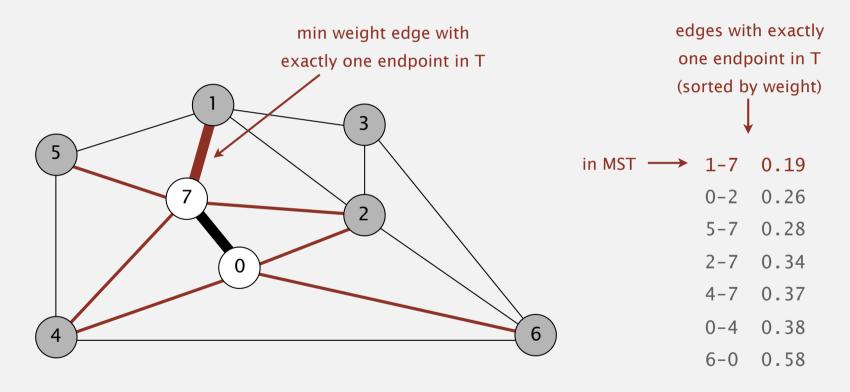


- Start with vertex 0 and greedily grow tree T.
- Add to *T* the min weight edge with exactly one endpoint in *T*.
- Repeat until V-1 edges.



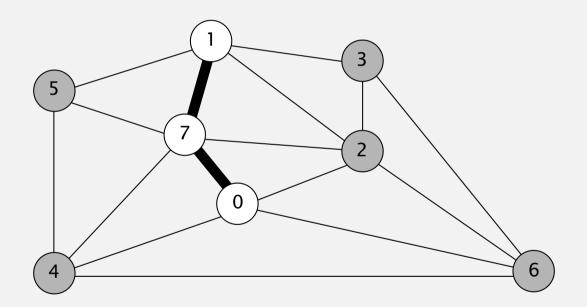
MST edges

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



MST edges

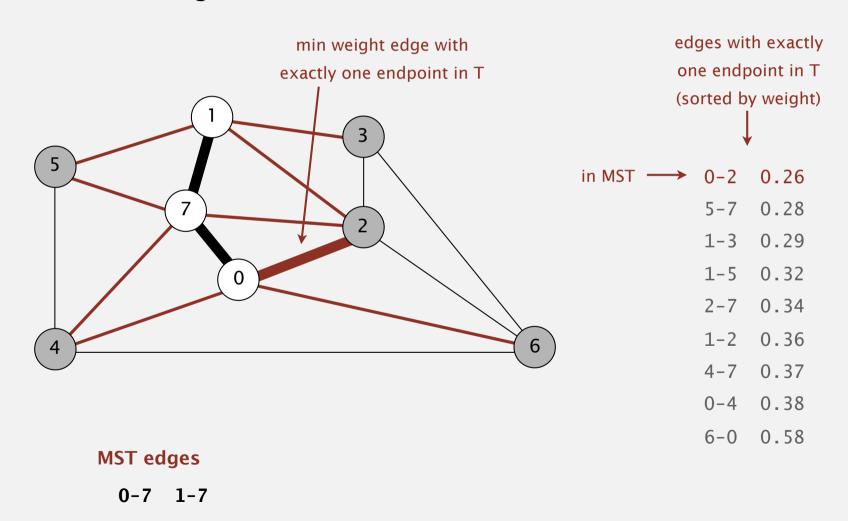
- Start with vertex 0 and greedily grow tree T.
- Add to *T* the min weight edge with exactly one endpoint in *T*.
- Repeat until V-1 edges.



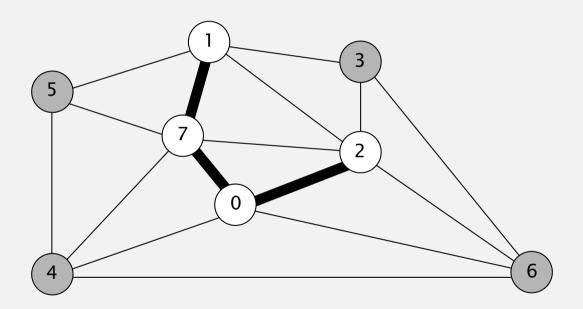
MST edges

0-7 1-7

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V-1 edges.



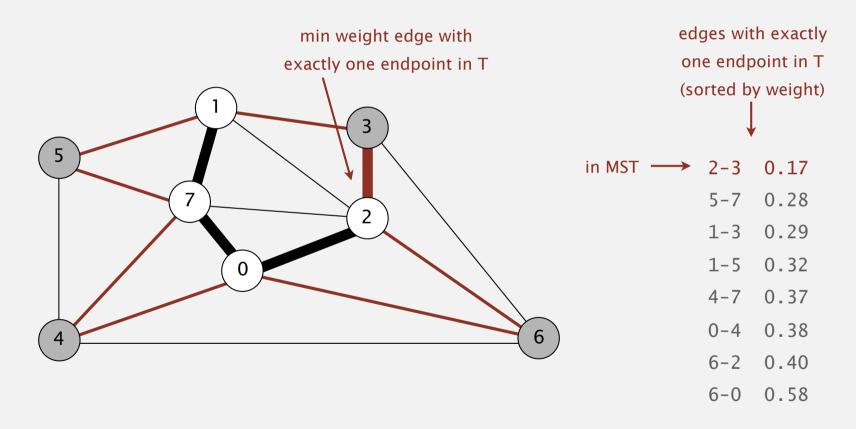
- Start with vertex 0 and greedily grow tree T.
- Add to *T* the min weight edge with exactly one endpoint in *T*.
- Repeat until V-1 edges.



MST edges

0-7 1-7 0-2

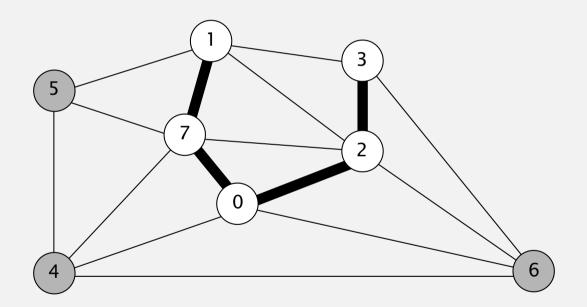
- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V-1 edges.



MST edges

0-7 1-7 0-2

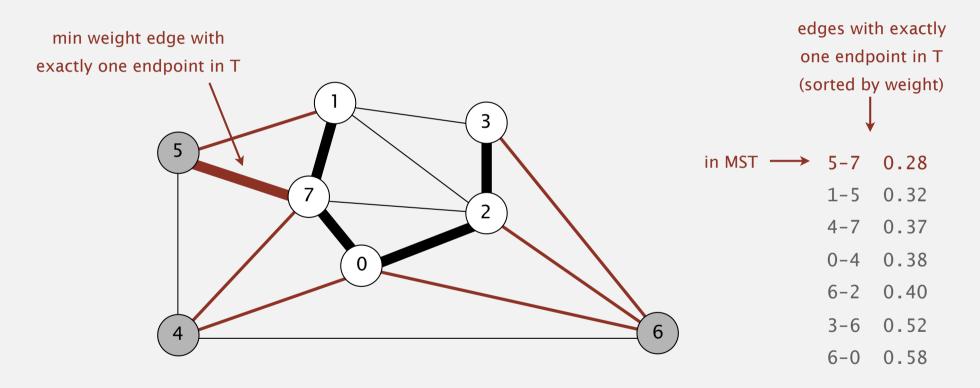
- Start with vertex 0 and greedily grow tree T.
- Add to *T* the min weight edge with exactly one endpoint in *T*.
- Repeat until V-1 edges.



MST edges

0-7 1-7 0-2 2-3

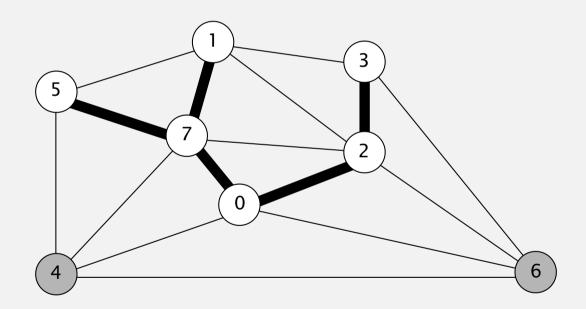
- Start with vertex 0 and greedily grow tree *T*.
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- Repeat until V 1 edges.



MST edges

0-7 1-7 0-2 2-3

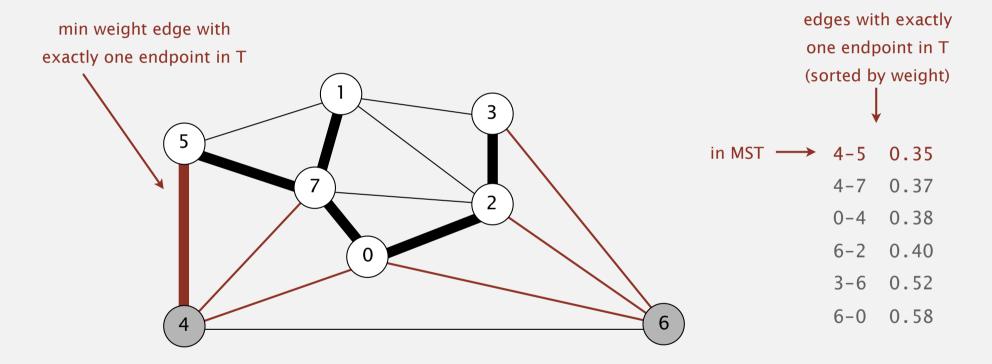
- Start with vertex 0 and greedily grow tree T.
- Add to *T* the min weight edge with exactly one endpoint in *T*.
- Repeat until V-1 edges.



MST edges

0-7 1-7 0-2 2-3 5-7

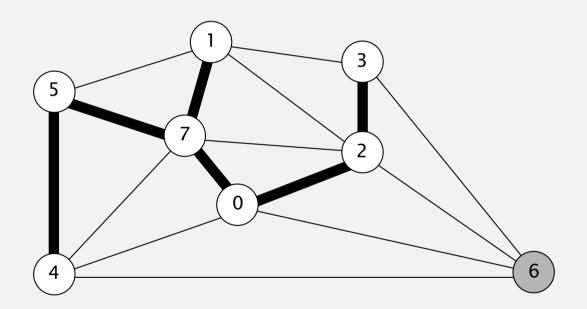
- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
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MST edges

0-7 1-7 0-2 2-3 5-7

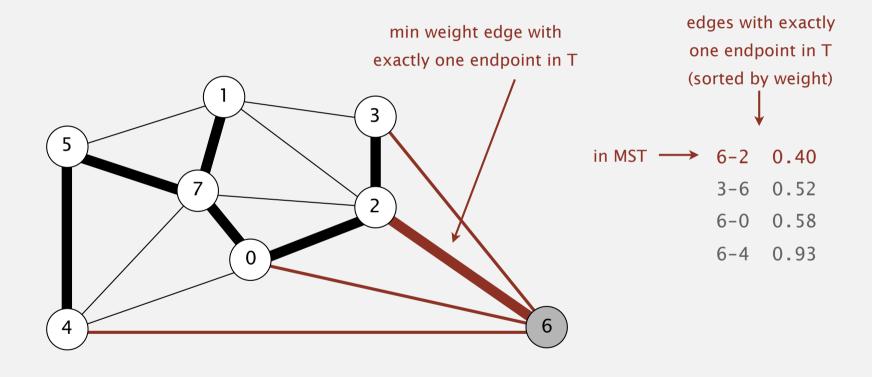
- Start with vertex 0 and greedily grow tree *T*.
- Add to *T* the min weight edge with exactly one endpoint in *T*.
- Repeat until V-1 edges.



MST edges

0-7 1-7 0-2 2-3 5-7 4-5

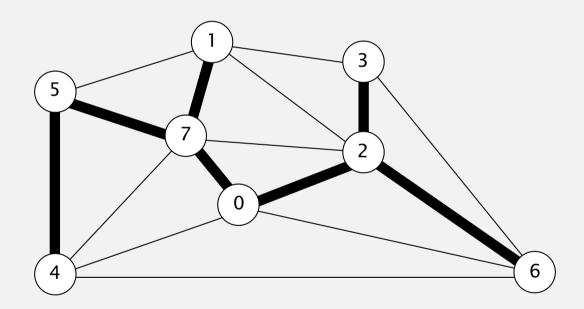
- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



MST edges

0-7 1-7 0-2 2-3 5-7 4-5

- Start with vertex 0 and greedily grow tree *T*.
- Add to *T* the min weight edge with exactly one endpoint in *T*.
- Repeat until V-1 edges.



MST edges

0-7 1-7 0-2 2-3 5-7 4-5 6-2

PRIM'S ALGORITHM DEMO

Prim's algorithm

lazy implementation

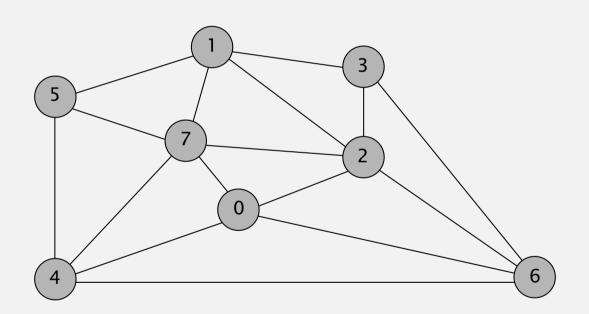
eager implementation

Algorithms

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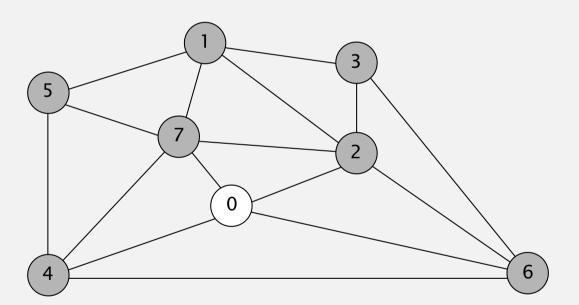
- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V-1 edges.



an edge-weighted graph

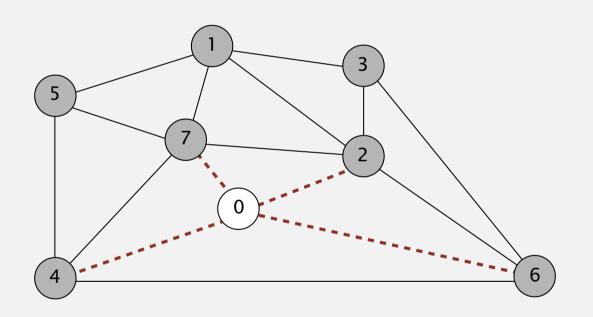
- 0-7 0.16
- 2-3 0.17
- 1-7 0.19
- 0-2 0.26
- 5-7 0.28
- 1-3 0.29
- 1-5 0.32
- 2-7 0.34
- 4-5 0.35
- 1-2 0.36
- 4-7 0.37
- 0-4 0.38
- 6-2 0.40
- 3-6 0.52
- 6-0 0.58
- $6-4 \quad 0.93$

- Start with vertex 0 and greedily grow tree *T*.
- Add to *T* the min weight edge with exactly one endpoint in *T*.
- Repeat until V-1 edges.



- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V-1 edges.

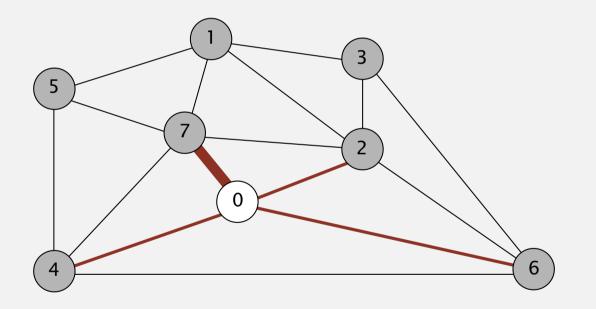
add to PQ all edges incident to 0



- * 0-7 0.16
- * 0-2 0.26
- * 0-4 0.38
- ***** 6-0 0.58

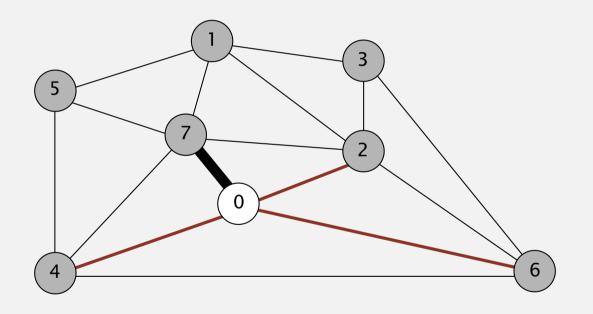
- Start with vertex 0 and greedily grow tree *T*.
- Add to *T* the min weight edge with exactly one endpoint in *T*.
- Repeat until V-1 edges.

delete 0-7 and add to MST



edges on PQ		
(sorted by weight)		
0-7	0.16	
0-2	0.26	
0-4	0.38	
6-0	0.58	

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V-1 edges.



edges on PQ (sorted by weight)

0-2 0.26

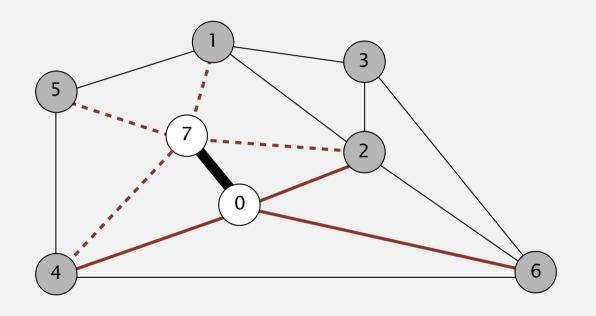
0-4 0.38

6-0 0.58

MST edges

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

add to PQ all edges incident to 7



edges on PQ (sorted by weight)

* 1-7 0.19

0-2 0.26

***** 5-7 0.28

***** 2-7 0.34

***** 4-7 0.37

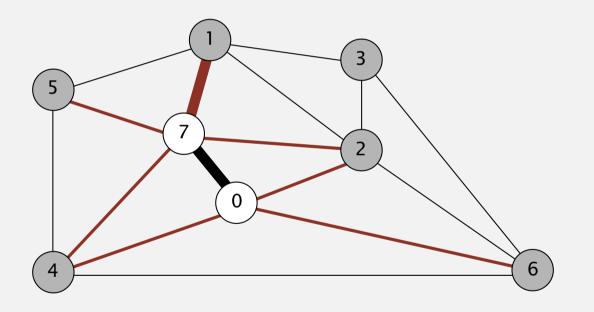
0-4 0.38

6-0 0.58

MST edges

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V-1 edges.

delete 1-7 and add to MST



edges on PQ (sorted by weight)

1-7 0.19

0-2 0.26

5-7 0.28

2-7 0.34

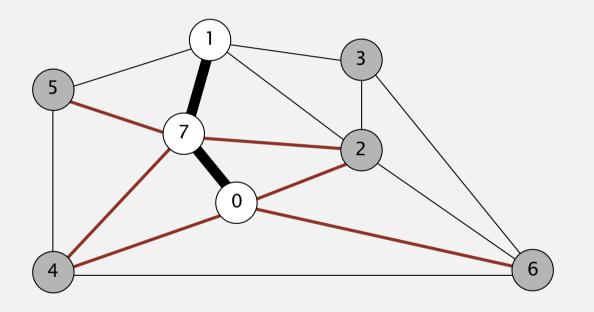
4-7 0.37

0-4 0.38

6-0 0.58

MST edges

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V-1 edges.



edges on PQ (sorted by weight)

0-2 0.26

5-7 0.28

2-7 0.34

4-7 0.37

0-4 0.38

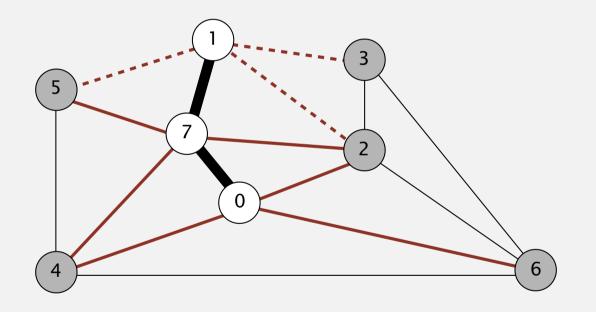
6-0 0.58

MST edges

0-7 1-7

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

add to PQ all edges incident to 1



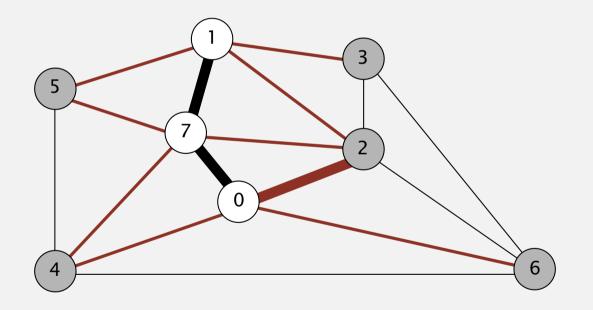
MST edges

0-7 1-7

0-2	Λ	. 26
()-/		. <i>/</i> n

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

delete edge 0-2 and add to MST

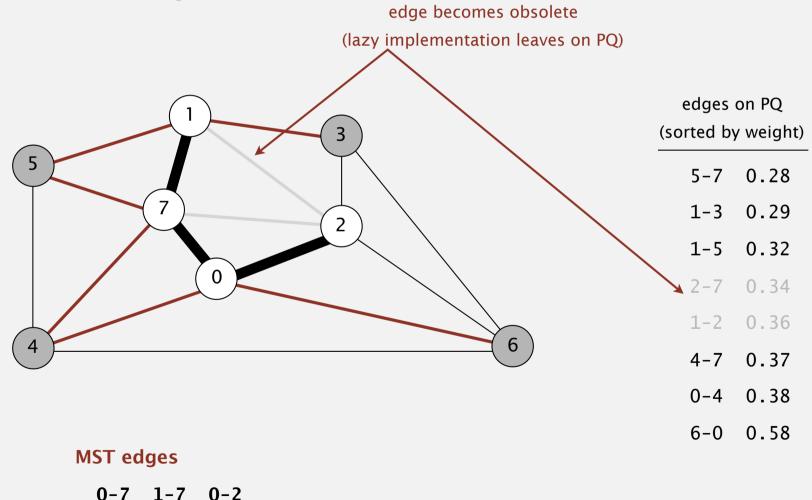


MST edges

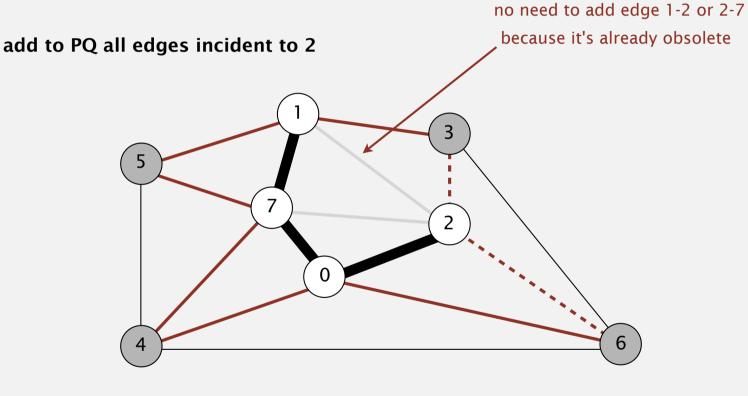
0-7 1-7

edges on PQ (sorted by weight) 0-2 0.26 5-7 0.28 1-3 0.29 1-5 0.32 2-7 0.34 1-2 0.36 4-7 0.37 0-4 0.386-0 0.58

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



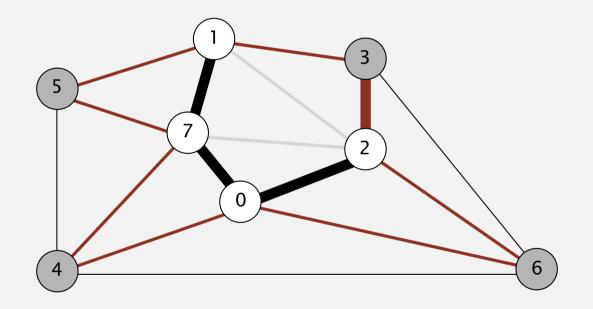
MST edges

0-7 1-7 0-2

*	2-3	0	17

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V-1 edges.

delete 2-3 and add to MST

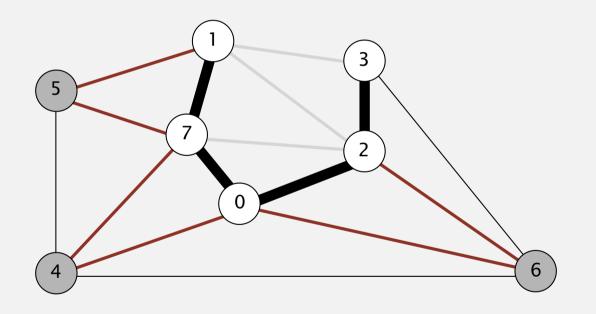


MST edges

0-7 1-7 0-2

- ***** 2-3 0.17
 - 5-7 0.28
 - 1-3 0.29
 - 1-5 0.32
 - 2-7 0.34
 - 1-2 0.36
 - 4-7 0.37
 - 0-4 0.38
- * 6-2 0.40
 - 6-0 0.58

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V-1 edges.



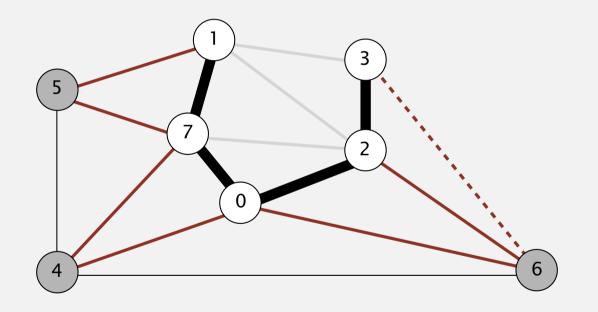
MST edges

0-7 1-7 0-2 2-3

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5- /	()	/X
<i></i>	•	

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

add to PQ all edges incident to 3



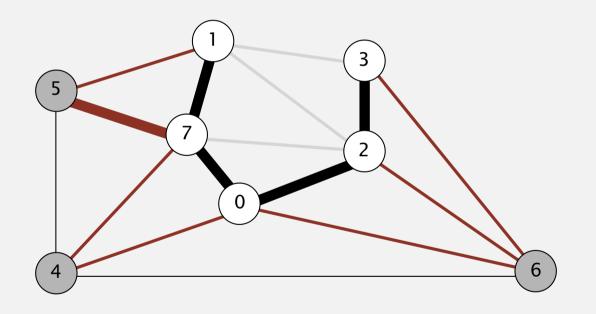
MST edges

0-7 1-7 0-2 2-3

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5-7	()	/X
<i>J</i> 1	•	

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

delete 5-7 and add to MST



MST edges

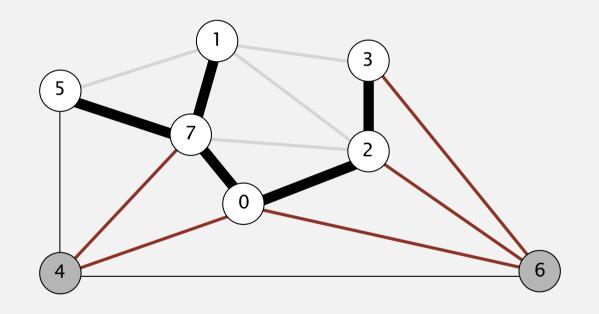
0-7 1-7 0-2 2-3

	_	~ ~
5-/	0.	28

$$1-3 \quad 0.29$$

$$6-2$$
 0.40

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V-1 edges.



MST edges

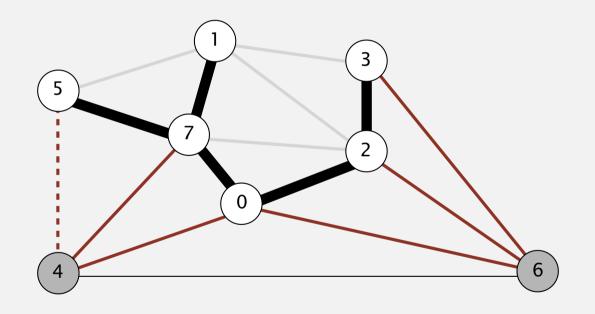
0-7 1-7 0-2 2-3 5-7

- 1	-3		20
	- <	()	79

$$6-2$$
 0.40

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V-1 edges.

add to PQ all edges incident to 5



MST edges

0-7 1-7 0-2 2-3 5-7

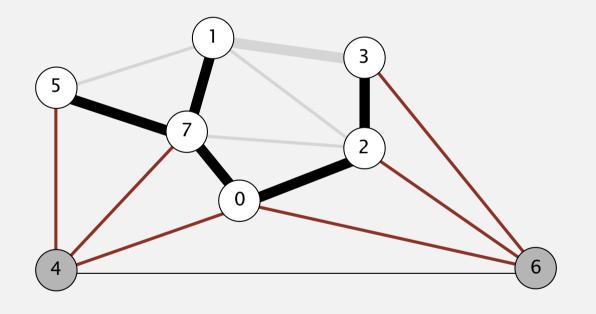
edges on PQ (sorted by weight)

1	_3	\cap	29

$$1-5$$
 0.32

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

delete 1-3 and discard obsolete edge



MST edges

0-7 1-7 0-2 2-3 5-7

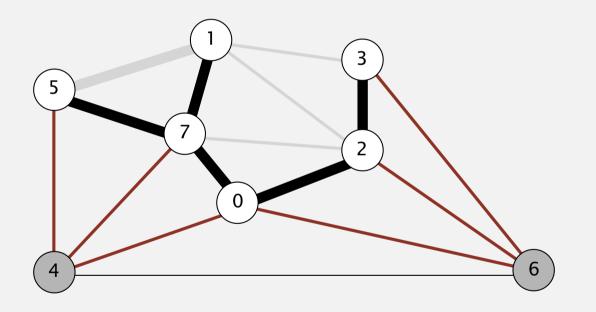
edges on PQ (sorted by weight)

- 1	_ 3	\cap	20

$$6-2$$
 0.40

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

delete 1-5 and discard obsolete edge



MST edges

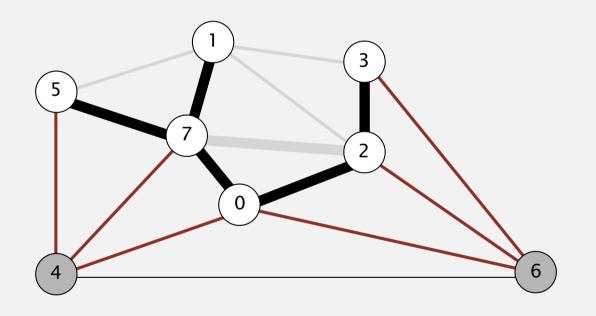
0-7 1-7 0-2 2-3 5-7

edges on PQ (sorted by weight)

1	_ 5	\cap	37

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V-1 edges.

delete 2-7 and discard obsolete edge



edges on PQ (sorted by weight)

2-7 0.34

4-5 0.35

1-2 0.36

4-7 0.37

0-4 0.38

6-2 0.40

3-6 0.52

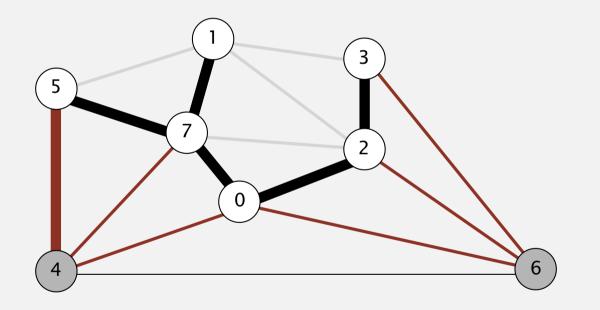
6-0 0.58

MST edges

0-7 1-7 0-2 2-3 5-7

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

delete 4-5 and add to MST



edges on PQ (sorted by weight)

4-5 0.35

1-2 0.36

4-7 0.37

0-4 0.38

6-2 0.40

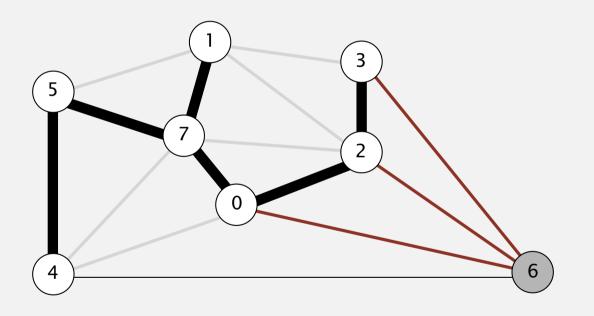
3-6 0.52

6-0 0.58

MST edges

0-7 1-7 0-2 2-3 5-7

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V-1 edges.



edges on PQ (sorted by weight)

1-2 0.36

4-7 0.37

0-4 0.38

6-2 0.40

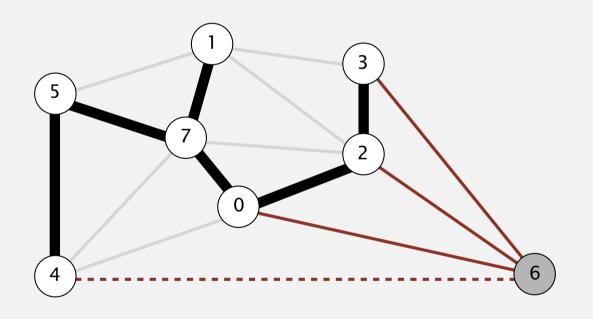
3-6 0.52

6-0 0.58

MST edges

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

add to PQ all edges incident to 4



edges on PQ (sorted by weight)

1-2 0.36

4-7 0.37

0-4 0.38

6-2 0.40

3-6 0.52

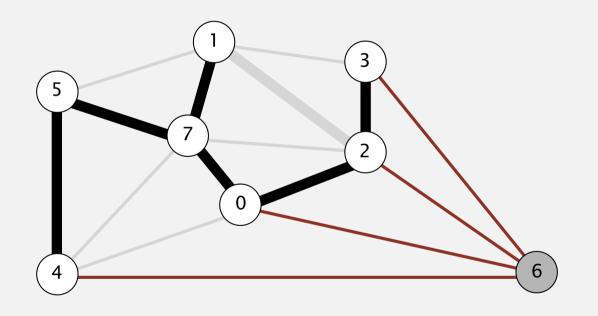
6-0 0.58

***** 6-4 0.93

MST edges

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V-1 edges.

delete 1-2 and discard obsolete edge



edges on PQ (sorted by weight)

1-2 0.36

4-7 0.37

0-4 0.38

6-2 0.40

3-6 0.52

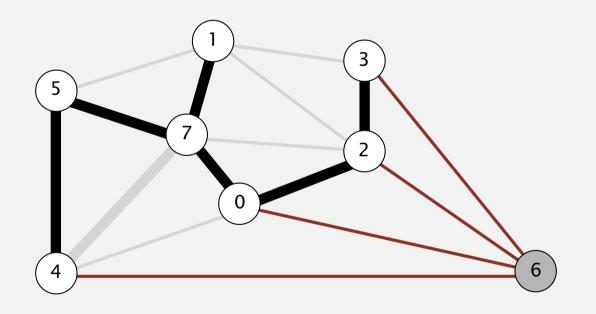
6-0 0.58

6-4 0.93

MST edges

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

delete 4-7 and discard obsolete edge



edges on PQ (sorted by weight)

4-7 0.37

0-4 0.38

6-2 0.40

3-6 0.52

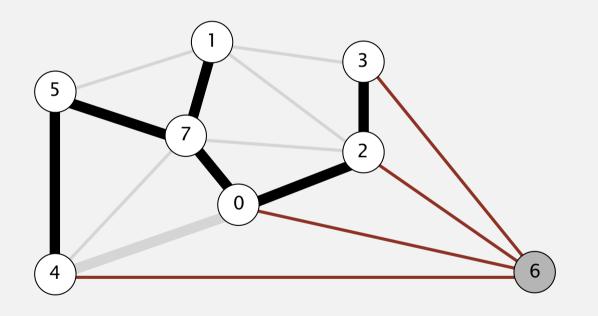
6-0 0.58

6-4 0.93

MST edges

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V-1 edges.

delete 0-4 and discard obsolete edge



edges on PQ (sorted by weight)

0-4 0.38

6-2 0.40

3-6 0.52

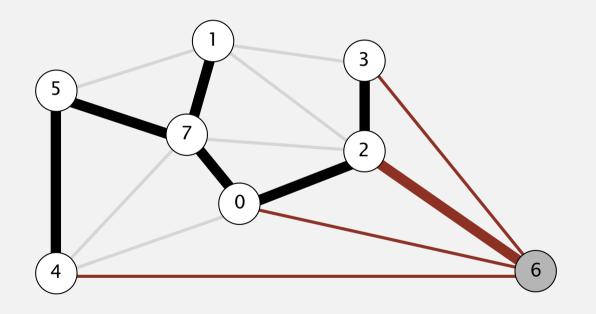
6-0 0.58

6-4 0.93

MST edges

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V-1 edges.

delete 6-2 and add to MST



edges on PQ (sorted by weight)

6-2 0.40

3-6 0.52

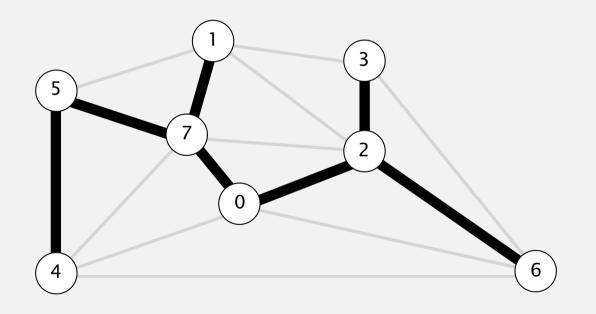
6-0 0.58

6-4 0.93

MST edges

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

delete 6-2 and add to MST



edges on PQ (sorted by weight)

3-6 0.52

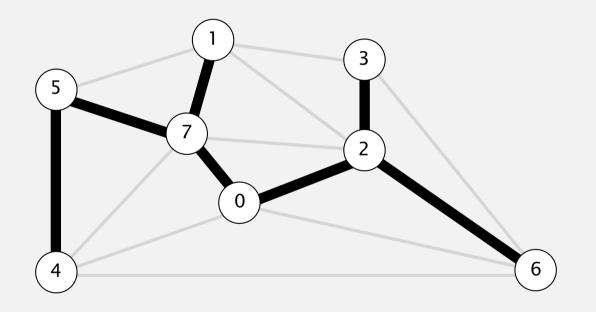
6-0 0.58

 $6-4 \quad 0.93$

MST edges

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V-1 edges.

stop since V-1 edges



edges on PQ (sorted by weight)

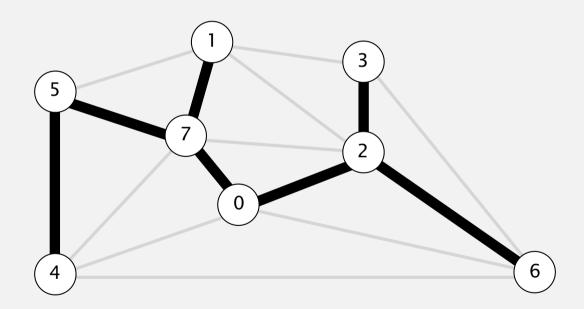
3-6 0.52

6-0 0.58

 $6-4 \quad 0.93$

MST edges

- Start with vertex 0 and greedily grow tree *T*.
- Add to *T* the min weight edge with exactly one endpoint in *T*.
- Repeat until V-1 edges.



MST edges

PRIM'S ALGORITHM DEMO

Prim's algorithm

Jazy implementation

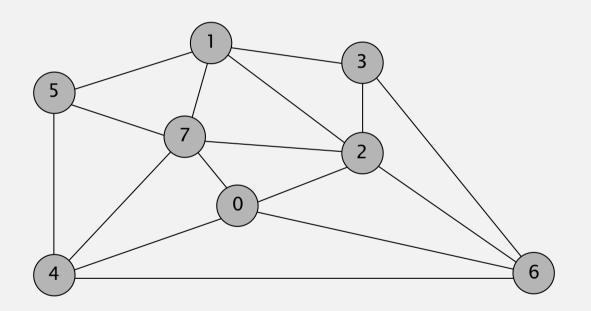
eager implementation



ROBERT SEDGEWICK | KEVIN WAYNE

http://algs4.cs.princeton.edu

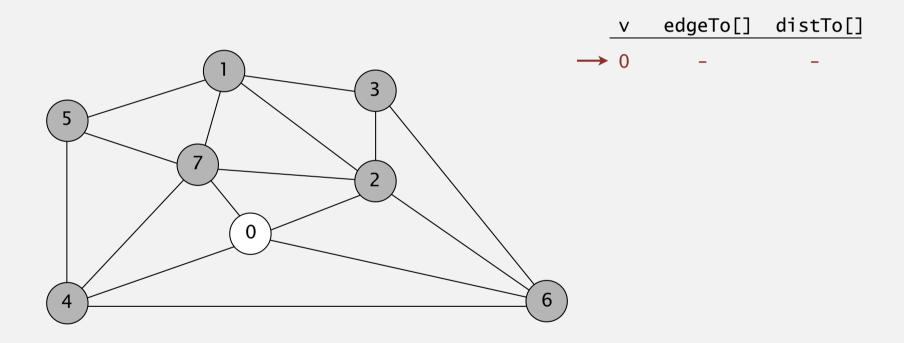
- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V-1 edges.



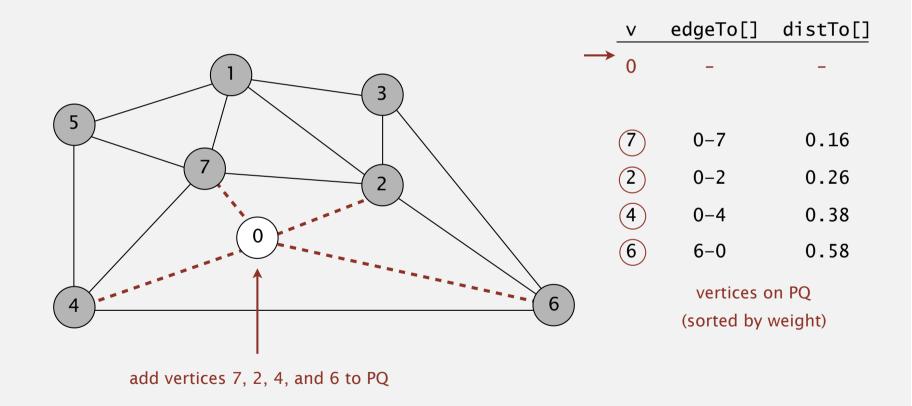
an edge-weighted graph

- 0-7 0.16
- 2-3 0.17
- 1-7 0.19
- 0-2 0.26
- 5-7 0.28
- 1-3 0.29
- 1-5 0.32
- 2-7 0.34
- 4-5 0.35
- 1-2 0.36
- 4-7 0.37
- 0-4 0.38
- 6-2 0.40
- 3-6 0.52
- 6-0 0.58
- 6-4 0.93

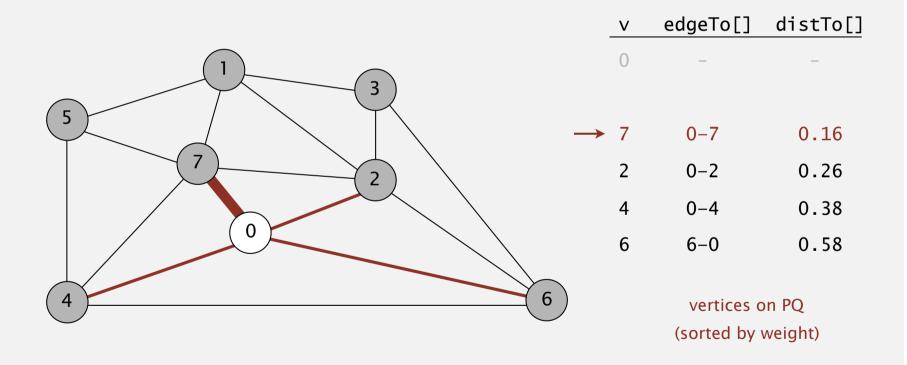
- Start with vertex 0 and greedily grow tree *T*.
- Add to *T* the min weight edge with exactly one endpoint in *T*.
- Repeat until V-1 edges.



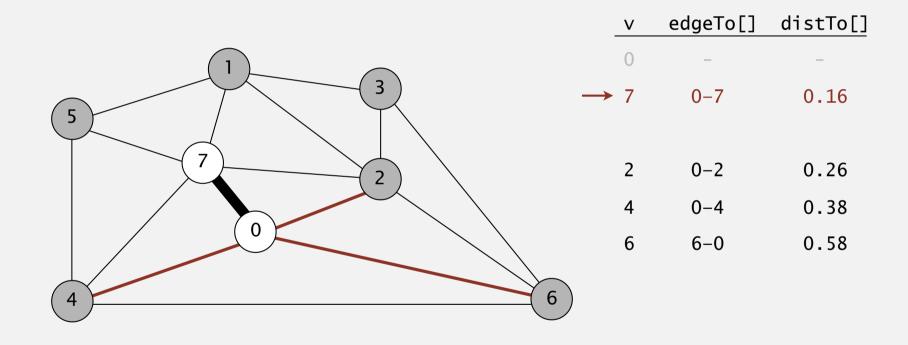
- Start with vertex 0 and greedily grow tree *T*.
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- Repeat until V-1 edges.



- Start with vertex 0 and greedily grow tree *T*.
- Add to *T* the min weight edge with exactly one endpoint in *T*.
- Repeat until V 1 edges.



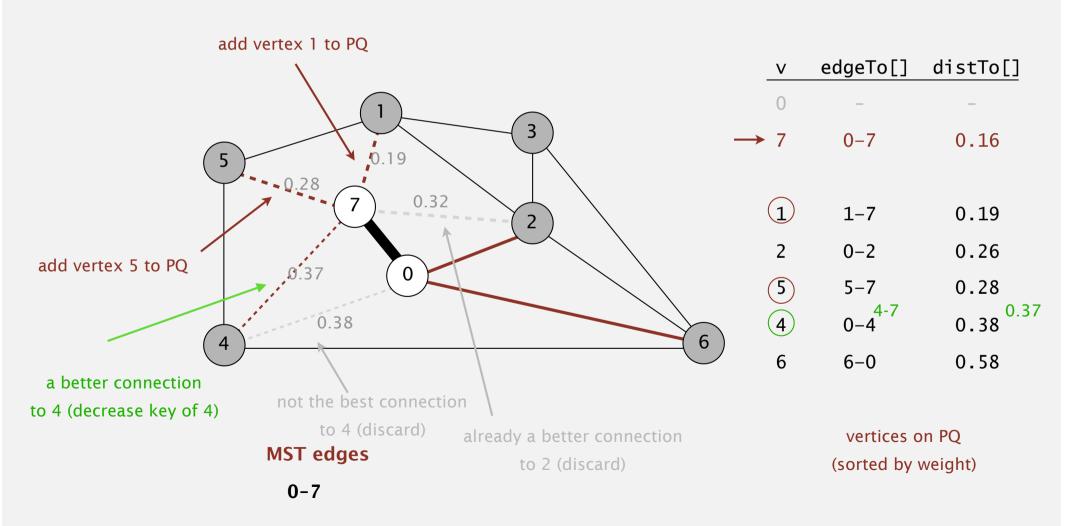
- Start with vertex 0 and greedily grow tree *T*.
- Add to *T* the min weight edge with exactly one endpoint in *T*.
- Repeat until V-1 edges.



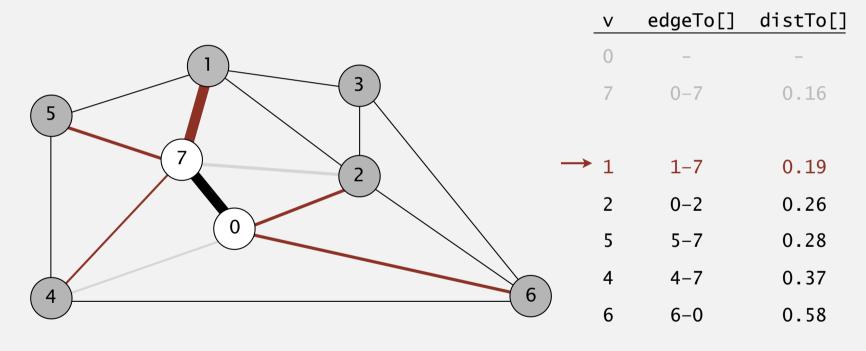
MST edges

0-7

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

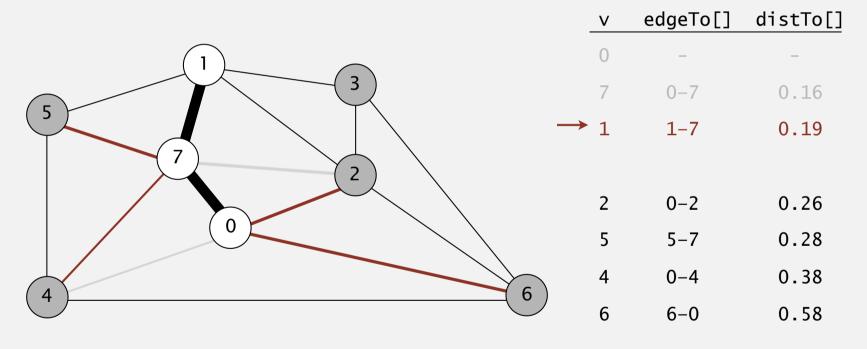


MST edges

0-7 1-7

vertices on PQ (sorted by weight)

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

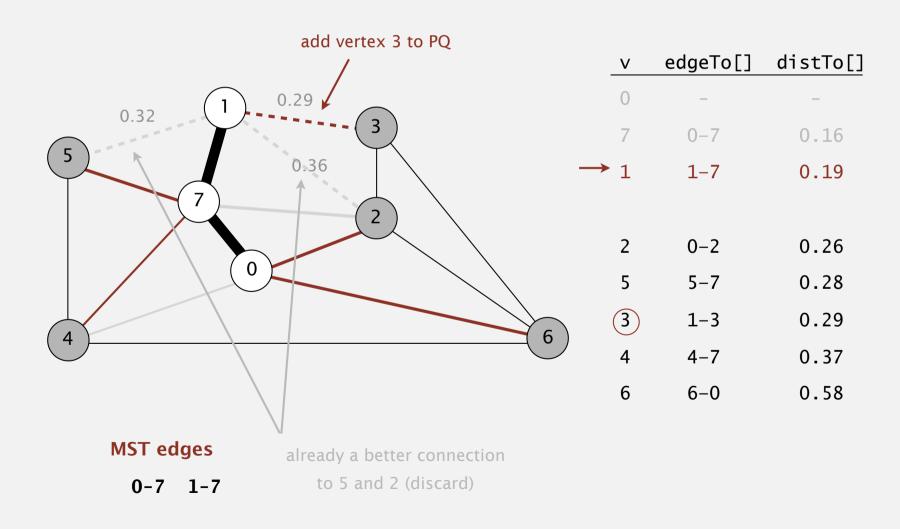


MST edges

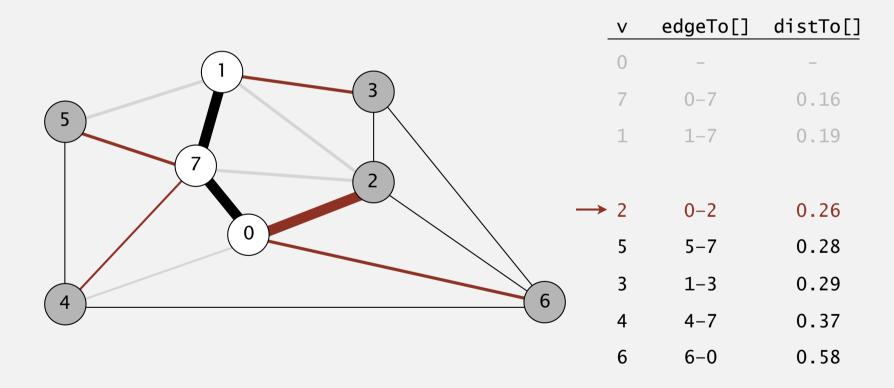
0-7 1-7

vertices on PQ (sorted by weight)

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



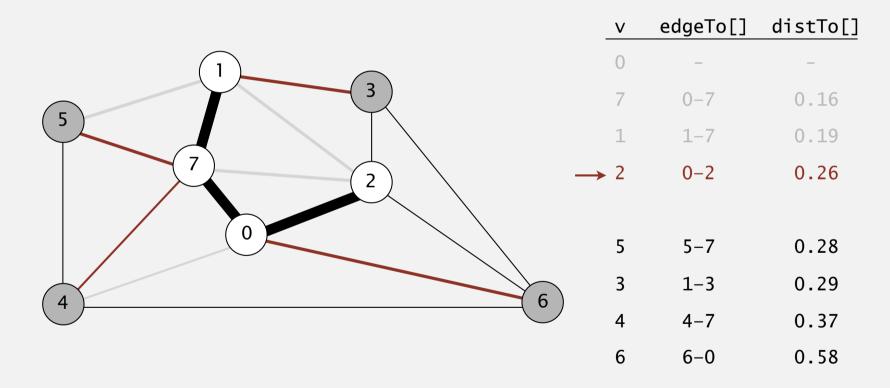
- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



MST edges

0-7 1-7

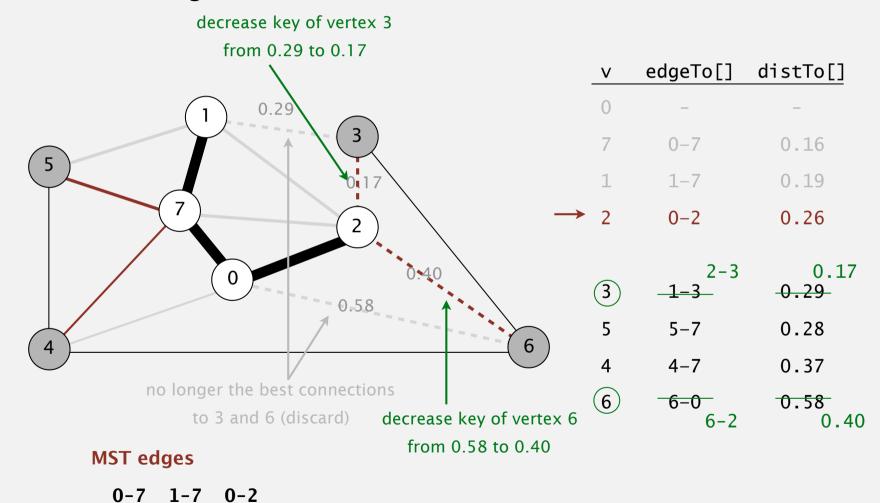
- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



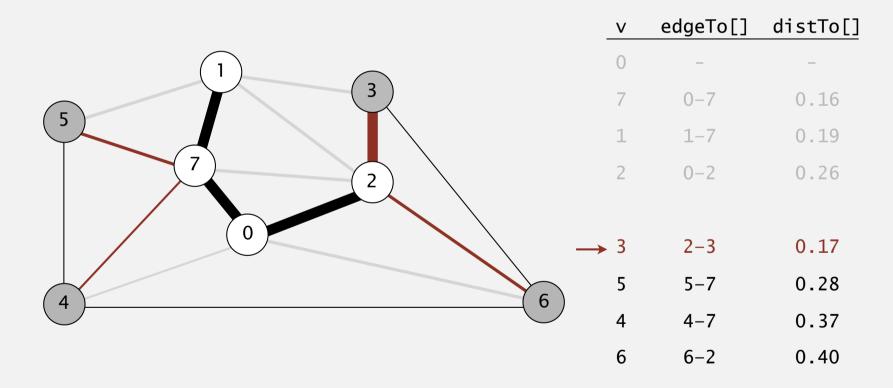
MST edges

0-7 1-7 0-2

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V-1 edges.



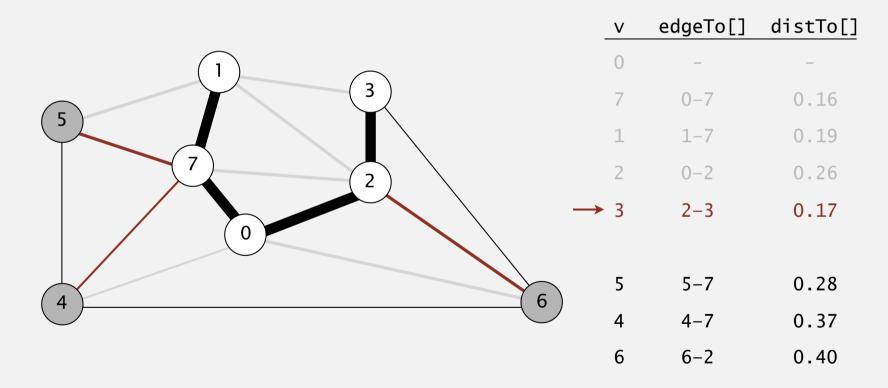
- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



MST edges

0-7 1-7 0-2 2-3

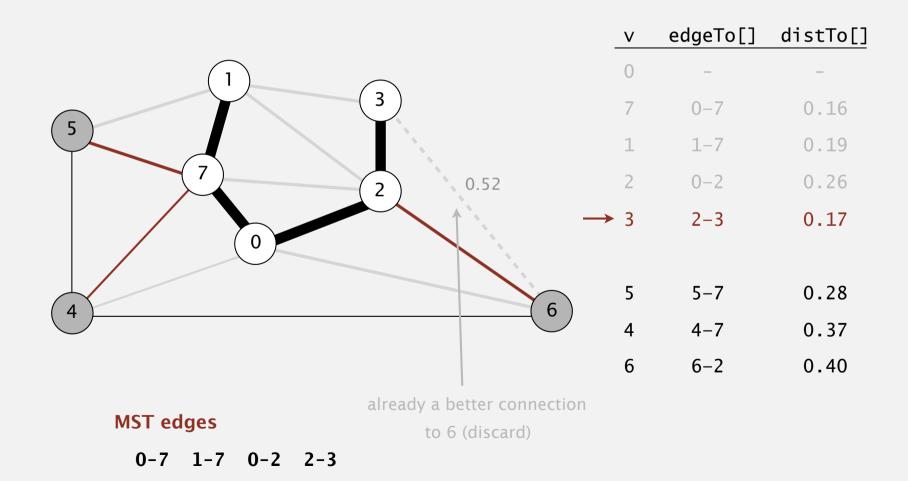
- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



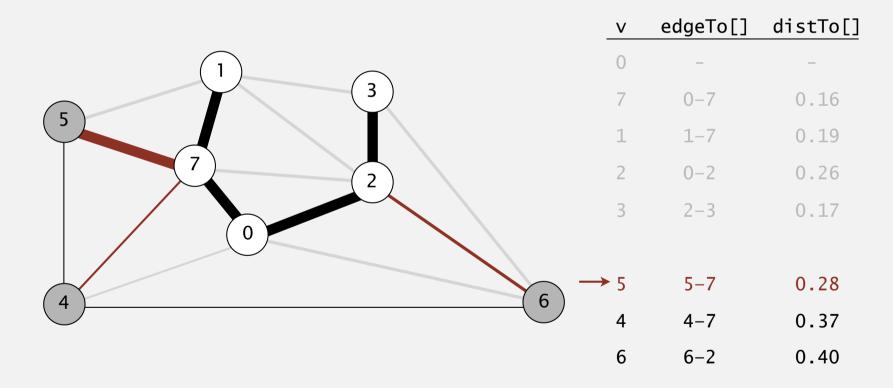
MST edges

0-7 1-7 0-2 2-3

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V-1 edges.



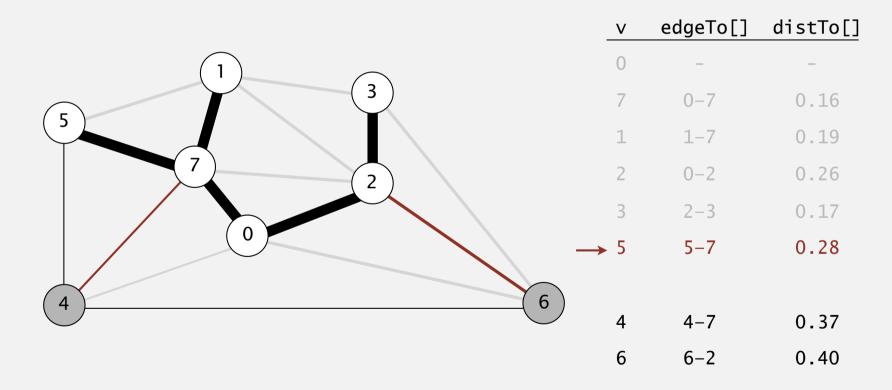
- Start with vertex 0 and greedily grow tree *T*.
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- Repeat until V-1 edges.



MST edges

0-7 1-7 0-2 2-3

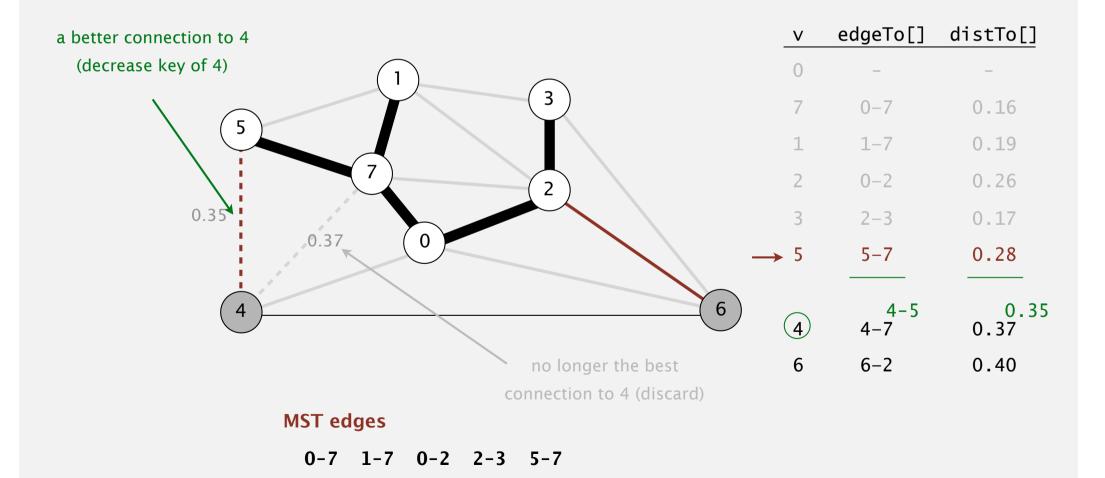
- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V-1 edges.



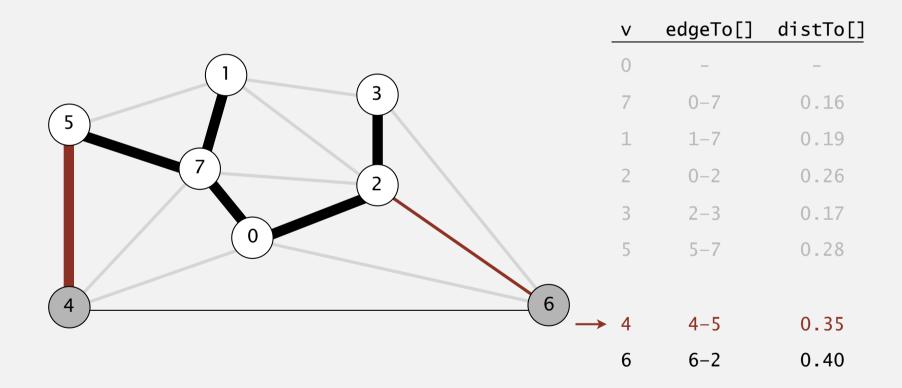
MST edges

0-7 1-7 0-2 2-3 5-7

- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



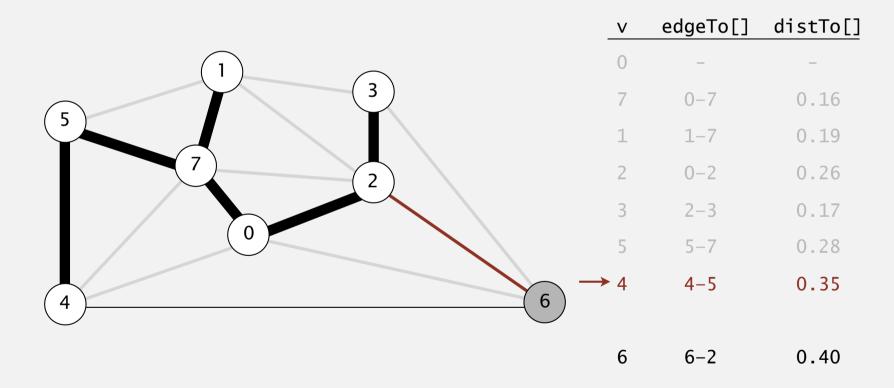
- Start with vertex 0 and greedily grow tree *T*.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V-1 edges.



MST edges

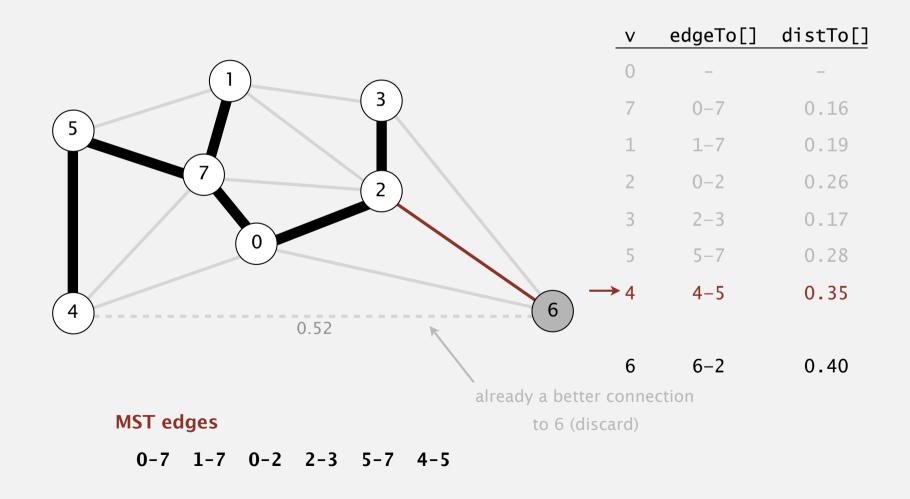
0-7 1-7 0-2 2-3 5-7

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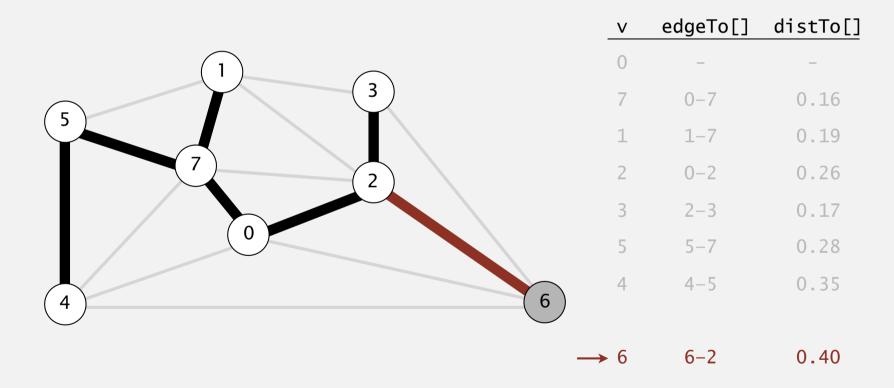


MST edges

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- Add to T the min weight edge with exactly one endpoint in T.
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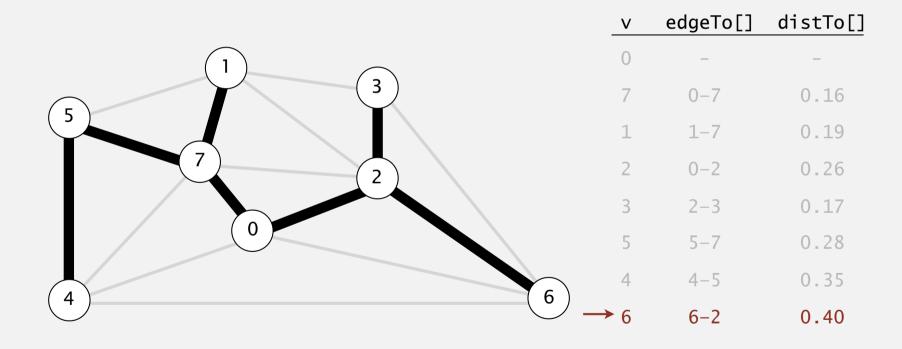


- Start with vertex 0 and greedily grow tree *T*.
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- Repeat until V-1 edges.



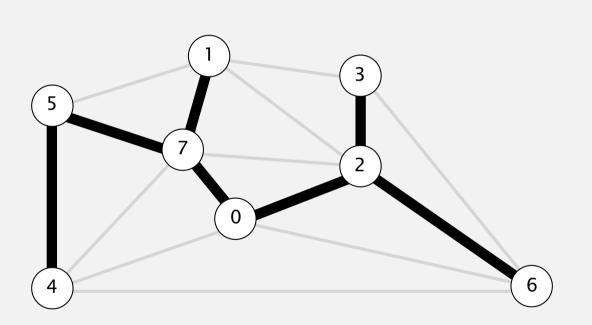
MST edges

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MST edges

- Start with vertex 0 and greedily grow tree *T*.
- Add to *T* the min weight edge with exactly one endpoint in *T*.
- Repeat until V-1 edges.



V	edgeTo[]	distTo[]
0	-	-
7	0-7	0.16
1	1-7	0.19
2	0-2	0.26
3	2–3	0.17
5	5-7	0.28
4	4–5	0.35
6	6–2	0.40

MST edges